## END-TERM EXAMINATIONS - TERM TWO

121/2- MATHEMATICS ALT. A
Paper 2
FORM 3
Time-2 $1 / 2$ Hours

(a) Write your name, admission number, school and class in the spaces provided at the top of this page.
(b) Sign and write the date of the examination in the spaces provided above.
(c) This paper consists of two sections: Section I and Section II.
(d) Answer ALL questions in Section I and all the questions from Section II.
(e) Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.
(f) Marks may be given for correct working even if the answer is wrong.
(g) Non-programmable silent electronic calculators and KNEC Mathematical Tables may be used.
(h) Candidates should check the question paper to ensure that all, the pages are printed as indicated and no questions are missing.

## For Examiners' Use Only

## SECTION I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## SECTION II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |
| Grand Total |  |  |  |  |  |  |  |  |

## Answer all questions in this section in the spaces provide.

1. Use logarithms to evaluate to 4 significant figures

$$
\frac{(0.5241)^{2} \times 83.59}{\sqrt[3]{0.23+0.126}}
$$

2. The height of a cone is exactly 12 cm . Calculate the percentage error in the volume if the radius is 7 cm correct to the nearest centimeter.
3. Make $h$ the subject of the formula

$$
V=\sqrt[3]{\frac{a x^{2} h}{b-h}}
$$

4. $\mathbf{Z}$ is directly proportional to $\mathbf{x}^{2}$ and inversely proportional to $\mathbf{y}$. If $\mathbf{x}$ is increased by $20 \%$ and $\mathbf{y}$ is decreased by $20 \%$. Find the percentage change in $\mathbf{Z}$.
5. Given that $\mathrm{OA}=3 \mathrm{i}+2 \mathrm{j}_{\sim}-\underset{\sim}{4} \mathrm{k} \underset{\sim}{\text { and }} \mathrm{OB}=4 \mathrm{i}+5 \mathrm{j}-\underset{\sim}{2 k} \underset{\sim}{\text { and }}$ a point $\mathbf{P}$ divides line $\mathbf{A B}$ externally in the ratio 3:2, determine the magnitude of $\mathbf{O P}$ to 2 decimal places
6. Given that $2 \cos \left(2 x-30^{\circ}\right)=-\frac{6}{5}$ find x where $180^{\circ} \leq x \leq 360^{\circ}$
(3 marks)
7. Irene buys a printer on hire purchase. She pays a deposit of sh. 4000 and 12 monthly installments of sh. 1500 each. Calculate the cash price if a compound interest of $5 \%$ per month is charged on the amount borrowed.
(3 marks)
8. Find the value of $\boldsymbol{x}$ in the equation

$$
\log (15-5 x)-\log (3 x-2)-2=0
$$


9. Rationalize the denominator and simplify

$$
\frac{4}{\sqrt{5+\sqrt{ } 2}}-\frac{3}{\sqrt{5}-\sqrt{2}}
$$

10. Given that $\mathbf{A}=\left[\begin{array}{lll}\mathbf{1} & \mathbf{O 1} \\ 3 & \mathbf{0}\end{array}\right] \quad$ and $\quad \mathbf{B}=\left[\begin{array}{ll}4 & 2 \\ 9 & 6\end{array}\right]$

Find $\mathrm{A}^{-1} \mathrm{~B}$
(3 marks)
11. Solve the equation $2 x^{2}+3 x=5$ by completing the square method.

12. The number of birds in a sanctuary was originally 1.2 million. Due to a mysterious diseases this number halved itself after every one week. Determine the number of birds remaining in the sanctuary at the end of the 5th week.
13. Simplify the expression
$\frac{3 x^{2}-4 x y+y^{2}}{9 x^{2}-y^{2}}$
15. The cost of an article is sh. 1,200. Find the rate of inflation if the cost of the article after 5 years is sh. 1,932.60.
16. The product of the third and fourth terms of an arithmetic sequence is 3000 . Find the first term if the common difference is 10 .
(3 marks)


Answer any five questions from this section in the spaces provided after each.
17. (a) Complete the table below for the function $y=2 x^{2}+4 x-3$

| X | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $2 \mathrm{x}^{2}$ | 32 |  | 8 | 2 | 0 | 2 |  |
| $4 \mathrm{x}-3$ |  |  | -11 |  | -3 |  |  |
| Y |  |  | -3 |  |  | 3 | 13 |

(b) Draw the graph of the function $y=2 x^{2}+4 x-3$ on the grid provided. Use the scale: 2 cm rep 1 unit on the x -axis and 1 cm rep 2 units on the y -axis.

(c) Use your graph to estimate the roots of the equation $2 x^{2}+4 x-3=0$
(d) Use your graph to obtain the roots of the equation $2 x^{2}+x-5=0$ to 1 decimal place.
(e) Draw the line of symmetry to pass through the turning point of this curve.
18. The table below shows how income tax was charged on income earned in a certain year.

| Taxable income per <br> year(Kenyan shillings) | Rate |
| :---: | :---: |
| $1-72,600$ | $10 \%$ |
| $72,601-145,200$ | $15 \%$ |
| $145,201-217,800$ | $20 \%$ |
| $217,801-290,400$ | $25 \%$ |

Mr. Mwongula is an employee of a certain company and earns a salary of ksh. 15,200 per month. He is housed by the company and pays a nominal rent of Ksh. 1050 per month. He is married and is entitled to a family relief of ksh. 450 per month.
i. Calculate his taxable income in Ksh p.a
ii. Calculate his gross tax per month.
19. The figure below is a cyclic quadrilateral $\operatorname{PQRS}$. Given that TRX is a tangent at $\mathbf{R}$ and $\mathbf{O}$ is the centre of the circle and that $\mathbf{P S X}$ is a straight line. Angle $\mathbf{P R S}=50^{\circ}$ and angle $\mathbf{Q P R}=30^{\circ}$ and chord $\mathbf{R S}=\mathrm{PS}$.

(a) Giving reason in each case, find;
(i) Angle SRX
(ii) Angle RXS
(iii) Angle PQR
(iv) Reflex angle QOR
(b) Given that $\mathbf{R X}=12 \mathrm{~cm}, \mathbf{S X}=8 \mathrm{~cm}$, find the length of chord PS
20. The first term of a G.P is 1 while the first term of an $\mathbf{A P}$ is 4. The third term of the $\mathbf{G . P}$ is the first term of the $\mathbf{A P}$. The ratio of the common difference to the common ratio of the progression is 3:2 (Common ratio is greater than O ). Find;
(a) The common ratio of the G.P and common difference of the A.P
(b) The fifth term of the A.P
(c) The $6^{\text {th }}$ term of the G.P
(d) The sum of the first four terms of the G.P.
21. (a) Complete the table below for the functions $y=3 \sin (2 x-30)$ and $y=\cos (x+60)$ in the domain $-180^{\circ} \leq \mathrm{x} \leq 180^{0}$
(2 marks)

| $\mathbf{x}^{\mathbf{0}}$ | $\mathbf{- 1 8 0}^{\mathbf{0}}$ | $\mathbf{- 1 5 0}$ | $\mathbf{- 1 2 0}$ | $\mathbf{- 9 0}^{\mathbf{0}}$ | $\mathbf{- 6 0 ^ { \mathbf { 0 } }}$ | $\mathbf{- 3 0}^{\mathbf{0}}$ | $\mathbf{0}^{\mathbf{0}}$ | $\mathbf{3 0}^{\mathbf{0}}$ | $\mathbf{6 0}^{\mathbf{0}}$ | $\mathbf{9 0}^{\mathbf{0}}$ | $\mathbf{1 2 0}^{\mathbf{0}}$ | $\mathbf{1 5 0}^{\mathbf{0}}$ | $\mathbf{1 8 0}^{\mathbf{0}}$ |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{y}=3 \sin (2 \mathrm{x}-30)$ | -1.5 |  |  | 1.5 | -1.5 |  |  | 1.5 | 3 |  |  | -3 |  |
| $\mathrm{y}=\cos (\mathrm{x}+60)$ | -0.5 |  |  | 0.87 | 1 |  |  | 0 | -0.5 |  |  | -0.87 |  |

(b) On the same axes draw the graphs of $y=3 \sin (2 x-30)$ and $y=\cos (x+60)$

Use the scale: 1 cm rep $30^{\circ}$ on the x -axis and 1 cm rep 1 unit on the y -axis.



(c) Use your graphs to solve:
(I) $3 \sin (2 x-30)^{0}=0$
(II) $\quad \cos (x+60)^{0}=0$
(III) $3 \sin (2 \mathrm{x}-30)^{0}-\cos (\mathrm{x}+60)^{0}=0$
22. In the figure below, E is the midpoint of $\mathrm{AB}, \mathrm{OD}: \mathrm{DB}=2: 3$ and f is the point of intersection of OE and AD .

O
D
B

Given $\mathbf{O A}=\boldsymbol{a}$ and $\mathbf{O B}=\boldsymbol{b}$
a) Express in terms of $\boldsymbol{a}$ and $\boldsymbol{b}$
i. $\mathbf{A D}$
ii. OE
b) Given that $\mathbf{A F}=s \mathbf{A D}$ and $\mathbf{O F}=\mathrm{t} \mathbf{O E}$ find the values of s and t

c) Show that E,F and O are collinear.
23. (a) A quantity P varies directly as the cube of Q and inversely as the square root of R . When $\mathrm{P}=189$, $\mathrm{Q}=6$ and $\mathrm{R}=16$. (i) Determine the value of P when $\mathrm{Q}=8$ and $\mathrm{R}=25$.
(ii) Find the percentage change in Q when P is increased by $15 \%$ and R is decreased in the ratio $4: 5$.
(b) The charge C shillings per person for a seminar in a hotel is partly fixed and partly varies inversely as the total number of persons attending the seminar. When 100 people attend, the charge is Ksh 2036 per person while when 80 people attend, the charge is Ksh 2045 per person. Calculate the charge per person when 200 people attend the seminar.
24.In an $n$-sided polygon, two angles are right angles and each of the remaining angles is $150^{\circ}$.
a) Find the value of $n$ hence the sum of interior angles of this polygon.
b) Name the polygon.
(1 mark)
c) Find the area of a regular octagon of sides 4 cm to 5 s.f.

