# MATHEMATICS TOPICAL QUESTIONS



# **ANSWERS**

# DISTRICTS SAMPLED AND COMPILED

- 1. NDHIWA
- 2. SOTIK
- 3. KAKAMEGA CENTRAL
- 4. NYAMIRA
- 5. HOMABAY
- 6. RACHUONYO
- 7. MIGORI
- 8. UGENYA/UGUNJA
- 9. KISUMU WEST
- 10. MATUNGU
- 11. BUTERE
- 12. KAKAMEGA EAST
- 13. NYATIKE
- 14. KHWISERO
- 15. TRANS NZOIA WEST
- 16. TRANSMARA
- 17. KAKAMEGA NORTH
- 18. MUMIAS

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# Teacher. ac

#### L.C.M



- 1. A piece of land is to be divided into 20 acres or 24 acres or 28 acres for farming and leave 7 acres for grazing. Determine the smallest size of such land.
- 2. When a certain number x is divided by 30, 45 or 54, there is always a remainder of 21. Find the least value of the number x
- 3. A number **m** is such that when it is divided by 30, 36, and 45, the remainder is always 7. Find the smallest possible value of **m**.
- 4. Find the L.C.M of  $x^2 + x$ ,  $x^2 1$  and  $x^2 x$

#### 1. Integers

- 1. 3x 1 > -4 $2x + 1 \le 7$
- 2. Find the value of x $2^{(x-3)} \times 8^{(x+2)} = 128$

#### 2. Decimals

1. Without using mathematical tables or calculators, evaluate: (3 mks)

$$\frac{0.0168 \times 2.46 \times 7}{5.74 \times 0.112}$$

- 2. A two-digit number is such that the sum of the ones digit and the tens digit is 10. If the digits are reversed, the number formed exceeds the original number by 54. Find the number (3 mks)
- 1. Use a calculator to find;
  - (a) 8754.3 x 53.84
  - (b) 0.8341 + 8.72

Hence find; 
$$3 \overline{\smash{)}\phantom{0}} 8754.3 \times 53.84 \over 0.8341 + 8.72$$

- 2. Express the recurring decimal below to a fraction 5.72 and leaving your answer in the form a/b where **a** and **b** are whole numbers
- 3. Evaluate:  $0.38 \times 0.23 \times 2.7$  without using tables or a calculator
- 4. Without using mathematical tables or calculator, evaluate:

Leaving the answer as a fraction in its simplest form.

5. Find without using a calculator, the value of :

$$\frac{12\sqrt{0.0625} - 12.4 \div 0.4 \times 3}{^{1}/_{8} \text{ of } 2.56 + 8.68}$$

# 3. Squares and square roots

- 1. Use tables to find;
  - a) i) 4.978<sup>2</sup>
    - ii) The reciprocal of 31.65

b) Hence evaluate to 4.S.F the value of  $4.978^2 - \frac{1}{31.65}$ 



2. Use tables of squares, square roots and reciprocals to evaluate correct to 4 s.f

$$\frac{3}{0.0136} - \frac{2}{(3.72)2}$$

3. Without using mathematical tables or calculator, evaluate:  $\sqrt{\frac{153 \times 1.8}{0.68 \times 0.32}}$  giving your answer in standard form

# 4. Algebraic expressions

- 1. Five year ago, a mother's age was four times that of her daughter. In four years to come, she will be  $2\frac{1}{2}$  times the age of her daughter. Calculate the sum of their present ages
- 2. Mutua bought 160 trays of 8 eggs each at shs.150 per tray. On transportation 12 eggs broke. He later discovered that 20 eggs were rotten. If he sold the rest at shs.180 per tray, how much profit did he make?
- 3. Simplify;

(a) 
$$6a - 2b + 7a - 4b + 2$$

(b) 
$$\frac{2x-2}{2x}$$
 -  $\frac{3x+2}{4x}$ 

4. Simplify 
$$\frac{6x^2y^2 + 13xy - 5}{3x^2y^2 - 13xy + 4}$$

5. Given that x + y = 8 and  $x^2 + y^2 = 24$ 

Find;

- (a) the value of  $x^2 + 2xy + y^2$
- (b) Find the value of; 2xy

(c) 
$$x^2 - 2xy + y^2$$

- (d) x y
- (e) Value of x and y
- 6. Simplify the expression.

$$\frac{6x^2 + 35x - 6}{2x^2 - 72}$$

7. Simplify the expression

$$^{2}/_{3}(3x-2) - \frac{3}{4}(2x-2)$$

8. Simplify by factorizing completely:

$$\frac{4y^2 - x^2}{2x^2 - yx - 6y^2}$$

9. Simplify as far as possible.

$$\frac{3}{x-y}$$
 -  $\frac{1}{x+y}$ 

- 10. By calculation, find the coordinates of the intersection of the graphs  $y = x^2 + 2x 5$  and y = 3x + 1
- 11. Simplify:

(a) 
$$\frac{y^2 + 2y}{y^3 - y^2 - 6y} = \frac{1}{4}$$

(b) hence solve:- 
$$y_2 + 2y = \frac{1}{4}$$
  
 $y^3 - y^2 - 6y$ 



- 12. A rectangular field measures 63.9m by 104.6metres find the minimum number of poles to be erected for fencing if they are to be at most 2.4meters apart.
- 13. Factorize completely the expression  $75x^2 27y^2$
- 14. Every time an insect jumps forward the distance covered is half of the previous jump. If the insect initially jumped 8.4cm, calculate
  - (i) To the nearest two decimal places distance of the sixth jump
  - (ii) The total distance covered after the sixth jump
- 15. Simplify  $P^3 Pq^2 + P^2q q^3$  $P^2 + 2pq + q^2$
- 16. Simplify the expression:  $\frac{9x^2 4y^2}{12x^2 + yx 6y^2}$
- 17. Given that  $(x-3)(Ax^2+bx+c) = x^3-7x-6$ , find the value of A, B and C
- 18. a) solve for **y** in  $8x(2^2)^y = 6x2^y 1$ 
  - b) Simplify completely  $\underline{2x^2-98}$   $\div$   $\underline{x+7}$   $3x^2-16x-35$  3x+5
- 19. Simplify the expression.:

$$\frac{4x^2 - y^2}{2x^2 - 7xy + 3y^2}$$

- 20. Simplify  $\frac{P^2 2Pq + q^2}{P^3 Pq^2 + P^2q q^3}$
- 21. The sum of two numbers is 15. The difference between five times the first number and three times the second number is 19. Find the two numbers
- 22. Simplify the following expressions by reducing it to a single fraction  $\frac{2x-5}{4} \frac{1-x}{3} \frac{x-4}{2}$
- 23. Simplify the expression:  $3a^2 + 4ab + b^2$  $4a^2 + 3ab - b^2$

# 5. Rates, Ratio and percentages

- 1. If 5 men can erect 2 cottages in 21days, how many more men, working at the same rate will be needed to erect 2 cottages in the same period?
- 2. The length and width of a rectangular paper were measured to the nearest centimeter and found to be 18cm and 12cm respectively. Find the percentage error in its perimeter in 6 hrs.
- 3. a) Two pipes **A** and **B** can fill a tank in 3hrs and 4 hrs respectively. Pipe **C** can empty the full tank

- i) How long would it take pipes **A** and **B** to fill the tank if pipe **C** is closed?
- ii) Starting with an empty tank, how long would it take to fill the tank with all pipes running eacher
- b) The high quality Kencoffee is a mixture of pure Arabica coffee and pure Robusta coffee in the ratio 1:3 by mass. Pure Arabica coffee costs shs. 180 per kg and pure Robusta coffee costs sh 120 per kg. Calculate the percentage profit when the coffee is sold at sh 162 per kg.
- 4. A number of nurses working at Sotik Health Centre decided to raise shs.144,000 to buy a plot of land. Each person was to contribute the same amount. Before the contributions were collected five of the nurses retired. This meant that the remaining contributors had to pay more to meet the target.
  - (a) If there were **n** nurses originally, find the expression of the increase in contribution per person
  - (b) If the increase in the contribution per person was shs.2,400, find the number of nurses originally at the health centre
  - (c) How much would each person have contributed to nearest shilling if the 5 people had not retired
  - (d) Calculate the percentage increase in the contribution per person because of the retirement
- 5. 3 taps **X,Y** and **Z** can fill a tank in 40 hours, 15 hours and 20 hours respectively. The three taps are turned on at 8.00a.m when the tank is empty for five hours then **Z** is turned off. After two hours tap **Y** is turned off. Work out ;-
  - (a) The proportion of water in the tank after seven hours
  - (b) The proportion of water in the tank after seven hours
  - (c) The time the tank will be completely full
- 6. Jane and Philip working together can do a piece of work in 6 days. Jane working alone takes 5 days longer than Philip. How many days does it take Philip to do the work alone?
- 7. Sixteen men working 9 hours a day can complete a piece of work in 14 days. How many more men working 7 hours a day would complete the same job in 12 days?
- 8. A group of people planned to contribute equally towards buying land at a price of shs.180000. However 3 members of the group withdrew from the project. As a result, each of the remaining members were to contribute kshs.3000 more.
  - (a) find the original number of members in the group
  - (b) How much would each person have contributed if the 3 people had not withdrew
  - (c) Calculate the percentage increase in the contribution per person caused by the withdrawal
- 9. Kori and Mue decided to start a business. Korir contributed shs.40,000 and Mue shs.64000. The two men agreed that in any year, 15% of the profit shall be divided equally between them and 20% of the profit will be used to meet the cost of running the business the following year. They also agreed to share the rest of the profit in the ratio of their contributions. The profit made after the first year was shs.43200.
  - a) How much did they set aside towards the cost of running the business for the second year?\*
  - b) How much did Mue receive at the end of the first year?
  - (c) Korir bought cows with his share of the profit. If each cow cost shs.1800, how many cows did he buy?
- 10. Given the ratio x : y = 2:3, find the ratio (7x 3y) : (2x + 3y)
- 11. Abdul bought five bulls and thirty goats at an auction spending a total of Kshs.117000. His friend Ali bought four bulls and twenty five goats at the same auction and spent Kshs.22,250 less.
  - (a) Find the cost of each animal at the auction
  - (b) Abdul later sold all his animals at a profit of 40% per bull and 30% per goat. Ali sold

all his animals at a profit of 50% per bull and 40% per goat. Determine who made more profit and by how much?



- 12. The cost of providing a commodity consists of transport, labour and raw material in the ratio 8:4:12 respectively. If the transport cost increases by 12% labour cost 18% and raw materials by 40%, find the percentage increase of producing the new commodity
- 13. A mother is now 2½ times as old as her daughter Mary; four years ago the ratio of their ages was 3:1. Find the present age of the mother
- 14. Sixteen men working at the rate of 9hrs a day can complete a piece of work in 14 days. How many more men working at the rate of 7 hours a day would complete the same job in 12 days
- 15. Two business partners, Kago and Beatrice contributed 90, 000/= and 120,000/= in order to start a business. They agreed that 25% of the profit made after end of the year will be put back into the business. They also estimated that 40% of the profit will cover salaries and other expenses for the year. The remainder would be shared between the partners in the ratio of their contributions. At the end of the first year the business realized a gross profit of shs.181,300.
  - a) Calculate how much each received after end of the year.
  - b) At the end of 2<sup>nd</sup> year the business realized the same gross profit as the previous year and the partners decided to dissolve the business and share everything. Determine how much money each received.
- 16. A number is such that the product of its digits is 24. When the digits are reversed, the number so formed exceeds the original number by 27. Find the number
- 17. The radius of a cylinder is increased by 30% while its height is decreased by 20%. Find the percentage change in the volume of the cylinder
- 18. Tap **A** fills a tank in 6 hours, tap **B** fills it in 8 hours and tap **C** empties it in 10 hours. Starting with an empty tank and all the three taps are opened at the same time, how long will it take to fill the tank?
- 19. Sixteen men working 9 hours a day can complete a piece of work in 14 days. How many more men working 7 hours a day would complete the same job in 12 days?
- 20. Three businessmen Langat, Korir and Koech contributed shs.160,000, Shs.200,000 and shs.240,000 respectively and started a business. They agreed that 30% of the profit each year will go to expenses, 15% of the reminder would go back to the business. The rest of the profit would be shared in the ratio of their contribution. At the end of the first year, the business realized a profit of kshs.60,000.
  - Calculate how much;
  - (a) (i) Langat received
    - (ii) Korir received
    - (iii) Koech received
  - (b) Express what Korir received as a percentage of the total profit
- 21. The price of a book is increased by 25%.
  - (a) In what ratio has the price increased?
  - (b) What is the new price if the book was shs.400 before the change?

 $\mathbf{X}$ 

(a) A chemist added 120 liters of a solution A containing 25% alcohol to 180 liters of solution 22. **B** containing 20% alcohol. What percentage of the resulting solution in alcohol?



- (b) He removed X liters of resulting mixture and added an equal amount of pure alcohol to the resulting mixture. If the new mixture contains 22% of the alcohol, find the value of X
- 23. The length and width of a rectangular paper were measured to the nearest centimeter and found to be 18cm and 12cm respectively. Find the percentage error in its perimeter
- 24. Given that a:b = 1: 2 and b:c = 3:4. Find a:b:c

# 6. length

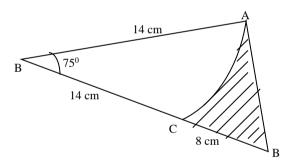
1 Simplify; by factorization:

$$\frac{15x^2 + xy - 6y^2}{5x^2 - 8xy + 3y^2}$$

Given the matrices  $M = \begin{pmatrix} 3 & 0 \\ -1 & 4 \end{pmatrix} R = \begin{pmatrix} -1 & 2 \\ 0 & 0 \end{pmatrix}$  and  $N = \begin{pmatrix} 2/3 & 1 \\ 2 & 4 \end{pmatrix}$ . Find the value of value of 3n +  $\frac{1}{2}$  (R-M) 2.

#### 7. Area

Calculate the area of the shaded region below, given that AC is an arc of a circle centre B. 1. AB=BC=14cm CD=8cm and angle  $ABD=75^{\circ}$ (4 mks)

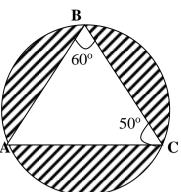


1. A student took the measurements of his classroom and gave the width as 7m and the length as 9m. If there is an error of 2% in each measurement, determine the greatest value of  $\mathbf{x} + \mathbf{y}$ 

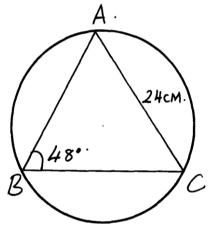
if x and v are the width and length of the classroom respectively. Give your answer to 4 decimal places.

- 2. The floor of a room is in the shape of a rectangle 10.5 m long by 6 m wide. Square tiles of length 30 cm are to be fitted onto the floor.
  - (a) Calculate the number of tiles needed for the floor.
  - (b) A dealer wishes to buy enough tiles for fifteen such rooms. The tiles are packed in cartons each containing 20 tiles. The cost of each carton is Kshs. 800. Calculate
    - (i) the total cost of the tiles.
    - (ii) If in addition, the dealer spends Kshs. 2,000 and Kshs. 600 on transport and subsistence respectively, at what price should he sell each carton in order to make a profit of 12.5% (Give your answer to the nearest Kshs.)

The figure below is a circle of radius 5cm. Points **A**, **B** and **C** are the vertices of the triangle ABC in which  $\angle ABC = 60^{\circ}$  and  $\angle ACB = 50^{\circ}$  which is in the circle. Calculate the area of  $\triangle ABC$ 



- 4. Mr.Wanyama has a plot that is in a triangular form. The plot measures 170m, 190m and 210m, but the altitudes of the plot as well as the angles are not known. Find the area of the plot in hectares
- 5. Three sirens wail at intervals of thirty minutes, fifty minutes and thirty five minutes. If they wail together at 7.18a.m on Monday, what time and day will they next wail together?
- 6. A farmer decides to put two-thirds of his farm under crops. Of this, he put a quarter under maize and four-fifths of the remainder under beans. The rest is planted with carrots. If 0.9acres are under carrots, find the total area of the farm
- 7 Find the area of the circle sector.

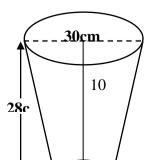


# 8. Volume and capacity

1. A village water tank is in the form of a frustrum of a cone of height 3.2m.

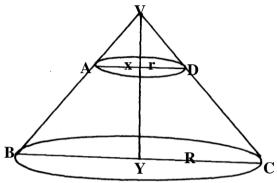
The top and bottom radii are 18m and 24m respectively

- (a) Calculate:
  - (i) The surface area of the tank excluding the bottom
  - (ii) The capacity of the water tank
  - (b) 15 families each having 15 members use the water tank and each person uses 65 litres of water daily. How long will it take for the full tank to be emptied
- 2. The diagram below shows a bucket with a top diameter 30cm and bottom diameter 20cm. The height of the bucket is 28cm
  - (a) Calculate the capacity of the bucket in litres





- (b) Find the area of the metal sheet required to make 100 such buckets taking 10% extra for overlapping and wastage
- 3. A rectangular water tank measures 2.6m by 4.8m at the base and has water to a height of 3.2m. Find the volume of water in litres that is in the tank
- 4. The figure alongside shows a cone from which a frustum is made. A plane parallel to the base cuts the cone two thirds way up the vertical height of the cone to form frustum **ABCD**. The top surface radius of the frustum is labeled **r** and the bottom radius is **R**



- a) Find the ratio r:R
- b) Given that r = 7cm, find R
- c) If the height VY of the original cone is 45cm, calculate to the nearest whole number the volume of the frustum
- d) The frustum represents a bucket which is used to fill a rectangular tank measuring 1.5m long, 1.2m wide and 80cm high with water. How many full buckets of water are required to fill the tank
- 5. Three litres of water (density1g/cm³) is added to twelve litres of alcohol (density 0.8g/cm³. What is the density of the mixture?
- 6. A rectangular tank whose internal dimensions are 2.2m by 1.4m by 1.7m is three fifth full of milk.
  - (a) Calculate the volume of milk in litres
  - (b) The milk is packed in small packets in the shape of a right pyramid with an equilateral base triangle of sides 10cm. The vertical height of each packet is 13.6cm. Full packets obtained are sold at shs.30 per packet. Calculate:
    - (i) The volume in cm<sup>3</sup> of each packet to the nearest whole number
    - (ii) The number of full packets of milk
    - (iii) The amount of money realized from the sale of milk
- 7. An 890kg culvert is made of a hollow cylindrical material with outer radius of 76cm and an inner radius of 64cm. It crosses a road of width 3m, determine the density of the material used in its construction in Kg/m<sup>3</sup> correct to 1 decimal place.

2.

# 9. Mass, weight and density



- A piece of metal has a volume of 20 cm<sup>3</sup> and a mass of 300g. Calculate the density of the meta in  $kg/m^3$ .
- 2.5 litres of water density 1g/cm<sup>3</sup> is added to 8 litres of alcohol density 0.8g/cm<sup>3</sup>. Calculate the density of the mixture

#### **10.** Time

- 1. A van travelled from Kitale to Kisumu a distance of 160km. The average speed of the van for the first 100km was 40km/h and the remaining part of the journey its average speed was 30km/h. Calculate the average speed for the whole journey. (3 mks)
- 1. A watch which looses a half-minute every hour was set to read the correct time at 0545h on Monday. Determine the time, in the 12 hour system, the watch will show on the following Friday at 1945h.
- 2. A watch which loses a half-minute every hour was set to read the correct time at 0445h on Monday. Determine the time in 12-hour system, the watch will show on the following Friday at 1845h
- The timetable below shows the departure and arrival time for a bus plying between two 3. towns M and R, 300km apart

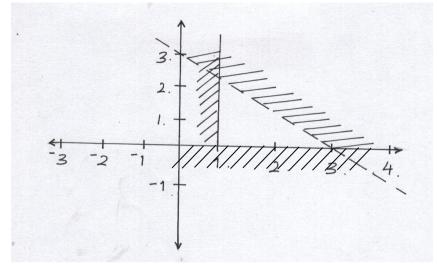
Town	Arrival	Departure
M		0830h
N	1000h	1020h
P	1310h	1340h
Q	1510h	1520h
R	1600h	

- (a) How long does the bus take to travel from town **M** to **R**?
- (b) What is the average speed for the whole journey?

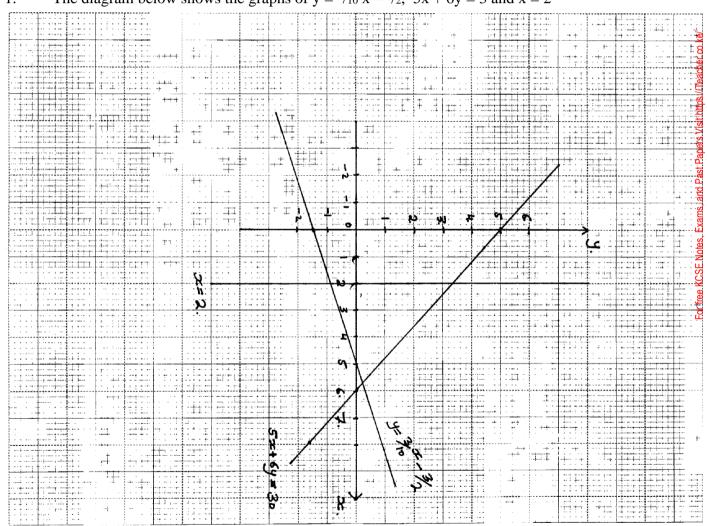
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1. Determine the inequalities that represent and satisfies the unshaded region

(3 mks)



1. The diagram below shows the graphs of  $y = \frac{3}{10} x - \frac{3}{2}$ , 5x + 6y = 3 and x = 2



By shading the unwanted region, determine and label the region **R** that satisfies the three inequalities;  $y \ge \frac{3}{10} x - \frac{3}{2}$ ,

$$5x + 6y \ge 30$$
 and  $x \ge 2$ 

2. The cost of 7 shirts and 3 pairs of trousers is shs. 2950 while that of 5 pairs of trousers and 3 shirts



- 3. Mr. Wafula went to the supermarket and bought two biros and five pencils at sh.120. Whereas three biros and two pencils cost him sh.114. Find the cost of each biros and pencils
- 4. A father is twice as old as his son now. Ten years ago, the ratio of their ages was 5:2. Find their present ages
- 5. List the integral values of **x** which satisfy the inequalities below:  $2x + 21 > 15 2x \ge x + 6$
- 6. Find the equation of a line which passes through (-1, -4) and is perpendicular to the line:- y + 2x 4 = 0
- 7. John bought two shirts and three pairs of trousers at Kshs. 1750. If he had bought three shirts and two pairs of trousers, he would have saved Kshs. 250. Find the cost of a shirt and a trouser.
- 8. Express the recurring decimal 3.81 as an improper fraction and hence as a mixed number
- 9. Karani bought 4 pencils and 6 biro pens for shs.66 and Mary bought 2 pencils and 5 biro pens for shs.51
  - (a) Find the price of each item
  - (b) Ondieki spent shs.228 to buy the same type of pencils and biro pens. If the number of biro pens he bought were 4 more than the number of pencils, find the number of pencils he bought
- 10. Two consecutive odd numbers are such that the difference of twice the larger number and twice the smaller number is 21. Find the product of the numbers
- 11. The size of an interior angle of a regular polygon is  $3x^0$  while its exterior angle is  $(x-20)^0$ . Find the number of sides of the polygon
- 12. Five shirts and four pairs of trousers cost a total of shs.6160. Three similar shirts and a pair of trouser cost shs.2800. Find the cost of four shirts and two pairs of trousers
- 13. Two pairs of trousers and three shirts costs a total of Shs.390. Five such pairs of trousers and two shirts cost a total of Shs.810. Find the price of a pair of trouser and a shirt

# 12. Equations

leacher.a

1. Solve the simultaneous equation

$$2x - y = 3$$
$$x^2 - xy = -4$$

- 1. A Kenyan businessman US\$100 to a company in the United States of America. The Kenyan can either pay through his account in Kenya or through his account in the United Kingdom. Which method is cheaper and by how much? Give your answer in Kenya shillings given that; 1 US dollar = 76.84 Kenya shillings
  - 1 Sterling Pound = 1.53 US dollars
  - 1 Sterling pound = 115.70 Kenya shillings
- 2. Foreign exchange on 27/5/2010 was given as follows:.

Currency	<b>Buying</b> (Kshs)	Selling (Kshs)
1 Euro	84.15	84.26
1 Sterling pound	118.35	121.47



A tourist came to Kenya from London with 6000 Euros which he converted to Kenya shillings at a bank. While in Kenya he spent a total of Kshs.300,000 then converted the balance into sterling pounds at the Same bank. Calculate the amount in sterling pounds he received.

3. A Kenyan football fan visited South Africa from Kenya. He changed his currency from Kenya shillings to South African rand. The exchange rates in Kenya were as per the table below:-

Buying	Selling
9.9399	10.0166

He has a total of shs.2, 8000,265 and must spend 13 days. During his stay, he spent 8900 Rands on food and accommodation, 97,000 Rands on a return air ticket and 53689 Rands on entertainment. On his return, he converted the remaining amount into Kshs. How much did he receive to the nearest cents?

- 4. A French tourist changes 3000 Francs into Kenyan shillings at 1 Franc = Kshs.1.89. He spends shs.4695, then exchanges the remaining shillings back into Francs at 1 Franc =1.95. How many Francs does he receive?
- 5. Hamisi arrived in Nairobi from USA with 40 travelers cheques each with 75 US dollars. How much does she receive in Kshs from the bank on a day when 1 US dollar was equivalent to Kshs 81.40 and the bank charges commission at the rate of Kshs.100 per travelers cheque
- 6. A Kenya bank buys and sells foreign currencies as shown below

	Buying in Kshs.	Selling in Kshs.
1 Hong Kong dollar	9.74	9.77
1 South African rand	12.03	12.11

A tourist arrived in Kenya with 105,000 Hong Kong dollars and changed the amount to Kenya shillings. While in Kenya, she spent Shs.403,879 and changed the balance to South African rand before leaving for South Africa. Calculate the amount, in South African rand that she received

7. A Japanese tourist entered Kenya with Kshs.500,000 Japanese Yen which he converted to Kenya currency. While in Kenya, he spend Kshs.16200 in all. He then converted all the remaining money into Euros before leaving for Italy. If he carried out all his transactions at the Stanbic bank using rates shown below, calculate to the nearest Euro, how much money he left Kenya with. (*Do not use mathematical tables for this question*)

	Selling (Kshs	<b>Buying Kshs</b>
100 Japanese Yen	66.35	66.05
1 Euro	78.15	77.85

8. Do not use mathematical tables in this question. Equity bank buys and sells foreign currencies as shown:-

	<b>Buying (Kshs.)</b>	Selling Kshs.
1 US dollar	77.43	78.10
I South African Rand	9.03	9.51

A tourist arrived in Kenya with 5,600 US dollars and changed the whole amount to Kenya shillings while in Kenya he spend shs.201,367 and changed the balance to South African rand



A tourist arriving from Britain had UK £ 9000. He converted the pounds to Kenyan shillings at a commission of 5%. While in Kenya he spent ¾ of his money. He exchanged the remaining to US dollars with no commission. Calculate to the nearest US dollars the amount using the exchange rate below.

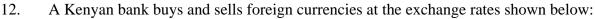
Currency	Buying Kshs.	Selling Kshs.
1 US Dollar	63.00	63.20
1 UK Dollar	125.30	125.95

- 10. A company was to import goods worth Kshs.100,000 from U.K and changed the money to Sterling pounds. The company later realized that it was cheaper to import the same goods from U.S.A and changed the sterling pounds to dollar. Unfortunately the transaction failed and the money was converted to Kenya shillings. How much money did the company end-up with, given that;
  - 1 US dollar = Kshs.78

Teacher. a

- 1 Sterling pound = Kshs.120
- 1 Sterling pound = 1.79 U.S dollar
- 11. A tourist arrives in Kenya from England with S.£ 50,000 and uses the money to buy Kenya shillings. He quickly changes his mind and sells the Kenya shillings to get back his s£. How much money in S.£ did he get? Use the table below

	buying	selling
1 Sterling pound	120.7131	120.9294



	Buying	Selling
	(Kshs.)	(Kshs.)
1 Euro	147.86	148.00
1 US Dollar	74.22	74.50



An American arrived in Kenya with 20000 Euros. He converted all the Euros to Kenya shillings at the bank. He spent Kshs.25100 200 while in Kenya and converted the remaining Kenya shillings into US Dollars at the bank. Find the amount in dollars that he received

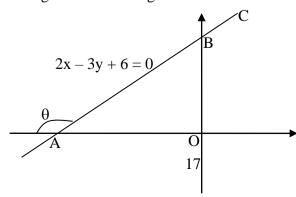
13. Simplify;

(a) 
$$6a - 2b + 7a - 4b + 2$$

(b) 
$$\frac{2x-2}{2x}$$
 -  $\frac{3x+2}{4x}$ 

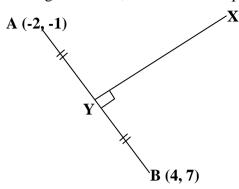
#### 13. Commercial arithmetic

- 1. Jane is a sales executive earning a salary of Ksh. 20,000 and a commission of 8% for the sales in excess of Ksh 100,000. If in January 2010 she earned a total of Ksh.48, 000 in salaries and commissions.
  - a) Determine the amount of sales she made in that month (4 mks)
  - b) If the total sales in the month of February and March increased by 18% and then dropped by 25% respectively. Calculate
    - (i) Jane's commission in the month of February (3 mks)
    - (ii) Her total earning in the month of March (3 mks)
- 2. Wekhomba bought a laptop in Uganda for Ush.1, 050,000. He then paid 60 US dollars as transportation charges to Kenya. On arrival in Kenya he paid duty and sales tax amounting to 55% of the cost in Uganda. He then gave it to a friend in Tanzania tax free. If the exchange rates were I US dollar = Ush 1016, 1Ksh = Ush 24.83 and Tsh 1 = Ksh 0.0714
  - (a) Calculate the total expenses in Kenya shillings incurred by Wekhomba (3 mks)
  - (b) Find the expenditure on transportation and taxes as a percentage of the total expenditure (2 mks)
  - (c) What is the total value of the laptop in Tanzanian shillings (2 mks)
  - (d) Find the overall increase in value of the laptop as percentage of the buying price (3 mks)
- 1. Find the angle  $\theta$  in degrees from the figure below





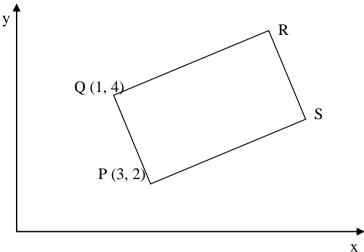
2. In the diagram below, determine the equation of the line **XY** in the form y = mx + c



- 3. Find the equation of a line which passes through the point (2, 3) and is perpendicular to y 3x + 1 = 0, giving your answer in the form y = mx + c
- 4. **T** is the mid-point of line **XY** where **X** is point (1,4) and **Y** is the point (-5, 10). Find the equation of a line,  $L_2$  which is perpendicular to line **XY** and goes through point **T**
- 5. (a) On the grid provided below, plot points A(2,1) B(-4,3) and C(2,5)
  - b) Given that the gradient of CD = -1 and CD = AD locate D and complete the quadrilateral ABCD
  - (c) What name is given to quadrilateral ABCD?

6. In the figure below (not drawn to scale), **PQRS** is a rectangle and **P** and **Q** are the points (3, 2) and (1,4) respectively





Given that the equation of the line PQ is y = 3x - 7, find:

- (a) The equation of line QR
- (b) The coordinates of point **R**
- (c) The coordinates of point S
- 7. OABC is a trapezium such that the coordinates of O, A, B and C are (0, 0), (2, -1), (4, 3) and (0, y)
  - (a) Find the value of y
  - (b) M is the mid-point of AB and N is the mid-point of OM. Find in column form
    - (i) the vector AN
    - (ii) the vector **NC**
    - (iii) Vector AC
  - (c) Hence show that A, N and C are collinear
- 8. Use ruler and a pair of compasses only in this question.
  - (a) Construct triangle ABC in which AB = 7 cm, BC = 8 cm and  $\angle$ ABC =  $60^{\circ}$ .
  - (b) Measure (i) side AC (ii) ∠ ACB
  - (c) Construct a circle passing through the three points A, B and C. Measure the radius of the circle.
  - (d) Construct  $\triangle$  PBC such that P is on the same side of BC as point A and  $\angle$  PCB =  $\frac{1}{2}$   $\angle$  ACB,  $\angle$  BPC =  $\angle$  BAC measure  $\angle$  PBC.
- 9. ABCD is a parallelogram with vertices A (1,1) and C(8,10). AB has the equation 4x 5y = -1 and BC has the equation 5x 2y = 20. Determine by calculation;
  - (a) the co-ordinates of the point M where the diagonals meet
  - (b) The co-ordinates of the vertices B and D
  - (c) the length of AB correct to 4 significant figures
- 10. The table shows corresponding values of x and y for a certain curve;

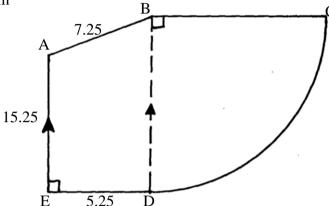
х	1.0	1.2	1.4	1.6	1.8	2.0	2.3
V	6.5	6.2	5.2	4.3	4.0	2.6	2.4

Using 3 strips and mid-ordinate rule estimate the area between the curve, x-axis, the lines x = 1 and x = 2.2



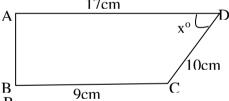
### 14. Coordinates and Graphics

- 1. The size of an interior angle of a rectangular polygon is 6 ½ times that of its exterior angle. Determine the number of sides of the polygon.
- 2. The sum of interior angles of two regular polygons of sides n and n + 2 are in the ratio 3:4. Calculate the sum of the interior angles of the polygons with n sides
- 3. The area of a rhombus is  $60 \text{cm}^2$ . Given that one of its diagonals is 15cm long. Calculate the perimeter of the rhombus.
- 4. In the figure below AE is parallel to BD. BC = BD, AB = 7.25cm, AE = 15.25cm and ED = 5.25 cm



Find the perimeter of the figure.

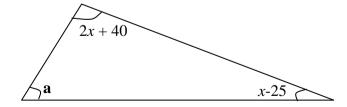
5. The figure below shows a trapezium ABCD in which side AB is perpendicular to both AD and BC. Side AD=17cm, DC=10cm



(i) What is the length of side AB

7.

- (ii) Find the value of  $\cos(90^{\circ} x^{\circ})$  in the form  $\underline{\mathbf{a}}$  where  $\mathbf{a}$  and  $\mathbf{b}$  are integers
- 6. The size of an interior angle of a regular polygon is  $3x^{o}$  while its exterior angle is  $(x-20)^{o}$ . Find the number of sides of the polygon



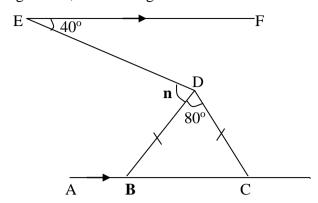
In the figure above, angle **a** is half the sum of the other angles. Evaluate the triangle

8. The sum of the interior angles of an **n**-sided polygon is 1260°. Find the value of **n** and hence deduce the polygon

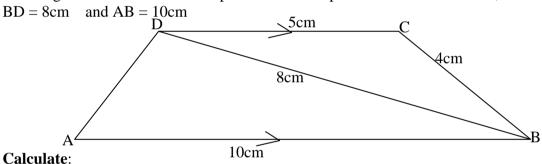
9.



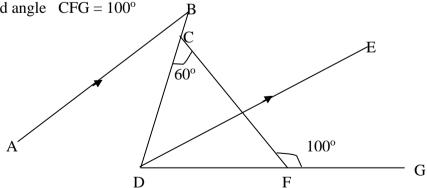
Giving reason, find the angle marked **n** 



- 10. Solve for **y** in the equation  $125^{y+1} + 5^{3y} = 630$
- 11. The interior angle of a regular polygon is 108° larger than the exterior angle. How many sides has the polygon?
- 12. The interior angle of a regular polygon is 4 times the exterior angle. How many sides has the polygon
- 13. In the figure below ABCD is a trapezium with DC parallel to AB. DC = 5cm, CB = 4cm,



- (a) the size of angle BDC
- (b) the area of triangle ABD
- In the figure below, DE bisects angle BDG and AB is parallel to DE. Angle DCF =  $60^{\circ}$  and angle CFG =  $100^{\circ}$  B

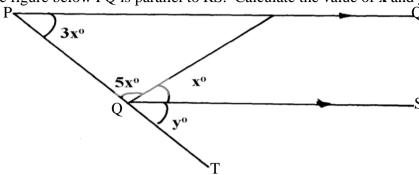


Find the value of angle:-

- (a) CDF
- (b) ABD
- 15. The size of an interior angle of a regular polygon is  $4x^{\circ}$ , while its exterior angle is  $(x 30)^{\circ}$ . Find the number of sides of the polygon



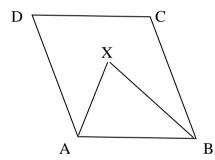
- 16. The sum of interior angles of a polygon is 1440°. Find the number of sides of the polygon hence name the polygon
- 17. In the figure below PQ is parallel to RS. Calculate the value of  $\mathbf{x}$  and  $\mathbf{y}$



18. The interior angle of a n-sided regular polygon exceeds its exterior angle by 132°. Find the value of n

# 15. Angles and Plane Figures

- 1. The sum of angles of a triangle is given by the expression  $(2a+b)^0$  while that of a quadrilateral is given by  $(13a-b)^0$ . Calculate the values of a and b (4 mks)
- 2. The figure below represents a quadrilateral ABCD. Triangle ABX is an equilateral triangle. If  $\angle ADX = 50^{\circ}$ , find  $\angle AXD$  with  $\angle BAD = 90^{\circ}$  (2 mks)



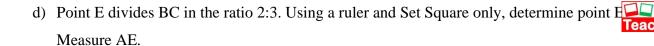
- 3. Wanjiku is standing at a point P, 160m south of a hill H on a level ground. From point P she observes the angle of elevation of the top of the hill to be 67<sup>0</sup>
  - (a) Calculate the height of the hill

(3 mks)

- (b) After walking 420m due east to the point Q, Wanjiku proceeds to point R due east of Q, where the angle of elevation of the top of the hill is 35°. Calculate the angle of elevation of the top of the hill from Q (3 mks)
- (c) Calculate the distance from P to R (4 mks)

#### 16. Geometrical Constructions

- 1. Using a ruler and a pair of compasses only,
  - a) Construct a triangle ABC in which AB = 9cm, AC = 6cm and angle BAC =  $37\frac{1}{2}^{0}$
  - c) Drop a perpendicular from C to meet AB at D. Measure CD and hence find the area of the triangle ABC



- 1. Chebochok deposited shs.120,000 in a financial institution which offered a compound interest at 8% p.a, compounded quarterly for 9 months. Find the accumulated amount by the end of the period
- Using a ruler and a pair of compasses only, draw a parallelogram ABCD in which AB = 6cm, BC = 4cm and angle  $BAD = 60^{\circ}$ . By construction, determine the perpendicular distance between the lines AB and CD
- 3. Without using a protractor, draw a triangle ABC where  $\angle CAB = 30^{\circ}$ , AC = 3.5cm and AB = 6cm. measure BC
- 4. (a) Using a ruler and a pair of compass only, construct a triangle ABC in which angle ABC =37.5°, BC =7cm and BA = 14cm
  - (b) Drop a perpendicular from A to BC produced and measure its height
  - (c) Use your height in (b) to find the area of the triangle ABC
  - (d) Use construction to find the radius of an inscribed circle of triangle ABC
- 5. In this question use a pair of compasses and a ruler only
  - a) Construct triangle PQR such that PQ = 6 cm, QR = 8 cm and  $< PQR = 135^{\circ}$
  - b) Construct the height of triangle PQR in (a) above, taking QR as the base
- 6. On the line AC shown below, point **B** lies above the line such that  $\angle BAC = 52.5^{\circ}$  and AB = 4.2cm. (*Use a ruler and a pair of compasses for this question*)



- (a) Construct ∠BAC and mark point **B**
- (b) Drop a perpendicular from **B** to meet the line **AC** at point **F**. Measure **BF**
- 7. Juma paid shs.450 for a trouser after getting a discount of 10%. The trader still made a profit of 25% on the sale. What profit would the trader have made if no discount was allowed?

# 17. Scale Drawing

- 1. Three mountains Mikai, Kembo and Chaka in a village are situated in such a way that Kembo is 900m on a bearing of 120<sup>0</sup> from Mikai. Mt. Chaka is 1200m on a bearing of 030<sup>0</sup> from Kembo.
  - (ii) Draw a sketch showing the position of the three mountains (1 mk)
  - (iii)Calculate the distance of Mt. Chaka from Mt. Mikai (2 mks)
- 1. Town **X** is 13.5km from town **Y** on a bearing of 028°. A matatu leaves **y** at 7:35a.m towards a bearing of 080°. The matatu is at point **Z** due south of **X** at 8:55a.m
  - (a) Calculate the average speed of the matatu from **Y** to **Z**
  - (b) If the matatu continues on the same bearing, calculate the distance it covers from  $\bf Z$  when it is East of  $\bf X$

2. Three towns X, Y and Z are such that Y is 500km on a bearing of 315° from X. Z is on a bearing of 230° from X. given that the distance between Y and Z is 800km.



- (a) using a scale of 1cm to represent 100km, draw a scale diagram to show the position of the Towns
- (b) Find the bearing of;
  - (i) X from Z
  - (ii) Z from Y
- (c) Use the scale drawing to find the distance from X to Z
- 3. Two aeroplanes **S** and **R** leave an airport at the same time. **S** flies on the bearing of 240° at 750Km/h while **R** flies due East at 600Km/hr..
  - (a) (i) Calculate the distance of each aeroplane after 30minutes
    - (ii) Using a scale of 1cm to represent 50km make an accurate scale drawing to show the positions of the aeroplanes after 30minutes
  - (b) (i) Use the scale drawing to find the distance between the two aeroplanes after 30minutes
    - (ii) If each aeroplane landed after 30minutes and **S** received a signal to join **R** in 45minutes. Find its speed
  - (c) Determine the bearing of:
    - (i) **S** from **R**
    - (ii) R from S
- 4. The table below gives a field book showing the results of a survey of a section of a piece of land between A and E. All measurements are in metres.

	E	
<b>D</b> 33	95	
	90	<b>F</b> 36
<b>C</b> 21	70	
<b>B</b> 42	30	<b>G</b> 25
	25	<b>H</b> 40
	A	

- (a) Draw a sketch of the land.
- (b) Calculate the area of this piece of land.
- 5. Three towns A B and C are situated such that town A is 40km from B on a bearing of 280°. C is 60km from B on a bearing of 130°. Another town D is only 10km from C on a bearing of 210°.
  - (a) Drawing accurately and using a scale of 1cm to 10km find the:-
  - (b) Distance from A to C and the bearing of A from C
  - (c) (i) Distance of B from D
    - (ii) Distance of A from D
    - (iii) Bearing of A from D
    - (iv) Bearing of C from D
- 6. A train left Naivasha for Nakuru at 1000hours. It traveled at an average speed of 45km/h and reached Gilgil after 40minutes. It then covered the remaining 50km in 1½ hours. A second train left Nakuru for Naivasha at 1015 hours and arrived at Gilgil at the same time as the first train arrived at Nakuru.
  - a) Using a scale of 1cm to represent 10minutes in the time axis and 1cm to represent 10km on the distance axis, draw on the same axes the graphs to show the movement of the two trains
  - b) use your graph to find;
    - i) the distance between Naivasha and Nakuru
    - ii) the time at which the train met
  - c) calculate the average speed, in km/h of the second train



- On a certain map, a road 20km long is represented by a line 4cm long. Calculate the area of a rectangular plot represented by dimensions 2.4cm by 1.5cm on this map leaving your answer in hectares
- A port **B** is on a bearings of 080° from a port **A** and at a distance of 95km. a submarine is stationed at a port **D**, which is on a bearing of 200° from **A**, and a distance of 124km from **B**. A ship leaves **B** and moves directly southwards to an island **P**, which is on a bearing of 140° from **A**. the submarine at **D** on realizing that the ship was heading for the island **P**, decides to head straight for the island to intercept the ship.
- (a) Using a scale of 1cm to represent 10km draw a diagram to show the positions of A,B,D, and P (b) Hence;

#### **Determine:**

- (i) the distance from **A** to **D**
- (ii) the bearing of the submarine from the ship when the ship was setting off from B
- (iii) the bearing of the island **P** from **D**
- (iv) the distance the submarine had to cover to reach the island P
- 9. Use a scale of 1cm represents 50km in these questions. Five towns **A**, **B**, **C**, **D** and **E** are situated such that **A** is 200 km from **B** on a bearing of 050° from **E**. **C** is 300 km from **B** on a bearing of 150° from **B**. **D** is 350km on a bearing of 240° from **C**. **E** is 200km from **D** and the bearing of **D** from **E** is 100°
  - a) Draw the diagram representing the positions of the towns
  - b) From the diagram, determine;
    - i) The distance in km of A from E
    - ii) The bearing of D from B
- 10. Four towns **P**, **Q**, **R** & **S** are such that **P** is 280 km North of **R**, **S** is 190 km from **R** on a bearing of 310° and **Q** is 240 km from **P** on a bearing of 105°.
  - a) Using scale of 1 cm rep. 50 km, locate the four towns.
  - b) Find; (i) distance **SQ**.
    - (ii) Bearing of **S** from **Q**.
    - (iii) The shortest distance between **P** and side **QR**.
- 11. Four ships are at sea such that a streamliner S is 150km on a bearing of 025° from a cargo ship C. A trawler T is 300km on a bearing of 145° from the cargo ship and a yacht Y is due West of C and on a bearing of 300° from T.
  - a) Using a scale of 1cm= 50km, draw on accurate scale drawing showing the positions of S, C, T and Y
  - b) By measurement from your scale drawing determine:
    - i) The distance and bearing of Y from S
    - ii) The distance ST
    - iii) The distance YT
- 12. A tea farm in Kakamega forest was surveyed and the results were recorded in the surveyors note book as shown below. The measurements are in meters

	250	Y
	240	D70
C80	170	
	70	B60
A60	50	
X	0	

Using a scale of 1: 25, draw the map of the plot and hence calculate the area of the plot in Hectares



13. The information below shows the entries in a surveyor's field book after a survey of a farm. XY = 280m is the baseline. All measurements are in metres

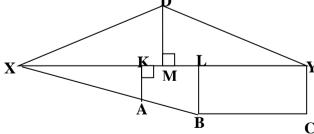
	280	Y	
B 105	230	110E	
	190		
	160	45E	
A 100	90		
	40	95G	
X	О		

- (a) Use a scale of 1cm represents 20m to draw the map of the farm
- (b) Estimate the area of the farm in hectares
- (c) If the point Y lies due north of X, find correct to 1 decimal place, the :
  - (i) Bearing of E from X
  - (ii) Distance of E from X
- 14. The measurements of a flower garden were recorded in a surveyor's field book as shown.

	250	Y
	240	D 70
C80	170	
	70	B 60
X	0	

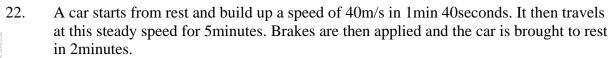
Draw a sketch of the field and find its area. (Measurements are in m)

- 15. A map has a scale 1:40,000:
  - (a) Calculate the distance between two points on the ground if the corresponding distance shown on the map is 3.25cm
  - (b) Calculate the area in the map of woodland which occupies 36ha on the ground
- 16. Three scouts John, Peter and Samwel stand on three adjacent peaks of equal altitude on mountain range. The distance between John and Peter is 800metres and the bearing of Peter from John is 020°. The distance between John and Samwel is 1500metres, and the bearing of Samwel from John is 320°.
  - (a) Calculate the bearing of John from Peter
  - (b) Calculate:- (i) the distance
    - (ii) the bearing of Samwel from Peter
- 17. The figure below represents a surveyor's sketch of a plot of land. Calculate the area of the plot in square metres given that XY = 50m, XK = 20m, XM = 25m, XL = 35m, KA = 40m, MD = 38m and LB = YC = 60m.



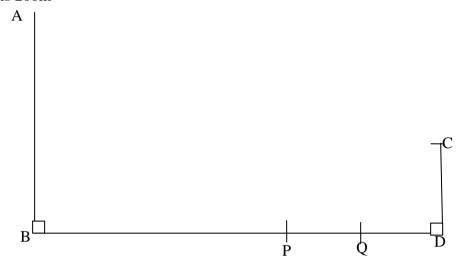
- 18. Two boats **P** and **Q** are located 30km apart; **P** being due North of **Q**. An observer at **P** spots a ship whose bearing he finds as S 56°E from **Q**, the bearing of the same ship is 038°. Calculate the distance of the ship from **Q** to 2 decimal places
- 19. A map is drawn to scale of 1:100,000. What area in km<sup>2</sup>, is represented by a rectangle measuring 4.5cm by 5.4 cm

Two places **A** and **B** are 900km apart on the earth's surface. If **A** is due North of **B** and given that the latitude of **A** is 5°N. Find the latitude of **B**. (Take radius of the earth to be 6370km)





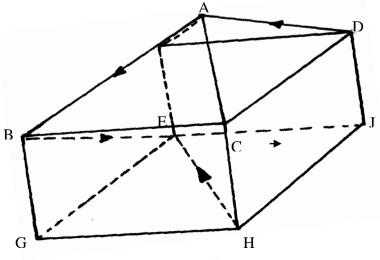
- (a) Draw a velocity-time graph to show the journey
- (b) Use your graph to find;
  - (i) the initial acceleration
  - (ii) the deceleration when the car is brought to rest
  - (iii) the distance traveled
- 23. The diagram below represents two vertical watch-towers AB and CD on a level ground. P and Q are two points on a straight road BD. The height of the tower AB is 20m and road BD is 200m



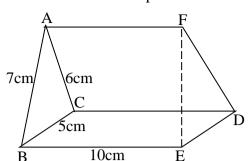
- (a) A car moves from B towards D. At point P, the angle of depression of the car from point A is 11.3°. Calculate the distance BP to 4 significant figures
- (b) If the car takes 5 seconds to move from P to Q at an average speed of 36km/.hr. Calculate the angle of depression of Q from A to 2 decimal places
- (c) Given that QC = 50.9m, calculate;
  - (i) the height of CD in metres to 2 decimal places
  - (ii) the angle of elevation of A from C to the nearest degree
- 24. Town B is 180 km on a bearing of 050<sup>0</sup> from town A. Another town C is on a bearing of 110<sup>0</sup> from town A and on a bearing of 150<sup>0</sup> from town B. A fourth town D is 240 km on a bearing of 320<sup>0</sup> from A. Without using a scale drawing, calculate to the nearest kilometer.
  - (a) The distance AC
  - (a) The distance CD

#### 18. Common solids

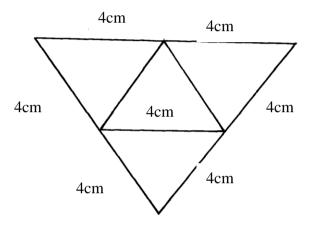
1. The figure below represents a square based solid with a path marked on it



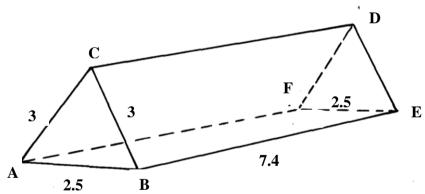
Sketch and label the net of the solid The below shows a solid prism:-



- (a) Sketch the net of the prism above
- (b) Use the net in (a) above to calculate the total surface area of the material used in making the solid
- 3. Draw the solid whose net is shown below.



4. Sketch the net of the solid shown in the figure below, measurements are in centimeters



# 19. Indices

- 1. Evaluate the value of x in  $8^{X+1} + 3^{4x} = 246$ .
- 2. Solve for **y** in the equation: $5^{(2y+1)} = 4(5)^{y+1} 15$
- 3. Without logarithm tables or calculators, evaluate:  $25^{34} \times 0.9^2 \times 2^2$  in the form A/B where A and B are integers  $5^{5}/_{2} \times 3^{3}$

Find the value of x given that: 4.

 $2^{x}=0.0625$  (x is an integer)

Find the value of x which satisfies the equation  $16^{x^2} = 8^{4x-3}$ 6.



- Solve the equation;  $9^{x+1} + 3^{2x+1} = 36$
- By letting  $P = 4^{-y}$  in the equation:

 $4^{-2y+1} - 3 \times 4^{-y} - 10 = 0$ 

- (a) Write the above equation in terms of **P**
- (b) Hence find the possible values of y
- 9. Solve for  $\mathbf{x}$  in the equation.
- In the expansion of  $\begin{bmatrix} \mathbf{a}\mathbf{x} \mathbf{\underline{2}} \\ \mathbf{x}^2 \end{bmatrix}$  the constant term is 4860. Find the value of  $\mathbf{a}$ . 10.

#### 20. Reciprocals

1. Use reciprocal, square and square root tables to evaluate, to 4 significant figures, the

expression. 
$$\sqrt{\frac{1}{24.56} + 4.346^2}$$
 (3 mks)

1. Use reciprocal table to evaluate giving your answer to three significant figures.

$$\frac{10}{0.834}$$
 -  $\frac{3}{129.64}$ 

2. Find the reciprocals of the numbers 807 and 0.0591;

Hence evaluate 
$$5 + 4$$
  
 $807 = 0.0591$ 

3. Use reciprocal tables to find the value of:

$$\frac{1}{3} \left\{ \frac{2}{0.6638} + \frac{5}{0.833} \right\}$$

4. Find without using a calculator, the value of:

$$\frac{12\sqrt{0.0625} - 12.4 \div 0.4 \times 3}{^{1}/_{8} \text{ of } 2.56 + 8.68}$$

Use tables of cubes, cube roots and reciprocal to find the value of:-5.

$$(8.68)^3 + \left[\frac{5}{34.46}\right]^{1/3}$$

Determine the value of **a** for which  $\frac{1}{127} + \frac{1}{11.5} = \frac{1}{a}$  Use mathematical tables only 6.

- 7. Use tables of squares, square roots and reciprocals only to find the value of x correct to 4 significant figures:  $\mathbf{x} = \sqrt{\frac{1}{3.593^2} + \frac{2}{0.526}}$
- 8. Use reciprocal tables to find the value of;

$$\frac{1}{3} \left\{ \frac{2}{0.6638} + \frac{5}{0.833} \right\}$$
 30



9. Use tables of reciprocals only to work out;

$$\frac{3}{0.6735} + \frac{13}{0.156}$$

10. Using tables of squares, cube roots and reciprocals find the value of  $\mathbf{x}$ .

$$\frac{1}{x} = \frac{1}{0.002593^{1/3}} - \frac{1}{1.28^{2}}$$

#### 21. Common Logarithms.

1. Use mathematical table to evaluate.

- 2. Given that  $y = Bx^n$ . Make n the subject of the formula and simplify your answer
- 3. Without using mathematical tables or calculators evaluate:  $6\log_2 64 + 10\log_3(243)$
- 4. Find the value of x that satisfies the equation  $\log (2x 11) \log 2 = \log 3 \log x$
- 5. Use logarithms to evaluate to 3 significant figures

$$\frac{(0.5241)^2 \times 83.59}{\sqrt[3]{0.3563}}$$

6. Use logarithm tables in all your steps to evaluate:

$$\frac{38.32 \times 12.964}{86.37 \times 6.285}$$
 leaving your answer to four decimal places

7. Make **L** the subject in :

$$H = 3 \left[ \frac{3d (L - d)}{10L} \right]$$

8. Using logarithm tables solve.

$$\left(\frac{6.195 \times 11.82}{83.52}\right)^{1/4}$$

9. Solve the simultaneous equation:-

$$Log (x-1) + 2log y = 2log 3$$
$$log x + log y = log 6$$

10. Without using logarithms tables or calculator evaluate:-

$$\frac{4}{5}\log_{10}32 + \log_{10}50 - 3\log_{10}2$$

11. Use logarithms to evaluate:-

$$\frac{6.598}{(0.9895)^2 \times 0.004974^{0.75}}$$
 and express the answer in standard form

12. Solve for **x** given that :- 
$$\log (3x + 8) - 3\log 2 = \log (x-4)$$



13. In this question, show all the steps in your calculations, giving your answer at each stage. Use logarithms correct to 4 decimal places to evaluate:

14. Use logarithms to evaluate correct to 4 s.f

$$\frac{\sin 44.5}{\tan 14.90 \times \cos 82}$$

15. Without using logarithm tables evaluate:

$$3 \overline{\smash{)}3.264 \times 1.215 \times \boxed{12.25}} \\
1.088 \times 0.4725$$

- 16. Without using a calculator/mathematical tables, solve:  $Log_8(x + 5) log_8(x 3) = Log_8 4$
- 17. Use tables to calculate  $(6.57^2 + 6.57) \div (7.92^2 \times 30.08)$  (Give your answer to 4 decimal places)
- 18. If  $\log^2 = 0.30103$ , and  $\log^3 = 0.47712$ , calculate without using tables or calculators the value of  $\log 120$
- 19. Solve for x in the following equation;  $\text{Log}_2(3x 4) = \frac{1}{3} \log_2 8x^6 \log_2 4$
- 20. By showing all the steps, use logarithms to evaluate:  $\frac{5.627 \times (0.234)^3}{(8.237)^{\frac{1}{2}}}$
- 21. Solve the logarithmic equation:  $\log_{10} (6x 2) 1 = \log_{10} (x-3)$
- 22. In this question, show all the steps in your calculations, giving your answers at each stage. Use logarithms, correct to 4 d.p to evaluate:-

$$3 \overline{ \frac{(0.07526)^2}{1.789 + 4.863}}$$

23. Evaluate using logarithms

# 22. Equations of straight lines

- 1. A solid right pyramid has a rectangular base 10cm by 8cm and slanting edge 16cm. calculate:
  - (a) The vertical height
  - (b) The total surface area
  - (c) The volume of the pyramid
- 2. The line passing through the points A (-1, 3K) and B (K, 3) is parallel to the line whose equation is 2y + 3x = 9. Write down the co-ordinates of A and B
- 3. Find the value of **a** if the gradient of the graphs of the function  $y = x^2 x^3$  and y = x ax are equal at  $x = \frac{1}{3}$



- 4. Two perpendicular lines meet at the point (4,5). If one of the lines passes through the point (-2,1), determine the equation of the second line in the form ax + by + c = 0.
- 5. Find the equation of the line passing through (-5, 2) and with X-intercept as 3. Leave your answer in the form of  $\mathbf{Y} = \mathbf{m}\mathbf{X} + \mathbf{C}$ 
  - (a) copy and complete the table below:

x	0	1	2	3	4	5	6
y = 2x - 4							
y = 12 - 2x							

- (b) (i) On the grid provided and using the same axes, draw the lines y = 2x + 4 and y = 12 2x
  - (ii) Hence use your graphs to solve the simultaneous equations

$$\frac{1}{2}x - \frac{1}{4}y = 1$$
  
  $x + \frac{1}{2}y = 6$ 

(c) By use of substitution method, solve the simultaneous equations;

$$6x + 4y = 36$$
$$x + 3y = 13$$

- 7. Find the equation of a line through point -2, 4 which is parallel to 3y = -2x + 8. Express your answer in the form y = [mx + c]
- 8. Determine the equation of a line passing through (-1, 3) and parallel to the line whose equation is 3x 5y = 10
- 9. On a certain map, a road 20km long is represented by a line 4cm long. Calculate the area of a rectangular plot represented by dimensions 2.4cm by 1.5cm on this map leaving your answer in hectares
- 10. A straight line passing through point (-3,4) is perpendicular to the line whose equation is 2y-5x=11 and intersects the x-axis and y-axis at the points P and Q respectively. Find the co-ordinates of P and Q
- 11. A triangle ABC is formed by the points A(3, 4), B(-7, 2) and C(1, -2)
  - (a) Find the co-ordinates of the mid-points K of AB and P of AC
  - (b) Find the equation of the perpendicular bisector of the KP
- 12. The equation of line  $L_1$  is  $^{-3}/_5x + 3y = 6$ . Find the equation of a line  $L_2$  passing through point T(1, 2) and perpendicular to line  $L_1$
- 13. Determine the equation of a line passing through (-1, 3) and parallel to the line whose equation is 3x 5y = 10
- 14. A straight line through the points A (2, 1) and B (4, m) is perpendicular to the line, whose equation is 3y = 5-2x. Determine the value of **m**
- 15. Determine the equation of a line which is perpendicular to the line 2x + 3y + 4 = 0 and passes through P(1,1)
- 16. Koech bought 144 pineapples at shs.100 for every six pineapples. She sold some of them at shs.72 for every three and the rest at shs.60 for every two. If she made a profit of 40%; Calculate the number of pineapples sold at 72 for every three
- 17. Solve the equation  $\frac{x+2}{3} \frac{x-1}{2} = 5$

1.

# 23. Reflection and Congruence



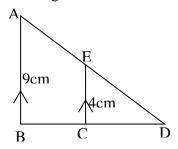
- 1. Given that A' (3, -3) is the image of A (-1, -5) under a reflection. Find the equation of the mirror line in the form of ax + by + c = 0 (4 mks)
  - Three planes **A**, **B** and **C** leave an airport **P** simultaneously at 9.30a.m. Plane **A** flies on a bearing of 070° from P at a speed of 400km/h. Plane **B** flies on a bearing of 290° at a speed of 500km/h. Plane C flies on a bearing of 162° from **P** at a speed of 300km/h. (*Use scale drawing for this question*)
    - (a) Show by scale drawing, the relative positions of the 3planes A, B and C three hours after leaving airport P. (Use scale 1cm represents 200km)
    - (b) After 3 hours,  $\bf B$  turns and head straight to the current position of  $\bf A$  at the same speed it had. Determine the scale drawing, the time it takes to reach this point, to the nearest minute
    - (c) Determine the bearing and distance of **B** from **C** after the first 3 hours of flight after leaving **P**

#### 24. Rotation

1. The ratio of the lengths of the corresponding sides of two similar rectangular water tanks is 3: 5. The volume of the smaller tank is 8.1m<sup>3</sup>. Calculate the volume of the larger tank

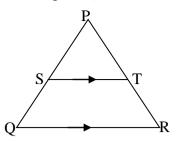
# 25. Similarities and Enlargement

- 1. Two tanks are similar in shape. The capacity of the tanks are 1,000,000 litres and 512, 000 litres respectively.
  - (a) Find the height of the smallest tank if the larger is 300cm tall (4 mks)
  - (b) Calculate the surface area of the larger tank if the smaller tank has a surface area of 1200m<sup>2</sup> (3 mks)
  - (c) Estimate the mass of the smaller tank if the mass of the larger one is 800kg (3 mks)
- 1. The image of P(0,2) under an enlargement with a scale factor 3 is  $P^1$  (4,6). Find the co-ordinates of Q
- 2. A model of a building is made using a scale 1:500.
  - (a) Find the height of a room (in meteres) in the building which is 5cm long on the model? S\*\*\*
  - (b) A room has a floor area of 36m<sup>2</sup>. What is the corresponding area on the floor of the model
  - (c) A room has a volume of 120m<sup>3</sup>. What is the corresponding volume of the model in cm<sup>3</sup>?S\*\*\*
- 3. In the triangle ABD, BA is parallel, to CE, given that BA= 9cm, CE = 4cm and AE = 3cm, find the length of DE

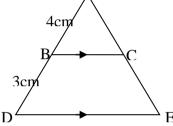




In the following figure, PR = 12cm, TR = 4cm and ST is parallel to QR. Given that the area of triangle PQR is  $336cm^2$ , find the area of quadrilateral QRTS



- 5. Two dogs regarded similar with the length in ratio 4:3:-
  - (a) If the bigger dog has a tail 64cm long, find the length of the tail of the smaller dog
  - (b) If the smaller dog requires 810g of meat per day how much meat per day does the bigger dog require
- 6. In the figure below, ADE is a triangle and BC is parallel to DE, AB, BD and BC are 4cm, 3cm and 8cm respectively.  $\Delta$

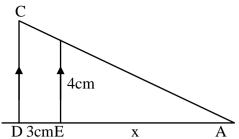


Find the length of DE

7. The surface area of two similar bottles are 12cm<sup>2</sup> and 108cm<sup>2</sup> respectively. If the larger one has a volume of 810cm<sup>3</sup>. Find the volume of the smaller one

8. Given that the area of the trapezium CDEB is  $15.6 \text{ cm}^2$ , find the length EA marked X.





# 26. The Pythagoras theorem

- 1. The angle of elevation of the top of a tree from a point P on the horizontal ground is 24.5°. From another point Q, five metres nearer to the base of the tree, the angle of elevation of the top of the tree is 33.2°. Calculate to one decimal place, the height of the tree
- 2. A block of wood in the shape of a frustrum of a cone of slanting edge 30 cm and base radius 10cm is cut parallel to the base, one third of the way from the base along the slanting edge. Find the ratio of the volume of the cone removed to the volume of the complete cone.

# 27. The Trigometric Ratio 1

- 1. At point A, David observed the top of a tall building at an angle of 30°. After walking for 100meters towards the foot of the building he stopped at point B where he observed it again at an angle of 60°. Find the height of the building
- 2. Find the value of  $\theta$ , given that  $\frac{1}{2}\sin\theta = 0.35$  for  $0^{\circ} \le \theta \le 360^{\circ}$
- 3. A man walks from point **A** towards the foot of a tall building 240 m away. After covering 180m, he observes that the angle of elevation of the top of the building is 45°. Determine the angle of elevation of the top of the building from **A**
- 4. The table below gives a field book showing the results of a survey of a section of a piece of land between A and E. All measurements are in metres.

	E	
<b>D</b> 33	95	
	90	<b>F</b> 36
<b>C</b> 21	70	
<b>B</b> 42	30	<b>G</b> 25
	25	<b>H</b> 40
	$\mathbf{A}$	

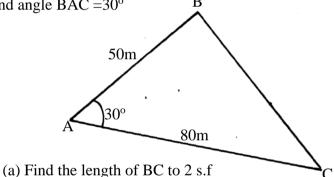
- (a) Draw a sketch of the land.
- (b) Calculate the area of this piece of land.
- 5. Solve for x in  $2 \cos 2x^0 = 0.6000 \ 0^0 \le x \le 360^0$ .
- 6. Wangechi whose eye level is 182cm tall observed the angle of elevation to the top of her house to be 32° from her eye level at point A. she walks 20m towards the house on a straight line to a point B at which point she observes the angle of elevation to the top of the building to the 40°. Calculate, correct to 2 decimal places the; a)distance of A from the house
  - b) The height of the house
- 7. Given that  $\cos A = \frac{5}{13}$  and angle A is acute, find the value of:-



- Given that  $\tan 5^{\circ} = 3 + 5$ , without using tables or a calculator, determine tan 25°, leaving your answer in the form a + b c
- A student whose eye level is 182cm from the ground observed the top of their house at an angle of elevation of 32° at point A. She walked for 20m towards the house along a straight road to a point **B**, where she observed the top of the building again at an angle of elevation of 40°. Calculate correct to 2 decimal places the:-
  - (a) Distance of A from the house
  - (b) The height of the house
- 10. Given that  $\tan \mathbf{x} = \underline{5}$ , find the value of the following without using mathematical tables or calculator:
  - (a) Cos x
  - (b)  $Sin^2(90-x)$
- 11. If  $\tan \theta = \frac{8}{15}$ , find the value of **Sin0** - **Cos0** without using a calculator or table  $\cos\theta + \sin\theta$

### 28. Area of a triangle

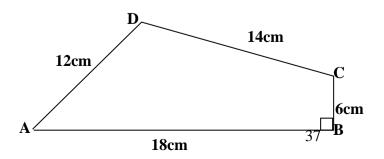
The figure below represents a triangular plot ABC. The lengths of AB = 50m, AC = 80m1. and angle BAC  $=30^{\circ}$ 



- (b) Find the area of the plot in hectares
- (c) The plot is fenced using 4 strands of barbed wire. The length of one roll of barbed wire is 600m and it costs shs.4000. Calculate;
- (i) The length of fencing wire required
- (ii) The number of complete rolls to be bought
- (iii) The cost of the rolls

# 29. Area of polygons

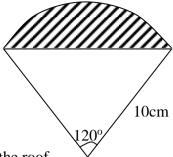
- Find the area of a regular polygon of length 10 cm and side **n**, given that the sum of interior 1. angles of  $\mathbf{n} : \mathbf{n} - \mathbf{1}$  is in the ratio 4 : 3.
- 2. Calculate the area of the quadrilateral ABCD shown:-





#### 30. Area of part of a circle

The ends of the roof of a workshop are segments of a circle of radius 10m. The roof is 20m long. The angle at the centre of the circle is 120° as shown in the figure below:



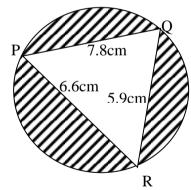
O

10cm

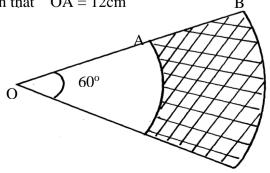
- (a) Calculate:-
- (i) The area of one end of the roof
- (ii) The area of the curved surface of the roof
- (b) What would be the cost to the nearest shilling of covering the two ends and the curved surface with galvanized iron sheets costing shs.310 per square metre
- 2. The diagram below, not drawn to scale, is a regular pengtagon circumscribed in a circle of radius 10cm at centre O



- (a) The side of the pentagon
- (b) The area of the shaded region
- 3. Triangle **PQR** is inscribed in he circle **PQ**= 7.8cm, **PR** = 6.6cm and **QR** = 5.9cm. Find:



- (a) The radius of the circle, correct to one decimal place
- (b) The angles of the triangle
- (c) The area of shaded region
- 4. The figure below represents sector OAC and OBD with radius OA and OB respectively. Given that OB is twice OA and angle  $AOC = 60^{\circ}$ . Calculate the area of the shaded region in  $m^2$ , given that OA = 12cm





D

#### 31. Surface Area of Solids

- A swimming pool water surface measures 10m long and 8m wide. A path of uniform width is made all round the swimming pool. The total area of the water surface and the path is 168m<sup>2</sup>
  - (a) Find the width of the path

(4 mks)

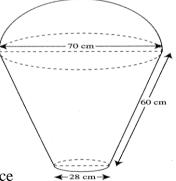
- (b) The path is to be covered with square concrete slabs. Each corner of the path is covered with a slab whose side is equal to the width of the path. The rest of the path is covered with slabs of side 50cm. The cost of making each corner slab is sh 600 while the cost of making each smaller slab is sh.50. Calculate
- (i) The number of the smaller slabs used

(4 mks)

(ii) The total cost of the slabs used to cover the whole path

(2 mks)

- 1. A lampshade is in the form of a frustrum of a cone. Its bottom and top diameters are 12cm and 8cm respectively. Its height is 6cm. Find;
  - (a) The area of the curved surface of the lampshade
  - (b) The material used for making the lampshade is sold at Kshs.800 per square metre. Find the cost of ten lampshades if a lampshade is sold at twice the cost of the material
- 2. A cylindrical piece of wood of radius 4.2cm and length 150cm is cut lengthwise into two equal pieces. Calculate the surface area of one piece
- 3. The base of an open rectangular tank is 3.2m by 2.8m. Its height is 2.4m. It contains water to a depth of 1.8m. Calculate the surface area inside the tank that is not in contact with water
- 4. The figure below represents a model of a solid structure in the shape of frustrum of a cone with a hemisphere top. The diameter of the hemispherical part is 70cm and is equal to the diameter of the top of the frustrum. The frustrum has a base diameter of 28cm and slant height of 60cm.



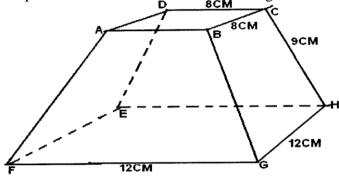
#### **Calculate:**

- (a) the area of the hemispherical surface
- (b) the slant height of cone from which the frustrum was cut
- (c) the surface area of frustrum
- (d) the area of the base
- (e) the total surface area of the model
- 5. A room is 6.8m long, 4.2m wide and 3.5m high. The room has two glass doors each measuring 75cm by 2.5m and a glass window measuring 400cm by 1.25m. The walls are to be painted except the window and doors.

- a) Find the total area of the four walls
- b) Find the area of the walls to be painted



- c) Paint **A** costs Shs.80 per litre and paint **B** costs Shs.35 per litre. 0.8 litres of **A** covers an area of 1m<sup>2</sup> while 0.5m<sup>2</sup> uses 1 litre of paint **B**. If two coats of each paint are to be applied. Find the cost of painting the walls using:
  - i) Paint A
  - ii) Paint B
- d) If paint A is packed in 400ml tins and paint B in 1.25litres tins, find the least number of tins of each type of paint that must be bought.
- 6. The figure below shows a solid frustrum of pyramid with a square top of side 8cm and a square base of side 12cm. The slant edge of the frustrum is 9cm



Calculate:

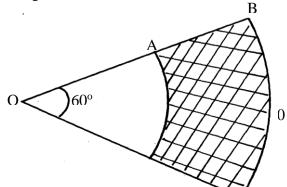
- (a) the total surface area of the frustrum
  - (b) the volume of the solid frustrum
  - (c) the angle between the planes BCHG and the base EFGH.

#### 32. Volume of solids

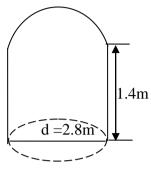
1. Metal cube of side 4.4cm was melted and the molten material used to make a sphere. Find to 3

significant figures the radius of the sphere 
$$\left(take \prod = \frac{22}{7}\right)$$
 (3 mks)

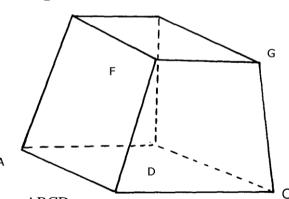
- 1. A solid right pyramid has a rectangular base 10cm by 8cm and slanting edge 16cm. calculate:
  - (a) The vertical height
  - (b) The total surface area
  - (c) The volume of the pyramid
- 2. A solid cylinder of radius 6cm and height 12cm is melted and cast into spherical balls of radius 3cm. Find the number of balls made
- 3. The sides of a rectangular water tank are in the ratio 1: 2:3. If the volume of the tank is 1024cm<sup>3</sup>. Find the dimensions of the tank. (4s.f)
- 4. The figure below represents sector OAC and OBD with radius OA and OB respectively. Given that OB is twice OA and angle  $AOC = 60^{\circ}$ . Calculate the area of the shaded region in  $m^2$ , given that OA = 12cm



The figure below shows a closed water tank comprising of a hemispherical part surmounted on top of a cylindrical part. The two parts have the same diameter of 2.8cm and the cylindrical part is 1.4m high as shown:-

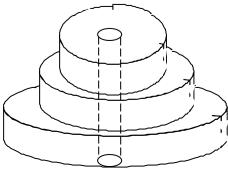


- (a) Taking  $\pi = \frac{22}{7}$ , calculate:
  - (i) The total surface area of the tank
  - (ii) the cost of painting the tank at shs.75 per square metre
  - (iii) The capacity of the tank in litres
- (b) Starting with the full tank, a family uses water from this tank at the rate of 185litres/day for the first 2days. After that the family uses water at the rate of 200 liters per day. Assuming that no more water is added, determine how many days it takes the family to use all the water from the tank since the first day
- 6. The figure below represents a frustrum of a right pyramid on a square base. The vertical height of the frustrum is 3 cm. Given that EF = FG = 6 cm and that AB = BC = 9 cm



Calculate;

- a) The vertical height of the pyramid.
- b) The surface area of the frustrum.
- c) Volume of the frustrum.
- d) The angle which line AE makes with the base ABCD.
- 7. A metal hemisphere of radius 12cm is melted done and recast into the shape of a cone of base radius 6cm. Find the perpendicular height of the cone
- 8. A solid consists of three discs each of 1½ cm thick with diameter of 4 cm, 6 cm and 8 cm respectively. A central hole 2 cm in diameter is drilled out as shown below. If the density of material used is 2.8 g/cm³, calculate its mass to 1 decimal place



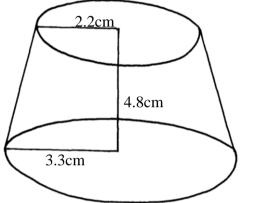


9. A right conical frustrum of base radius 7 cm and top radius 3.5 cm and height 6 cm is stuck onto a cylinder of base radius 7 cm and height 5 cm which is further attached to form a closed solid as shown below.

5cm



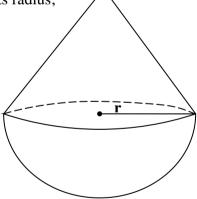
- a) The volume of the solid.
- b) The surface area of the solid.
- 10. The figure below shows a frustrum



Find the volume of the frustrum

11. The diagram below shows a metal solid consisting of a cone mounted on hemisphere.

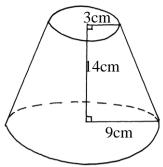
The height of the cone is 1½ times its radius;



Given that the volume of the solid is  $31.5\pi$  cm<sup>3</sup>, find:

- (a) The radius of the cone
- (b) The surface area of the solid
- (c) How much water will rise if the solid is immersed totally in a cylindrical container which contains some water, given the radius of the cylinder is 4cm
- (d) The density, in kg/m<sup>3</sup> of the solid given that the mass of the solid is 144gm
- 12. A solid metal sphere of volume 1280 cm<sup>3</sup> is melted down and recast into 20 equal solid cubes. Find the length of the side of each cube.
- 13. The figure below shows a frustrum cut from a cone

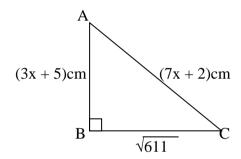




Calculate the volume of the frustrum

# 33. Quadratic equations

1. In a triangle ABC, angle B is 90°. Find the value of x and hence the area of the triangle



2. Solve the following inequalities and represent the solution on a number line hence state the integral values  $7x - 4 \le 9x + 2 < 3x + 14$ 

1.

### 34. Linear inequalities

Find without using a calculator, the value of:

$$\frac{12\sqrt{0.0625} - 12.4 \div 0.4 \times 3}{^{1}/_{8} \text{ of } 2.56 + 8.68}$$

2. Solve and write down all the integral values satisfying the inequality.

$$X - 9 \le -4 < 3x - 4$$

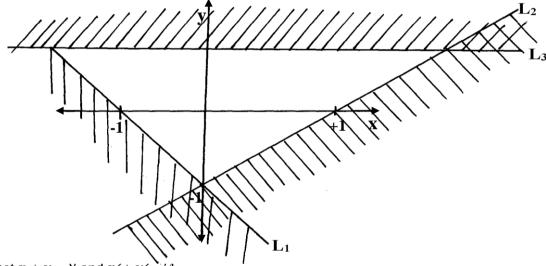
3. Solve the inequality and show the solution on the number line.

$$3-2x \angle x \angle 2x + 5$$

4. Show on a number line the range of all integral values of x which satisfy the following pair of inequalities:  $3 - x \le 1 - \frac{1}{2}x$ 

$$-\frac{1}{2}(x-5) \le 7-x$$

- 5. Solve the inequalities  $4x 3 \le 6x 1 < 3x + 8$ ; hence represent your solution on a number line
- 6. Find all the integral values of **x** which satisfy the inequalities 2(2-x) < 4x 9 < x + 11
- 7. Find the inequalities that define the unshaded region

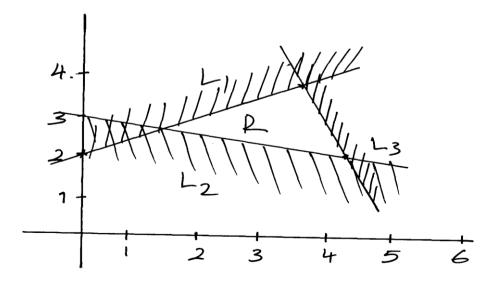


8. Given that x + y = 8 and  $x^2 + y^2 = 34$ 

Find the value of:- a)  $x^2+2xy+y^2$ 

b) 2xy

9. Find the inequalities satisfied by the region labelled **R** 

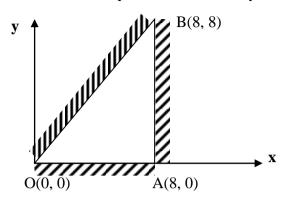


10. The region R is defined by  $x \ge 0$ ,  $y \ge -2$ ,  $2y + x \le 2$ . By drawing suitable straight line

- on a sketch, show and label the region R
- 11. Find all the integral values of x which satisfy the inequality 3(1+x) < 5x 11 < x + 45



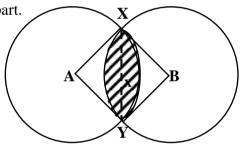
12. The vertices of the unshaded region in the figure below are O(0, 0), B(8, 8) and A(8, 0). Write down the inequalities which satisfy the unshaded region



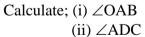
### 35. Angle Properties of Circles

1. Two circles of radii 4cm and 6cm intersect as shown below. If angle  $XBY = 30^{\circ}$  and angle  $XAY = 97.2^{\circ}$ .

Find the area of the shaded part. (Take =  $\pi \frac{22}{7}$ )

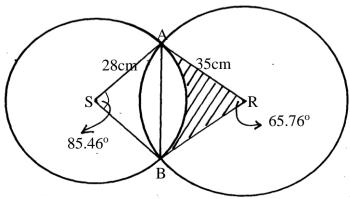


2. In the diagram, O is the centre of the circle and AD is parallel to BC. If angle ACB = $50^{\circ}$  and angle ACD =  $20^{\circ}$ .



3. Two intersecting circles have centres S and R. wo radii are 28cm and 35cm, their common chord AB = 38cm and angles ASB = 85.40 and ARB = 65.76 $^{\circ}$ ,

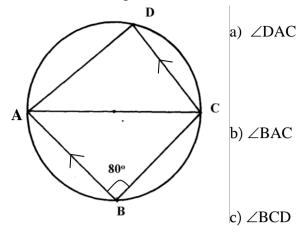
D





#### Calculate the shaded area

In the figure below ABCD is a cyclic quadrilateral in which AD = DC and AB is parallel to CD. Given that angle  $ABC = 80^{\circ}$ , Find the size of:



- 5. Line QR = 6.5cm is given below:-(*Do not use a protractor for this question*)
  - (a) Draw triangle PQR such that **p** lies above line QR,  $\angle$  PQR = 30° and PQ = 7cm

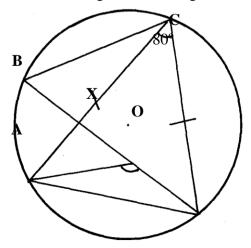


- (b) By accurate construction on the diagram above, show the locus of a point which lies within the triangle such that:-
  - (i) T is more than 2.5cm from line PQ and
  - (ii) T is not more than 4.5cm from Q Shade the region in which T lies
- (c) Lines QP and QR are produced to K and M respectively
  - (i) Show by construction on the diagram above, the locus of a point C which is equidistant from each of the lines PK, PR and RM
  - (ii) With centre C and an appropriate radius, draw a circle to touch each of the lines PK, PR and RM only once

Measure the radius

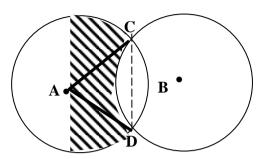
What name is given to the circle drawn in (c) (ii) with respect to triangle QPR

6. The figure below shows a circle centre  $\mathbf{O}$  and a cyclic quadrilateral ABCD. AC = CD, angle ACD is  $80^{\circ}$  and BOD is a straight line. Giving reasons for your answer, find the size of :-

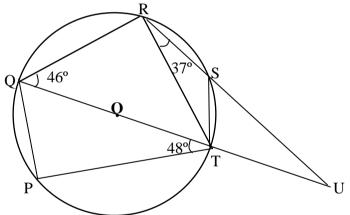


- (i) Angle ACB
- (ii) Angle AOD
- (iii) Angle CAB
- (iv) Angle ABC
- (v) Angle AXB
- The figure below shows two circles of equal radius of 9 cm with centres A and B. Angle  $CAD = 80^{\circ}$

D

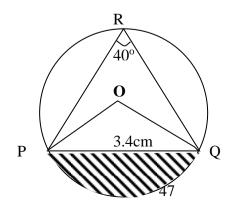


- a) Calculate the area of:
  - i) The sector CAD.
  - ii) The triangle CAD.
  - iii) The shaded region.
- 8. In the diagram below,  $\angle QOT$  is a diameter.  $\angle QTP = 48^{\circ}$ ,  $\angle TQR = 46^{\circ}$  and  $\angle SRT = 37^{\circ}$



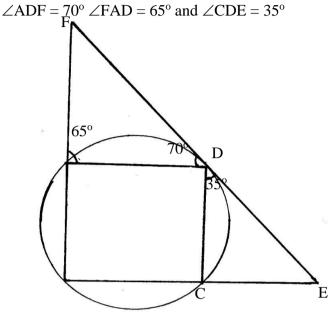
Calculate, giving reasons in each case:-

- (a) ∠RST
- (b) ∠SUT
- (c) ∠ROT
- (d) ∠PST
- (e) Reflex ∠SOP
- 9. The diagram below shows a circle with a chord PQ= 3.4cm and angle PRQ=40°. Calculate the area of the shaded segment.



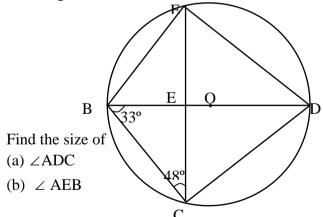


10. The figure below shows circle ABCD. The line EDF is a tangent to the circle at D.



Find the values of the following angles, stating your reasons in each case

- (a) ∠ABC
- (b) ∠BCD
- (c) ∠DCE
- (d) ∠ACD
- 10. In the figure below BD is the diameter of the circle and O is the centre.



# 36.Vectors

1. Given that  $4p-3q = \binom{10}{5}$  and  $p+2q = \binom{-14}{15}$  find

a) (i) p and q

- (3 ml<mark>Teacher.co.ke</mark>
- (iv) |p+2q| (3 mks)
- (b) Show that A (1, -1), B (3, 5) and C (5, 11) are collinear

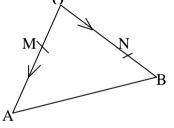
- (4 mks)
- 1. The position vectors of points x and y are x = 2i + j 3k and y = 3i + 2j 2k respectively. Find x y as a column vector (2 mks)
- 1. Express in surds form and rationalize the denominator.

$$\frac{1}{\sin 60^{\circ} \sin 45^{\circ} - \sin 45^{\circ}}$$

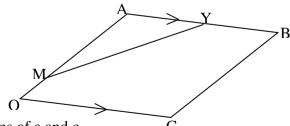
- 2. If  $\overrightarrow{OA} = 12i + 8j$  and  $\overrightarrow{OB} = 16i + 4j$ . Find the coordinates of the point which divides  $\overrightarrow{AB}$  internally in the ratio1:3
- 3. Find scalars **m** and **n** such that

$$\mathbf{m} \begin{bmatrix} 4 \\ 3 \end{bmatrix} + \mathbf{n} \begin{bmatrix} -3 \\ 2 \end{bmatrix} = \begin{bmatrix} 5 \\ 8 \end{bmatrix}$$

4. In a triangle OAB, M and N are points on OA and OB respectively, such that OM: MA = 2:3 and ON: NB = 2:1. **AN** and **BM** intersect at X. Given that OA = a and OB = b



- (a) Express in terms of a and b
  - (i) BM
  - (ii) AN
- (b) By taking  $\mathbf{BX} = \mathbf{t}$  and  $\mathbf{AX} = \mathbf{h}$   $\mathbf{AN}$ , where  $\mathbf{t}$  and  $\mathbf{h}$  are scalars, express  $\mathbf{OX}$  in two different ways
- (c) Find the values of the scalars t and h
- (d) Determine the ratios in which **X** divides :-
  - (i) **BM**
  - (ii) AN
- 5. OABC is a parallelogram, M is the mid-point of OA and  $AX = \frac{2}{7} AC$ , QA = a and QC = c

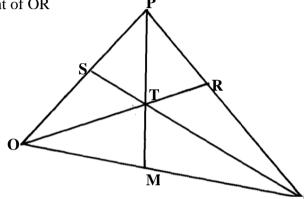


- (a) Express the following in terms of a and c
  - (i) MA
  - (ii) AB
  - (iii) AC

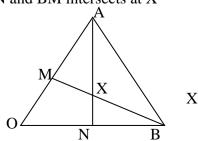
- (b) Using triangle MAX, express MX in terms of a and c
- (c) The co-ordinates of A and B are (1, 6, 8) and (3, 0, 4) respectively. If O is the origin and P the midpoint of AB. Find;
  - (i) Length of OP
  - (ii) How far are the midpoints of OA and OB?
- a) If A, B & C are the points (2, -4), (4, 0) and (1, 6) respectively, use the vector method to find the coordinates of point D given that ABCD is a parallelogram.
- b) The position vectors of points P and Q are  $\mathbf{p}$  and  $\mathbf{q}$  respectively. R is another point with position vector  $\mathbf{r} = \frac{3}{2} \mathbf{q}$   $\frac{1}{2} \mathbf{p}$ . Express in terms of P and q
- (i) PR

eacher.a

- (ii) PQ, hence show that P, Q & R are collinear.
- (iii) Determine the ratio PQ: QR
- 7. The figure shows a triangle of vectors in which OS: SP = 1:3, PR:RQ = 2:1 and T is the midpoint of OR  $\mathbf{P}$



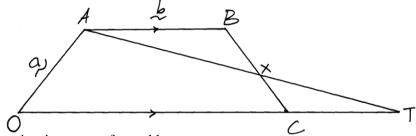
- a) Given that OP = p and OQ = q, express the following vectors in terms of P and q
  - i) OR
  - ii) OT
- b) Express **TS** in terms of **p** and **q** and hence show that the points **Q**, **T** and **S** are collinear
- c) M is a point on OQ such that OM = KOQ and PTM is a straight line. Given that PT: TM = 5:1, find the value of **k**
- 8. Given that a = 0, b = 0 and c = 0 and that  $p = 3q \frac{1}{2}b + \frac{1}{10}c$ Express  $\mathbf{p}$  as a column vector and hence calculate its magnitude  $\frac{1}{2}$  correct to two decimal places
- 9. In a triangle OAB, M and N are points on OA and OB respectively, such that OM:MA= 2:3 and ON:NB= 2:1. AN and BM intersect at X. Given that OA = **a** and OB = **b** 
  - (a) Express in terms of **a** and **b**:-
    - (i) BM
    - (ii) AN
  - (b) Taking BX = kBM and AX = hAN where **k** and **h** are constants express OX in terms of
    - (i) **a, b** and **k** only
    - (ii) **a, b**, and **h** only
  - (c) Use the expressions in (b) above to find values of **k** and **h**
- 10. In the figure below OAB is a triangle in which M divides OA in the ratio 2:3 and N divides OB in the ratio 4:1. AN and BM intersects at X



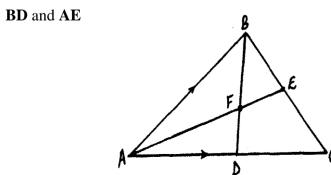


- (a) Given that OA = a and OB = b, express in terms of a and b
  - (i) AN
  - (ii) BM
  - (iii) AB
- (b) If  $\mathbf{A}\mathbf{X} = \mathbf{s}\mathbf{A}\mathbf{N}$  and  $\mathbf{B}\mathbf{X} = \mathbf{t}\mathbf{B}\mathbf{M}$ , where **s** and **t** are constants, write two expressions for  $\mathbf{O}\mathbf{X}$  in terms of  $\mathbf{a}$ ,  $\mathbf{b}$ ,  $\mathbf{s}$  and  $\mathbf{t}$ . Find the value of **s** and **t** hence write  $\mathbf{O}\mathbf{X}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$
- 11. A student traveling abroad for further studies sets a side Kshs. 115800 to be converted into US dollars through a bank at the rate of 76.84 per dollar. The bank charges a commission of 2 ½ % of the amount exchanged. If he plans to purchase text books and stationery worth US\$270, how much money, to the nearest dollar, will he be left with?
- 12. Given that:- r = 5i 2j and m = -2i + 6j k are the position vectors for R and M respectively. Find the length of vector RM  $\sim$
- OABC is a trapezium in which OA = a and AB = b. AB is parallel to OC with 2AB = OC.

  T is a point on OC produced so that OC: CT = 2:1. At and BC intersect at X so that BX = hBC and AX = KAT



- (a) Express the following in terms of a and b:-
  - (i) OB
  - (ii) BC
  - (b) Express  $\mathbf{CX}$  in terms of  $\mathbf{a}$ ,  $\mathbf{b}$  and  $\mathbf{b}$
- (c) Express **CX** in terms of a, b and k
- (d) Hence calculate the values of h and  ${\bf k}$
- 14. Given that  $\mathbf{a} = 2\mathbf{i} + \mathbf{j} 2\mathbf{k}$  and  $\mathbf{b} = -3\mathbf{i} + 4\mathbf{j} \mathbf{k}$  find:  $|\mathbf{a} + \mathbf{b}|$ .
- 15. In the figure below, **E** is the mid-point of **BC**. **AD:DC**=3:2 and **F** is the meeting point of





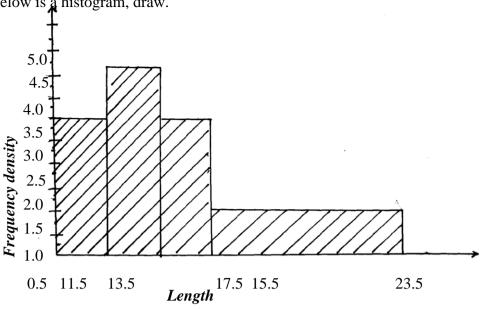
#### If AB = b and AC = c;

- (i) Express **BD** and **AE** in terms of **b** and **c**
- (ii) If BF = tBD and AF = nAE, find the values of t ad n
- (iii) State the ratios in which F divides BD and AE
- 16. The coordinates of point **O**, **A**, **B** and **C** are (0,0) (3,4) (11,6) and (8,2) respectively.

  A point **P** is such that the vector **OP**, **BA**, **BC** satisfy the vector equation **OP** = **BA** +  $\frac{1}{2}$  **BC**Find the coordinates of **P**
- 17. A point Q divides AB in the ratio 7:2. Given that A is (-3, 4) and B(2, -1). Find the co-ordinates of Q

### 37. Representation of data

1. Below is a histogram, draw.



Use the histogram above to complete the frequency table below:

Length	Frequency
$11.5 \le x \le 13.5$	
$13.5 \le x \le 15.5$	
$15.5 \le x \le 17.5$	
$17.5 \le x \le 23.5$	

2. Wambui spent her salary as follows:

	10
Food	40%
Transport	10%
Education	20%
Clothing	20%
Rent	10%

Draw a pie chart to represent the above information

2. The examination marks in a mathematics test for 60 students were as follows;-

<b>C</b> 1	7D. 11			T7	т.	T	10 04		
30	26	17	15	80	90	65	55	69	89
46	82	58	85	61	69	24	40	88	34
25	51	71	59	68	73	90	88	93	85
69	42	53	74	92	27	39	41	49	54
70	71	47	60	63	59	58	46	39	35
60	54	34	83	52	74	61	27	65	22

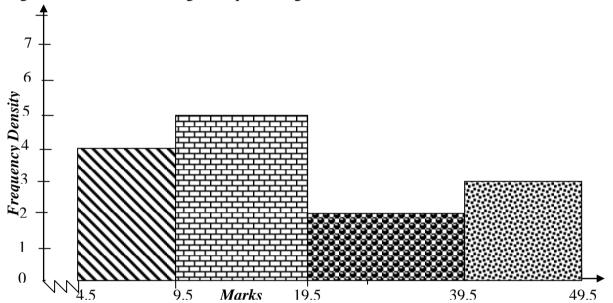
Class	Tally	Frequency	Upper class limit
10-29			
30-39			
40-69			
70-74			
75-89			
90-99			

From the table;

- (a) State the modal class
- (b) On the grid provided, draw a histogram to represent the above information The marks scored by 200 from 4 students of a school were recorded as in the table below.

Marks	41 – 50	51 - 55	56 – 65	66 - 70	71 - 85
Frequency	21	62	55	50	12

- (a) On the graph paper provided, draw a histogram to represent this information.
- (b) On the same diagram, construct a frequency polygon.
- (c) Use your histogram to estimate the modal mark.
- 5. The diagram below shows a histogram representing the marks obtained in a certain test:-



- (a) If the frequency of the first class is 20, prepare a frequency distribution table for the data
- (b) State the modal class
- (c) Estimate:
- (i) The mean mark
- (ii) The median mark
- 6. The data below shows the number of sessions different subjects are taught in a week.

Draw a pie chart to show the data:

Subject	Eng	Maths	Chemistry	C.R.E
No. of sessions	8	7	4	3

7. The height of 50 athletes in Moi University team were shown below:

Height (cm)	150-159	160-169	170-179	180-189	190-199	200-209
Frequency	2	9	12	16	7	4

- i) State the modal class
- ii) Calculate the median height of the athletes



The table below shows the length of 40 mango tree leaves;

tuele select shows the length of to mange tree leaves,							
Length (mm)	Frequency	Cumulative frequency					
118-126	3	3					
127-135	4	7					
136-144	10	17					
145-153	12	29					
154-162	5	34					
163-171	4	38					
172-180	2	40					

- (a) Determine the;
  - (i) Modal class
  - (ii) Median class
- (b) Calculate;
- (i) the mean of the leaves
- (ii) the median of the leaves

#### 38. Measures of central tendency

1. The results of a mathematics test that a hundred students took are as shown below:-

Marks	No. of students
30-34	4
35-39	6
40-44	10
45-49	14
50-54	X
55-59	24
60-64	14
65-69	6

- (a) Determine (i) the value of X
  - (ii) The modal class
  - (b) Calculate the mean
  - (c) The median
- 2. Without using logarithms or calculator evaluate:

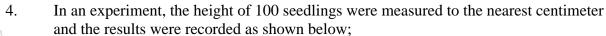
$$2\log_{10}5 - 3\log_{10}2 + \log_{10}32$$

3. The table below shows heights of 50 students :-

Height (cm)	Frequency
140-144	3
145-149	15
150-154	19
155-159	11
160-164	2

- (a) State the modal class(b) Calculate the median height





Height (cm)	20-24	25-29	30-34	35-39	40-44	45-49
Frequency	3	19	25	20	18	15

Calculate the median height

- 5. Given that x = -4 is a root of the equation  $2x^2 + 6x 2k = 0$ ; Find;
  - (a) the value of **k**
  - (b) the second root

Marks	60 - 62	63 - 68	69 – 73	74 - 80
Frequency	10	20	40	15

7. The table below shows the distribution of marks obtained by some candidates in a mathematics test

Marks	30-39	40-49	50-59	60-69	70-79	80-89	90-99
No. of candidates	2	3	10	12	8	3	2
c.f							

- a) state the total number of candidates who sat the test
- b) state the modal class
- c) calculate the mean mark using an assumed mean of 64.5 marks
- d) calculate the median mark
- 8. Find these statistics of the following data 4, 2, 2, 6, 1, 3, 4, 1, 4
  - a) Mode
  - b) Median
  - c) Mean
- 9. (a) The marks scored by a group of form two students in a mathematical test were as recorded in the table below:-

Marks	0-9	10-19	20-29	30-39	40-49	50-59	60-69	70-79	80-89	90-99
Frequency	1	2	4	7	10	16	20	6	3	1

- (a) (i) State the modal class
  - (ii) Determine the class in which the median mark lies
  - (iii) Using an assumed mean of 54.5, calculate the mean mark
- 10. Six weeks after planting, the height of maize plants were measured correct to the nearest centimeter. The frequency distribution is given in the table below:

Height (x)	$0 \le x < 4$	$4 \le x < 8$	$8 \le x < 12$	$12 \le x < 16$	$16 \le x < 20$
Frequency	3	8	19	14	6

Estimate the median height of the plants

11. Below are marks scored by student in maths talk in science congress.

Marks	1 - 5	6 - 15	16 - 20	21 - 35	36 – 40	41 - 50
No. of students	1	3	6	12	5	3

Draw a histogram from the table above.

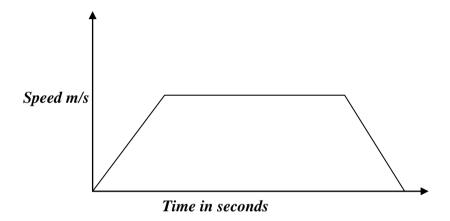




#### 39. Linear motion

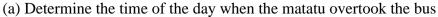


- Two motorists Kinyua and Nyaboke travelled between two towns K and M which are 580km apart. Kinyua started from K at 6.20 a.m and traveled towards M at 90km/hr. Nyaboke started from town M 1 <sup>2</sup>/<sub>3</sub> hours later and traveled towards town K at an average speed of 120km/h. At a small shopping centre along the way, Kinyua had a snack and car check for 20 minutes before proceeding
  - (a) (i) How far from town M did they meet?
    - (ii) At what time did they meet?
  - (b) A rally driver starts from town **M** going to town k at 9.30a.m. If he averages 180km/hr, Calculate the distance from **K** and the time when the rally driver overtook Nyaboke
- 2. The distance between two towns A and B is 150km. A car starts from town A at 10.00a.m and travels at an average speed of 80km/h towards B. A transit lorry travels from B at 10:15a.m towards town A at an average speed of 40km/h. At what time will the two vehicles meet?
- 3. The diagram below shows the speed-time graph for a bus traveling between two towns. The bus starts from rest and accelerates uniformly for 50seconds. It then travels at a constant speed for 150seconds and finally decelerates uniformly for 100seconds.



Given that the distance between the two towns is 2700m, calculate the;

- (a) maximum speed in km/h, the bus attained
- (b) acceleration
- (c) distance the bus traveled during the last 50seconds
- (d) time the bus takes to travel the first half of the journey
- 4. A cyclist covers a distance of 45 kilometres at a speed of 10km/h and a further 45 kilometres at 15km/h. Find his average speed for the journey
- 5. A lorry left town **A** for town **B** 1½ hours before a car. The lorry and the car are traveling in the same direction at  $80 \text{kmh}^{-1}$  and  $120 \text{kmh}^{-1}$  respectively. After the overtake, the car moved for  $\frac{199}{800}$  another hours before reaching town **B**. Calculate:
  - (a) The time the car took before overtaking the lorry completely
  - (b) The distance between the two towns
  - (c) The time the lorry will take to reach town **B** after the arrival of the car
- 6. A country bus left Nairobi at 10.45a.m and traveled towards Mombasa at an average speed of 60km/h. A matatu left Nairobi at 1:15p.m on the same day and traveled along the same road at an average speed of 100km/h. The distance between Nairobi and Mombasa is 500km.

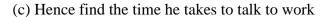




(b) Both vehicles continue towards Mombasa at their original speeds. How long had the matatu waited before the bus arrived?

7. Two passenger trains **A** and **B** which are 240m apart are travelling at 164km/h and 88km/h respectively approach on another one a straight railway line. Train **A** is 150m long and train **B** is 100m long. Determine the time in seconds that elapses before the two trains completely pass each other

- 8. A bus 5m long completely overtakes a trailer 15m long travelling in the same direction in 4.8. seconds. If the speed of the bus is 40 km/hr, determine the speed of the trailer in km/hr.
- 9. Find the LCM and GCD of the following numbers:  $2 \times 3 \times 5^3$  and  $2^4 \times 3^2 \times 5^2$ .
- 10. A boat sails from a point A to a point B upstream, a distance of 30 km and back to A in 3hrs 12 min. The current in the river is flowing at 5km/hr. Determine the speed of the boat in still water.
- 11.. Two friends Ojwang and David live 40 km apart. One day Ojwang left his house at 9.00 a.m. and cycled towards David's house at an average speed of 15 km/h. David left his house at 10.30 a.m. on the same day and cycled towards Ojwang's house at an average speed of 25 km/h.
  - a) Determine;
    - (i) The distance from Ojwang's house, where the two friends met.
    - (ii) The time they met.
    - (iii) How far Ojwang was from David's house when they met.
  - b) The two friends took 10 minutes at the meeting point and they cycled to David's house at an average speed of 12 km/h. Find the time they arrived at David's house.
- 12. Mr. Kamau left town **S** at 6.00a.m and travels at an average speed of 24km/hr towards **R**. Mrs. Ronoh left town **R** to town **S** 10minutes later and arrived at 7.00a.m. If distance **RS** = 42km, find;
  - (a) Where and when they will meet
  - (b) The time Kamau arrived at **R**
  - (c) If at 7.00a.m another traveler left **S** and travels towards R at speed twice that of Mrs. Ronoh, find where and when Mr. Kamau was overtaken by the traveler if so
- 13. A train 100m long travelling at 72km/hr, overtakes another train traveling in the same direction at 56km/hr and passes it completely in 54 seconds.
  - i) Find the length of the second train
  - ii) Find also the time they would have taken to pass one another if they had been traveling at these speeds in opposite directions
- 14. An unskilled worker may either walk to work along a route 5km to take a bus journey of 7km. The average speed of the bus is 24km/hr faster than his average speed. Taking the average walking speed as **x** km/hr;
  - (a) Write down expressions for time of the journey;
    - (i) When walking
    - (ii) When using the bus
  - (b) The journey by bus takes 36 minutes less than the journey on foot, find his walking speed





- 15. At 1.50 p.m. a matatu is traveling at 80 km/h and it is 40 km behind a motorcycle traveling at 60 km/h.
  - (a) After how long will the matatu overtake the motorcycle?
  - (b) At what time will the matatu overtake the motorcycle?
- 16. A bus left Nairobi at 8:00a.m and traveled towards Kisumu at an average speed of 80km/h.

At 8.30a.m, a car left Kisumu towards Nairobi at an average speed of 120km/hr. Given that the distance between Nairobi and Kisumu is 400km. Calculate:-

- (a) The time the car arrived in Nairobi
- (b) The time the two vehicles met
- (c) The distance from Nairobi to the meeting point
- (d) The distance of the bus from Kisumu when the car arrived in Nairobi
- 17. Two trucks A and B travelling at 28km/hr and 26km/hr respectively approach one another on a straight road. Truck A is 10m long, while truck B is 15m long. Determine the time in seconds that elapses before the trucks completely pass each other

# 40. Quadratic expressions and equation 2

1. Complete the table below for the function  $y = 2x^3 + 5x^2 - x - 6$  (2 mks)

X	-4	-3	-2	-1	0	1	2
2x <sup>3</sup>	-128	-54			0	2	16
5x <sup>2</sup>	80	45	20	5	0	5	20
-X	4	3			0	-1	
-6	-6	-6	-6	-6	-6	-6	-6
у	-50				-6	0	

(b) On the grid provided draw the graph  $y = 2x^3 + 5x^2 - x - 6$  for  $-4 \le x \le 2$ . Use 2cm to

represent 1 unit on the x-axis and 1 cm to represent 5 units on the y – axis (4 mks)

(c) By drawing a suitable line, use the graph in (b) to solve the

i. equation 
$$2x^3 + 5x^2 + x - 4 = 0$$
 (2 mks)

ii. equation 
$$2x^3 + 5x^2 - x + 2 = 0$$
 (2 mks)

- 1. (a) Use a convenient scale to draw the graph of  $y = -x^2 + 5x 3$  for the range  $-2 \le x \le 6$ 
  - (b) Use your graph to determine the roots of the equation  $5x x^2 3 = 0$
  - (c) Use your graph to solve the equation  $2x x^2 + 3 = 0$  by drawing a suitable straight line
- 2. Find a quadratic equation whose roots are  $2.5 + \sqrt{3}$  and  $2.5 \sqrt{3}$ , expressing it in the form  $ax^2 + bx + c = 0$  Where a, b and c are integers



Find the products of 17.3 and 13.8. Find also the percentage error in getting the product. 3.

(a) Complete the table below for the equation :-  $y = x^2 + 3x - 6$  for  $-6 \le x \le 4$ 

X	ζ.	-6	-5	-4	-3	-2	-1	0	1	2	3	4
У	7	12			-6			-6				22

(b) Using a scale 1cm to represent 2 units in both axes. Draw the graph of  $y = x^2 + 3x - 6$ (c) Use your graph to solve:-

(i) 
$$X^2 + 3X = 6$$

(i) 
$$X^2 + 3X = 6$$
  
(ii)  $X^2 + 3X - 2 = 0$ 

(a) Complete the table for the function:  $y = 2x^2 + 3x + 1$ 5.

X	- 4	-3	-2	-1	0	1	2	3
$2x^2$		18			0			18
3x + 1		-7			0			10
y		11			1	6		

(b) Use the table in (a) above to draw the graph:  $-y = 2x^2 + 3x + 1$  for  $-4 \le x \le 3$ 

(c) Use the graph in (b) to solve the equation :-

(i) 
$$2x^2 + 4x - 3 = 0$$

(ii) 
$$x^2 + \underline{3}x + 2 = 3$$

- 6. A youth group decided to raise Ksh 480,000 to buy a piece of land costing Ksh. 80,000 per hectare. Before the actual payment was made, four of the members pulled out and each of the remaining had to pay an additional Kshs. 20,000.
  - (a) If the original number of the group members was x, write down;
    - (i) An expression of how much each was to contribute originally.
    - (ii) An expression of how the remaining members were to contribute after the four pulled out.
  - (b) Determine the number of members who actually contributed towards the purchase of the land.
  - (c) Calculate the ratio of the supposed original contribution to the new contribution.
  - (d) If the land was sub-divided equally, find the size of land each member got. (2 mk)
- 7. a) Draw the graph of  $y = 2x^2 + x 2$  given the range  $-3 \le x \le 2$ 
  - b) Use your graph above to solve
    - i)  $2x^2 + x 2 = 0$
    - ii)  $2x^2 + x 3 = 0$
    - iii)  $2x^2 + x-5 = 0$
- 8. Three planes **A**, **B** and **C** leave an airport **P** simultaneously at 9.30a.m. Plane **A** flies on a bearing of 070° from P at a speed of 400km/h. Plane **B** flies on a bearing of 290° at a speed of 500km/h. Plane C flies on a bearing of 162° from **P** at a speed of 300km/h. (*Use scale drawing for this question*)
  - (a) Show by scale drawing, the relative positions of the 3planes A, B and C three hours after leaving airport P. (Use scale 1cm represents 200km)
  - (b) After 3 hours,  $\bf B$  turns and head straight to the current position of  $\bf A$  at the same speed it had. Determine the scale drawing , the time it takes to reach this point, to the nearest minute
  - (c) Determine the bearing and distance of  $\bf B$  from  $\bf C$  after the first 3 hours of flight after leaving  $\bf P$
- 9. a) Use trapezoidal rule to find the area between the curve  $y = x^2 + 4x + 4$ , the x- axis and the co-ordinates x = -2 and x = 1. Take values of x at intervals of  $\frac{1}{2}$  unit.
  - b) Use integration to find the exact area. Hence find the percentage error in your approximation.
- 10. a) Use trapezoidal rule to find the area between the curve  $y = x^2 + 4x + 4$ , the x- axis and the co-ordinates x = -2 and x = 1. Take values of x at intervals of  $\frac{1}{2}$  unit.
  - b) Use integration to find the exact area. Hence find the percentage error in your approximation.
- 11. Draw the graph of  $y = 2x^2 4x 5$  for x between -3 and 5 on the grid provided
  - (a) State the line of symmetry for the graph
  - (b) State the range of values for which  $2x^2 4x 5 \le 0$
  - (c) On the same set of axes, draw the graph of y=2x +3
  - (d) Determine the solutions to the equation:  $2x^2 4x 5 = 2x + 3$
- 12. Complete the table below for the equation  $y = 5 + 3x 2x^2$  by filling in the blank space

X	-2	-1.5	-1	-0.5	0	0.5	1	1.5	2	2.5	3	3.5
Y	-9			3		6	6				-4	

- (i) Use the values from the table above to draw the graph of  $y = 5 + 3x 2x^2$
- (3mks

- (ii) Use the graph to:-
  - (a) Find the maximum point of the function  $5 + 3x 2x^2$
  - (b) Determine the range of values and give the integral values which satisfy the inequality  $5 + 3x 2x^2 \ge -2$

13. (a) Complete the table below for the function  $y = 2x^2 + 4x - 3$ 

X	-4	-3	-2	-1	0	1	2
$2x^2$	32		8	2	0		
4x - 3			-11		-3		5
V			-3			3	13

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- (b) Draw the graph of the function  $y = 2x^2 + 4x 3$  and use your graph to estimate the roots of the equation  $2x^2 + 4x 3 = 0$ .
- (c) In order to solve graphically the equation  $2x^2 + x 5 = 0$ , a straight line must be drawn to intersect the curve  $y = 2x^2 + 4x 3$ . Determine the equation of this line, draw it and hence obtain the roots of the equation  $2x^2 + x 5 = 0$  to 1 decimal place.

14. a) Complete the table for the function  $y = 1 - 2x - 3x^2 - 3 \le x \le 3$ .

X	-3	-2	-1	0	1	2	3
$-3x^2$	-27		-3	0		-12	
-2x		4		0			-6
1	1	1	1	1	1	1	1
y	-20			1		-15	

- b) Using the table above, draw the graph of  $y = 1 2x 3x^2$  (Scale 1 cm represent 0.5 units on **x-axis** and 1 cm rep 2 units on the **y axis** on the grid provided.
- c) Use the graph in (b) above to solve.

(i) 
$$1 - 2x - 3x^2 = 0$$

(ii) 
$$2 - 5x - 3x^2 = 0$$

- 15. A quadratic equation  $\mathbf{x}^2 + \mathbf{a}\mathbf{x} \mathbf{b} = \mathbf{0}$  has roots 1 and -5, determine the values of  $\mathbf{a}$  and  $\mathbf{b}$
- 16. Find a quadratic equation whose roots are  $1.5 + \sqrt{2}$  and  $1.5 \sqrt{2}$ , expressing it in the form  $ax^2 + bx + c = 0$ , where a, b, and c are integers
- 17. If  $a^2 + b^2 = 89$  and a + b = 13
  - (a) Find the values of;

(i) 
$$a^2 + 2ab + b^2$$

- (ii) 2ab
- (iii)  $a^2 2ab + b^2$
- (iv) a b
- (b) Determine the values of a and b

#### 41. Approximation and errors

- 1. A rectangular room has length 12.0 metres and width 8.0 metres. Find the maximum percentage error in estimating the perimeter of the room.
- 2. In this question mathematical tables or calculator should not used. The base and perpendicular height of a triangle measured to the nearest centimeters are 12cm and 8cm respectively; Find;
  - (a) the absolute error in calculating the are of the triangle
  - b) the percentage error in the area, giving the answer to 1 decimal place
- 3. A rectangular plate has a perimeter of 28cm. determine the dimensions of the plate that



- 4. A wire of length 5.2m is cut into two pieces without wastage. One of the pieces is 3.08m long. What is the shortest possible length of the second piece?
- 5. The dimensions of a rectangle are 10cm and 15cm. If there is an error of 5% in each of the Measurements. Find the percentage error in the area of the rectangle.
- 6. Find the products of 17.3 and 13.8. Find also the percentage error in getting the product.
- 7. The mass of a metal is given as 14kg to the nearest l0g. Find the percentage error in this measurement.
- 8. Complete the table below for the functions  $y = \cos x$  and  $y = 2 \cos (x + 30^\circ)$  for  $0^\circ \le X \le 360^\circ$

X	0°	30°	60°	90°	120°	150°	180°	210°	240°	270°	300°	330°	360°
Cos X	1	0.87	0.5		-0.5	0.87	-1.0		0.5	0		0.87	1
2 cos	1.7		0	-		-2.0	-1.73	-1.0		1	1.73	2.00	1.73
(x+	3			1.0									
30°)													

- a) On the same axis, draw the graphs of  $y = \cos x$  and  $y = 2 \cos (x + 30^\circ)$  for  $0^\circ \le X \le 360^\circ$
- b) i) State the amplitude of the graph  $y = \cos x^{\circ}$ 
  - ii) State the period of the graph  $y = 2\cos(x + 30^{\circ})$
- c) Use your graph to solve

$$\cos x = 2 \cos (x + 30^{\circ})$$

9. Given that  $8 \le y \le 12$  and  $1 \le x \le 6$ , find the maximum possible value of:

$$\frac{y+x}{v-x}$$

# 42. Trigometry 2

- 1. If  $\tan x^{\circ} = \frac{12}{5}$  and x is a reflex angle, find the value of  $5\sin x + \cos x$  without using a calculator or mathematical tables
- 2. Find  $\theta$  given that  $2 \cos 3\theta 1 = 0$  for  $0^{\circ} \le \theta \le 360^{\circ}$
- 3. Without a mathematical table or a calculator, simplify: Cos300° x Sin120° giving your answer in Cos330° Sin 405° rationalized surd form.
- 4. Express in surds form and rationalize the denominator.

5. Simplify the following without using tables;

Tan 45 + cos 45sin 60

6. Simplify the following surds in the form of  $\mathbf{a} + \sqrt{\mathbf{b}} \mathbf{c}$  where  $\mathbf{a}$ ,  $\mathbf{b}$ , and  $\mathbf{c}$  are constants

$$\frac{5}{2\sqrt{2}}$$
 +  $\frac{2}{2 \cdot 2 \cdot \sqrt{5}}$ 

8. John cycles from shopping centre **A** on a bearing of  $120^{\circ}$  for 5 km to shopping centre **B**. He then cycles on a bearing of  $200^{\circ}$  for 7 km to the shopping centre **C**. Calculate to 1 decimal place.

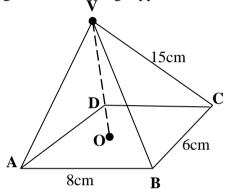
- a) The direct distance from A to C.
- b) The bearing of A from C.
- c) Bearing of B from C.

#### 43. Surds

- 1. Simplify;  $\frac{3}{7} 2^+ \sqrt{7}$  leaving the answer in the form  $\mathbf{a} + \mathbf{b} \sqrt{\mathbf{c}}$ , where  $\mathbf{a}, \mathbf{b}$  and  $\mathbf{c}$  are rational numbers  $\sqrt{7} 2^+ \sqrt{7}$
- 2. Given that:-  $\frac{2+\sqrt{5}}{2-\sqrt{5}}$   $\frac{3+\sqrt{5}}{2+\sqrt{5}}$  =  $a+b\sqrt{5}$  Find the values of **a** and **b** where **a** and **b** are rational numbers

3. If:- 
$$\frac{4}{\sqrt{7} - \sqrt{12}}$$
 -  $\frac{4}{\sqrt{7} + \sqrt{2}}$  =  $a\sqrt{7} + b\sqrt{2}$  Find the values of **a** and **b**, where **a** and **b** are rational numbers \*

- 4. Rationalize the denominator  $\frac{2-\sqrt{2}}{(\sqrt{2}-1)^3}$  and express your answer in the form of a+c 2
- 5. The figure below is a right pyramid with a rectangular base ABCD and vertex V.



O is the centre of the base and M is a point on OV such that  $OM = \frac{1}{3} OV$ , AB = 8 cm, BC = 6 cm and VA = VB = VD = VC = 15 cm. Find;

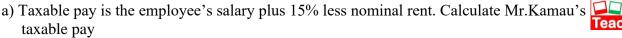
- i) The height OV of the pyramid.
- ii) The angle between the plane BMC and base ABCD.
- 6. Find the value of **y** which satisfies the equation  $Log_{10} 5 2 + log_{10} (2y + 10) = log_{10} (y 4)$
- 7. Simplify the expression  $\sqrt{3} \sqrt{2}$  giving your answer in the for of  $a + b \sqrt{c}$ .

# 44. Further logarithms

- 1. In this question, show all the steps in your calculations, giving the answer at each stage. Use logarithms correct to 4 decimal places, to evaluate; (1934)<sup>2</sup> x 0.00324 Log 746
- 2. The table below shows monthly income tax rates

Monthly taxable pay in KE	Rate of the tax (Kshs/ E)
1 - 342	2
343 – 684	3
685 - 1026	4
1027 - 1368	5
1369 – 1710	6
1710 and above	7

Mr. Kamau who is a civil servant earns a Monthly salary of Kshs.20000 and is provided with a house at a nominal rent of Kshs.700 per month





- b) Calculate the total tax Mr. Kamau pays
- c) Mr. Kamau is entitled to a personal relief of Kshs.600 per month. What was his net tax.
- d) Mr. Kamau has the following deductions made on his pay;

Loan repayment of Kshs.2100 per month

NSSF Kshs.200 per month

WCPS calculated at 2 % of monthly salary

Calculate Mr. Kipchokes net pay

- 3. A man bought a matatu at Kshs.400,000 in January 1999. It depreciated at a rate of 16% per annum. If he valued it six months, calculate its value in January 2003
- 4. The table shows corresponding values of x and y for a certain curve;

x	1.0	1.2	1.4	1.6	1.8	2.0	2.3
У	6.5	6.2	5.2	4.3	4.0	2.6	2.4

Using 3 strips and mid-ordinate rule estimate the area between the curve, x-axis, the lines x = 1 and x = 2.2

5. Evaluate without using a calculator or mathematical tables.

$$\frac{\text{Log } 32 + \log 128 - \log 729}{\text{Log } 32 + \log 2 - \log 27}$$

6. Find the value of  $\mathbf{x}$  that satisfies the equation:

$$\log (x+5) = \log 4 - \log(x+2)$$

- 7. Find the least number of terms for which the sum of the GP  $100 + 200 + 400 + \dots$  exceeds 3100.
- 8. A two digit number is formed from the first four prime numbers.
  - a) Draw the table to show the possible outcomes, if each number can be used only once.
  - b) Calculate the probability that a number chosen from the digit numbers is an even number
- 9. Find the gradient of a line joining the centre of a circle whose equation is  $x^2 + y^2 6x = 3 4y$  and a point P(6,7) outside the circle..
- 10. A lady invests shs.10,000 in an account which pays 16% interest p.a. The interest is compounded quarterly. Find the amount in the account after 1½ hrs
- 11. Use logarithm tables to evaluate

$$\frac{3}{63.5}$$
  $\frac{13.6 \cos 40^{\circ}}{63.5}$ 

12. Without using logarithms or calculator evaluate:

$$2\log_{10}5 - 3\log_{10}2 + \log_{10}32$$

13. Evaluate without using tables or calculators.

$$Log (3x + 8) - 3 log 2 = log (x - 4)$$

### 45. Commercial Arithmetic 2

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Chepkemoi bought a new washing machine for Kshs.420,000. Its value depreciated over the next 5years at the following rates; 15%, 13%, 12%, 9% and 7%. For the next 6 years, the rate of depreciation remained constant at 5% then the rate of depreciation remained at 4% each. How long did it take for the value of the washing machine to be  $^{1}/_{3}$  of its original value?

2.

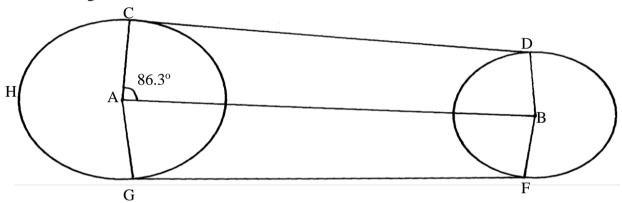
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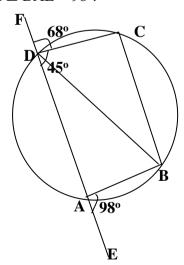
Taxable income in shs. Pa	Rate of tax in %
1 - 120,000	10
120,001 – 240,000	15
240,001 – 360,000	25
360,001 – 480,000	35
Over 480,000	50

Nafula is married and claims a tax relief of shs.1,120 per month. She stays in a company house For which she pays a nominal rent of shs.1200 per month. She found that in a particular month, her employer deducted shs.4830 as tax. If she is entitled to a maximum insurance policy; relief of shs.600 per month. Calculate her monthly salary. (10mks)

3. The figure below represents two pulley wheels, centres A and B with a rubber band CDEFGHC stretched round them. Radius of wheel centre A = 16cm, AB = 30cm. CD, GF are tangents to the circles  $< CAB = 86.3^{\circ}$ 



- a) calculate the length of the belt CD
- b) Find the angle ABD
- c) Find the length of the belt that would go round the pulleys (CDFGHC)
- 4. In the figure below, ABCD is a cyclic quadrilateral and BD is a diagonal. EADF is a straight line,  $\angle CDF = 68^{\circ}$ ,  $\angle BDC = 45^{\circ}$  and  $\angle BAE = 98^{\circ}$ .



Calculate the size of:

- a)  $\angle$  ABD.
- b)  $\angle$  CBD
- 5. A customer deposited Ksh.15,500 in a savings account. Find the accumulated amount after 3½ years if interest was paid at 16% per annum compounded semi-annually
- 6. A retailer mixes three types of rice, Bismatti costing shs.120 per tin with Pishori costing shs.150 per tin and Ahero rice costing shs.80 per tin in the ratio  $\mathbf{x} : \mathbf{1} : \mathbf{2}$  respectively. If he sells the

mixture at shs.137.50 per tin making a profit of 25%. Calculate the value of x.



7. Ashanti is a saleswoman and earns a commission on sales based on the monthly rates shown in the table below:-

Sales (Kshs)	Commission rate % of sales
The first 5000	10%
The next 3000	15%
Sales above 8000	20%

In addition, she earns a basic monthly pay of Kshs.6700. During a certain month, she earned a total salary amounting to Kshs.8368. How much worth of sales did she make?

9. The table below shows the annual income tax rates for a certain year.

Total income per month in Kshs.	Rates in Kshs. Per £	
1-10164	2	
10165 – 19740	3	
19741 – 29316	4	
29317 – 33892	5	
388983 and above	6	
Automatic personal relief shs.1162		

Kiptoo earns a monthly salary of Kshs.25000. He is entitled to house and medical allowances of Kshs.12000 and Kshs.3000 respectively

Calculate:

Teacher.a

- (a) His taxable income per month
- (b) His monthly tax payable
- (c)His annual tax payable
- 10. A company employee earns a basic salary of Kshs.25,000 and is also given taxable allowances amounting to Kshs.10,480.

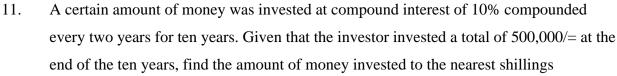
Monthly taxable income	Rate in Kshs. /Pound
1- 4350	2
4351 – 8900	3
8901 - 13455	4
13451 – 18005	5
18006 and above	6

Using the table of taxation above:-

- (a) Calculate the employee's taxable income
- (b) If the employee is entitled to a personal tax relief of Kshs.800 per month, determine the net tax
- (c) If the employee was given 40% increase in his income, calculate the percentage increase









- 12. The cash price of a T.V set is Ksh. 26,000. Linda bought the set on hire purchase terms by paying a deposit of Ksh. 6,000 and the balance by 24 equal monthly installments of Khs. 1,045.30. Find the compound rate of interest per year.
- 13. What would Kshs.15000 amount to after 3 years at 16% per annum compounded quarterly?
- 14. Income rates for income earned were charged as follows:

Income in Kshs. p.m	Rate in Kshs. per sh.20
1- 8400	2
8401- 18,000	3
18,001- 30,000	4
30,000 - 36,000	5
36,001 - 48,000	6
48,001 and above	7

A civil servant earns a monthly salary of Ksh.19,200. His house allowance is Ksh12,000 per month. Other allowces per month are transport Ksh.1300 and medical allowance Ksh.2300. He is entitled to a family relief of Kshs. 1240 per month.

#### **Determine:**

- a) (i) His taxable income per month.
  - (ii) Net tax.
- b) In addition, the following deductions were made

NHIF	shs. 230
Service charge	Kshs. 100
Loan repayment	Kshs. 4000
Co-operative shares of	Kshs. 1200.

Calculate his net salary per month.

15. Use the taxation rates in the table below to answer the questions that follow;-

Taxable income in K £ p.a	Rate % per K£
1-4500	10
4501-7500	15
7501 - 10500	20
10501 - 13500	25
13501 - 16500	30
Over 16500	35

The manager of a certain company is entitled to a monthly personal relief of shs.3000 and her tax (PAYE) is kshs.9000 per month she is also deducted NHIF shs.350 per month, WCPS shs.800 per month and cooperative shares shs.1200 per month, **calculate** 

- (a) The managers total deductions per month
- (b) Total tax per month
- (c) The manager's annual gross salary
- (d) The manager's monthly basic salary if her monthly allowance and medical allowances are 10000 and 2000 shillings

16. The table below shows the income tax for a certain year;

Monthly taxable income (Kshs.)	Tax rates (%)
1- 9680	10%
9681- 18800	15%
18801 - 27920	20%
27921 - 37040	25%
37940 and above	30%

In that year, Odero paid a net tax of Kshs.5,512 per month. His total monthly taxable allowances amounted to Kshs.15,220 and he was entitled to a monthly personal relief of kshs.1,162.

Every month the following deductions were made;

N.H.I.F Kshs.320

Union dues Kshs.200

Co-operative shares Kshs.7,500

- (a) Calculate Odero's monthly basic salary in Kshs
- (b) Calculate his monthly salary
- 17. (a) A car is worth shs.800,000 when new. During the first year it depreciates by 20% of its value and in the second it deprecates by 5% of its value at the start of the year. During the third, fourth and fifth year, depreciation rate is 10%. How much less will it cost at the end of the fifth year?
  - (b) Find by how much the compound interest will exceed simple interest on shs.3,000 for two years at 15% per year
- 18. The table below shows the income tax rates:

Income per month (K£)	Rate in Kshs per £
1 - 325	2
326 - 975	3
976 - 1300	5
1301 - 1625	6
Over 1625	7.50

Mr. Misoi is a public servant who lives in a government house and pays a nominal rent of Kshs.1,220 per month. He earns a basic salary of Kshs. 24,800 and a house allowance of Kshs.12,000 per month. He is entitled to a monthly relief of kshs.1620.

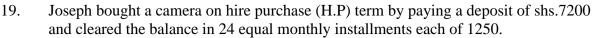
- (a) Calculate his monthly;
  - (i) Taxable income in K£
  - (ii) Tax payable without relief
  - (iii) Tax after relief
- (b) Apart from the income tax. The following monthly deductions are made from his earnings
  - -HELB loan repayment Kshs.2400
  - Health insurance fund Kshs.1200
  - 2% of Basic salary union fee

Calculate:- (i) the total monthly deduction made on Mr. Misoi's income

(ii) Mr. Misoi's net income per month









- (a) find the hire purchase price of the camera
- (b) the hire purchase price of the camera is 24% higher than the cash price. Find the cash price of the camera
- (c) Kangara took a loan from a financial institution and bought the camera with cash. He repaid the loan at 18% p.a compound interest at the end of the two years. Find the total interest paid by Kangara.
- 20. Income tax for all the income earned was charged at the rates shown.

Total Income p.a (K.£)	Rate in sh per K£
1 – 1980	2
1981 – 3960	3
3961 – 6440	5
6441 – 7920	7
7921 – 9900	9
Excess of 9900	10

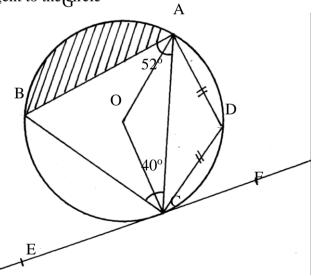
(a) Wanyonyi earned a salary of Kshs.10,500 per month. In addition he was given a house allowance of Kshs. 6500 per month. He got tax relief of Kshs. 300 per month.

Find; (i) His taxable income p.a

- (ii) Income tax he pays per month.
- (b) A part from income tax the following deductions are made per month. NHIF of Kshs.320, widow and pension scheme of 2% of his gross salary. Calculate his net monthly pay.

### **46.**Circles –chords and tangents

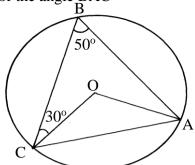
1. In the figure below angle BAC = $52^{\circ}$ , angle ACB =  $40^{\circ}$  and AD = DC. The radius of the circle is 7cm. EF is a tangent to the circle



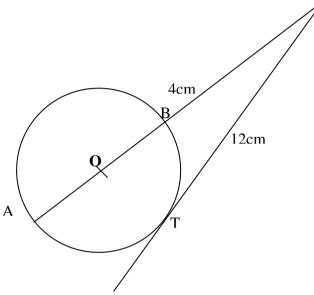
- (a) Find; giving reasons
  - (i) angle DCF
  - (ii) angle AOB (obtuse)
- (b) Calculate the area of the shaded segment AGB

2. In the figure below, O is the centre of the circle. Angle CBA =  $50^{\circ}$  and angle BCO =  $30^{\circ}$ . Find the size of the angle BAC B\_\_\_

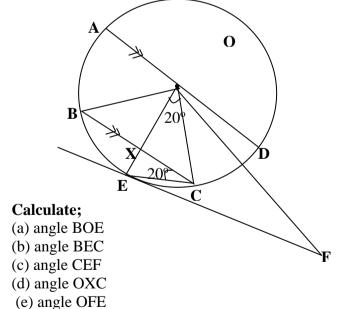




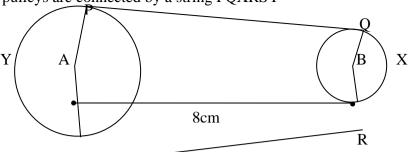
3. In the given figure, O is the centre of the circle and AOBP is a straight line. PT is a tangent to the circle. If PT = 12cm and BP = 4cm. find the radius of the circle



4. In the figure below AOD is a diameter of the circle cetre O. BC is a chord parallel to AD. FE is a tangent to the circle. OF bisects angle COD. Angle BCE = angle COE =  $20^{\circ}$  BC cuts OE at X

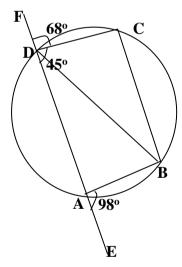


The figure below shows two pulleys of radii 6cm and 4cm with centres **A** and B respectively  $\mathbf{AB} = 8$ cm. The pulleys are connected by a string PQXRSY



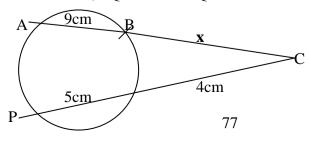
Calculate:

- (a) Length PQ
- (b) ∠PAS reflex
- (c) Length of arc PYS and QXR
- (d) The total length of the string PQXRSY
- 6. a) Two pipes **A** and **B** can fill a tank in 3hrs and 4 hrs respectively. Pipe **C** can empty the full tank in 6 hrs.
  - i) How long would it take pipes **A** and **B** to fill the tank if pipe **C** is closed?
  - ii) Starting with an empty tank, how long would it take to fill the tank with all pipes running?
  - b) The high quality Kencoffee is a mixture of pure Arabica coffee and pure Robusta coffee in the ratio 1:3 by mass. Pure Arabica coffee costs shs. 180 per kg and pure Robusta coffee costs sh 120 per kg. Calculate the percentage profit when the coffee is sold at sh 162 per kg.
- 7. In the figure below, ABCD is a cyclic quadrilateral and BD is a diagonal. EADF is a straight line,  $\angle CDF = 68^{\circ}$ ,  $\angle BDC = 45^{\circ}$  and  $\angle BAE = 98^{\circ}$ .



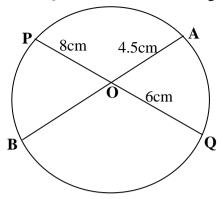
Calculate the size of:

- a)  $\angle$  ABD.
- b) ∠ CBD
- 8. The figure below shows a circle centre O. AB and PQ are chords intersecting externally at a point C. AB = 9cm, PQ = 5cm and QC = 4cm. Find the value of  $\mathbf{x}$

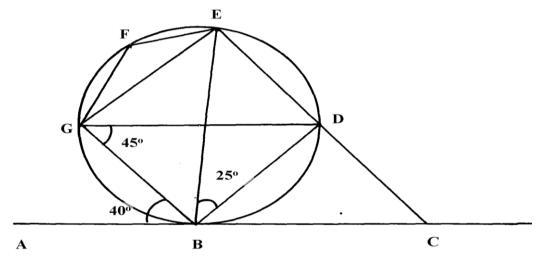




9. The chords AB and PQ intersects internally at O. Given that the length of OP=8cm, OA= 4.5cm and OQ=6cm. Calculate the length of OB

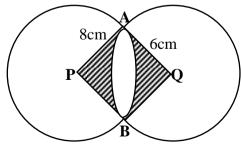


10. In the figure below ABC is a tangent to the circle at B. given that <ABG=40°, <BGD=45°, and <DBE=25° as shown below.



Find the sizes of the following angles giving reasons in each case:

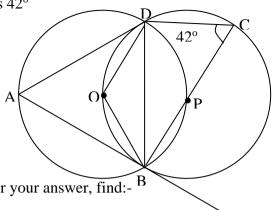
- a) ∠BDG
- b)∠DGE
- c)∠EFG
- d)∠CBD
- e)∠BCD
- 11. The figure below shows two intersecting circles radii 8 cm and 6 cm respectively. The common chord AB = 9cm ad  $\mathbf{P}$  and  $\mathbf{Q}$  are the centres as shown:



- (a) Calculate the size of angles:-
  - (i) ∠APB
  - (ii) ∠AQB

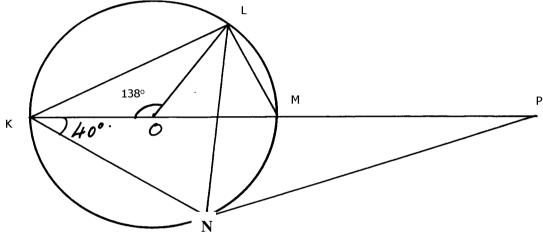


12. The figure O and P are centres of two intersecting circles. ABE is tangent to circle BCD at B angle BCD is 42°



- (a) Giving reasons for your answer, find:-
  - (i) CBD
  - (ii) DOB
  - (iii) DAB
  - (iv) CDA
- b) Show that  $\triangle ADB$  is isosceles

13.

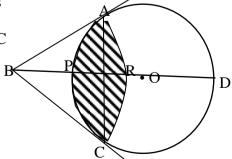


In the figure above K, M & P are points on a straight line. PN is a tangent of the circle centre O. Angle  $KOL = 130^{\circ}$  and angle  $MKN = 40^{\circ}$ . Find, giving reasons, the values of angles.

- (i) ∠MLN
- (ii) ∠OLN
- (iii) ∠LNP
- (iv) ∠MPN
- (v) ∠LMO
- 14. In the diagram below, O is the centre of the circle of radius 8cm. BA and BC are tangents to the circle at A and C respectively. PD is the diameter and AC is a chord of length 8cm. Angle ADC = 120°. ARC is an arc of the circle, Centre B and radius 4.6cm

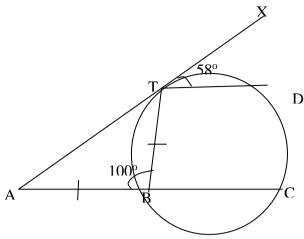
Calculate correct to 2 decimal places

- (a) Angle ABR
- (b) Area of sectors ABCR and OAPC
- (c) Area of the shaded part



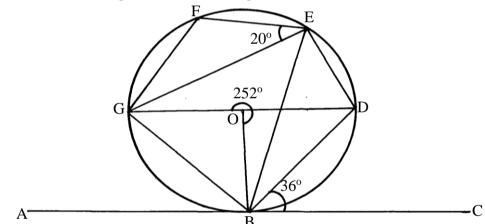
15. In the figure below, ATX is a tangent to the circle at point T, ABC is a straight line, angle  $ABT = 100^{\circ}$ , angle  $XTD = 58^{\circ}$  and line AB = line BT. C and D lie on the circle





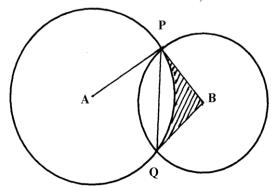
Find by giving reasons, the value of angle:

- (a) TDC
- (b) TCB
- (c) TCD
- (d) BTC
- (e) DTC
- 16. In the figure below, B, D, E, F and G are on the circumference of the circle centre O. A, B and C form a tangent to the circle at point B. GD is the diameter of the circle. Given that FG = DE, reflex angle GOB = 252°, angles DBC = 36° and FEG = 20°



Giving reasons in each case find the angles:

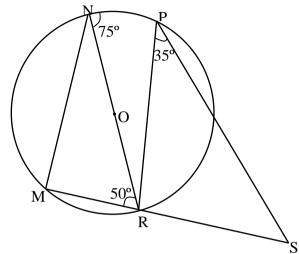
- a) GEB
- b) BED
- c) OBE
- d) BGE
- e) GFE
- 17. XYZ is a triangle in which x = 13.4cm, Z = 5cm and  $\angle XYZ = 57.7$ °. Find:
  - (i) Length of XZ
  - (ii) The circum radius of the triangle
- 18. In the figure shown below, the centers of the two circles are A and B. PQ is a common chord to the two circles. AP = 6cm, BP=4cm and PQ =5cm





Calculate the area of the shaded region (take  $\pi$  as 3.142)

In the figure below NR is a diameter of the circle centre O. Angle PNR =  $750^{\circ}$   $\angle$  NRM =  $50^{\circ}$ and  $\angle RPQ = 35^{\circ}$ . MRS and PQS are straight lines.



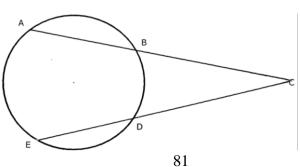
Giving reasons for every statement you write, find the following angles

- (a)  $\angle$  PQR
- (b) ∠QSR
- (c) Reflex ∠POR
- (d)  $\angle$  MQR
- (e) ∠ PON
- 20. In the diagram below, ATX is a tangent to the circle at point T, ABC is a straight line,  $\angle ABT = 100^{\circ}$ ,  $\angle XTD = 58^{\circ}$  and the line AB = BT

D

Find giving reasons the value of: (a) ∠TDC (b) ∠TCB (c) ∠TCD

- (d) ∠BTC
- (e) ∠DTC



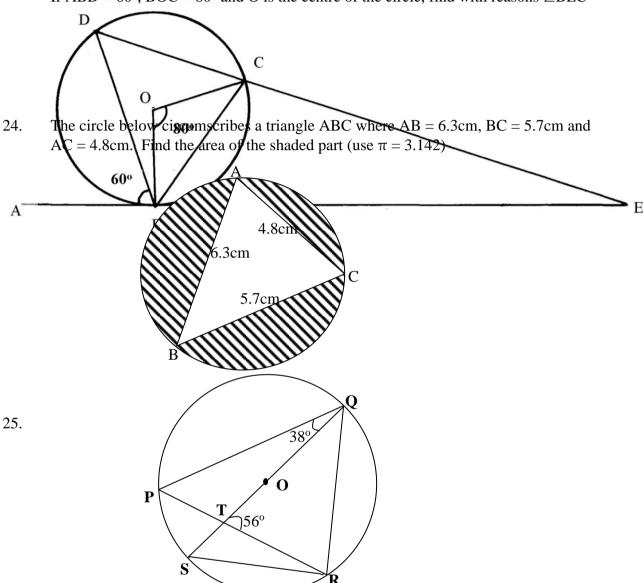
21.



In the figure above AB = 6 cm, BC = 4 cm DC = 5 cm. Find the length DE.

- 22. The eleventh term of an AP is four times the second term. If the sum of the first seven terms of the AP is 175, find the first term and the common difference
- 23. In the diagram below ABE is a tangent to a circle at B and DCE is a straight line.

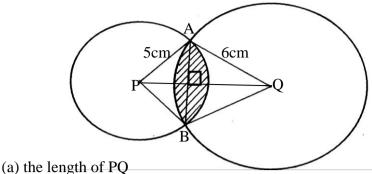
If ABD =  $60^{\circ}$ , BOC =  $80^{\circ}$  and O is the centre of the circle, find with reasons  $\angle$ BEC



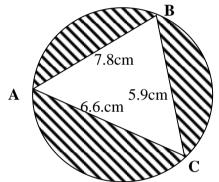
- (a) O is the centre of the circle and QOTS is a diameter. P, Q, R and S are points on the circumference of the circle. Angle PQS = 38° and angle QTR = 56°. Calculate the size of;
- (i) ∠PRQ
- (ii) ∠RSQ
- (b) Given that A varies directly as B and inversely as the cube of C and that; A = 12 when B = 3 and C = 2. Find B when A = 10 and C = 1.5
- (c) A quantity y is partly constant and partly varies inversely as the square of x. The quantity y=7 when x=10 and  $y=5\frac{1}{2}$  when x=20. Find the value of y when x=18

26. The figure below shows two intersecting circles with centres P and Q and radius 5cm and 6cm respectively. AB is a common chord of length 8cm. Calculate;

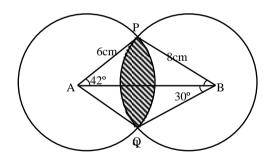




- (b) the size of;
  - (i) angle APB
  - (ii) angle AQB
- (c) the area of the shaded region
- 27. Triangle ABC is inscribed in the circle. AB= 7.8cm, AC 6.6cm and BC= 5.9cm. Find:



- (a) The radius of the circle correct to one decimal place
- (b) The area of the shaded region
- 28. The figure below shows two circles centres A and B and radii 6 cm and 8 cm respectively. The circles intersect at P and Q. Angle PAB =  $42^{\circ}$  and angle ABQ =  $30^{\circ}$ .



- (a) Find the size of  $\angle PAQ$  and PBQ.
- (b) Calculate, to one decimal place the area of:
  - (i) Sector APQ and PBQ.
- (ii) Triangle APQ and PBQ.
- (iii) The shaded area (take  $\pi$  22)
- 29. The minute hand of a clock is 6.5 cm long. Calculate the distance in cm moved by its tip between 10.30 am. and 10. 45 a.m. to 2 dpl.

# 47. Matrices

Teacher.



Given that A is  $\begin{pmatrix} 3 & 2 \\ 4 & -1 \end{pmatrix}$  and A  $\begin{pmatrix} 1 & 2 \\ 11 & 11 \end{pmatrix}$   $\begin{pmatrix} 4 & -3 \\ 11 & 11 \end{pmatrix}$ 

(3 mks)

Find the value of a and b in the expression:
$$\begin{pmatrix}
3 & 2 \\
4 & -1
\end{pmatrix}
\begin{pmatrix}
a \\
b
\end{pmatrix}
=
\begin{pmatrix}
12 \\
5
\end{pmatrix}$$

2. Solve for the unknowns given that the following is a singular matrix.

 $\begin{bmatrix}
1 & 2 \\
x & x-3
\end{bmatrix}$ 

- 3. Given that  $A = \begin{pmatrix} 1 & 5 \\ 3 & 7 \end{pmatrix}$  and  $B = \begin{pmatrix} 7 & 3 \\ -4 & -2 \end{pmatrix}$  and that C = AB, find  $C^{-1}$
- 4. B is a matrix  $\begin{pmatrix} 3 & 2 \\ 2 & 2 \end{pmatrix}$  and C is the matrix  $\begin{pmatrix} 9 & -3 \\ 2 & 1 \end{pmatrix}$

. If A is a 2 x 2 matrix and A x B = C. determine the matrix A.

- 5. An object of area 20 cm<sup>2</sup> undergoes a transformation given by the matrix  $\begin{pmatrix} -1 & -2 \\ 4 & 3 \end{pmatrix}$  followed by  $\begin{pmatrix} 2 & 3 \\ -1 & 2 \end{pmatrix}$  find the area of the final image.
- 6. Find the matrix B such that AB = I and  $A = \begin{bmatrix} 3 & 2 \\ -1 & 3 \end{bmatrix}$ . Hence find the point of intersection of the lines 3x + 2y = 10 and 3y 4 = x.
- 7. Given that  $\mathbf{P} = \begin{pmatrix} 2 & 3 \\ 1 & 2 \end{pmatrix}$  and  $\mathbf{Q} = \begin{pmatrix} 2 & -3 \\ -1 & 2 \end{pmatrix}$  find ; the matrix product PQ. Hence solve the simultaneous equations below:-2x 3y = 5 -x + 2y = -3
- 8. Solve for x and y in the following matrix equation using elimination method

 $\begin{pmatrix} \frac{1}{2} & -\frac{1}{4} \\ \frac{2}{5} & \frac{1}{6} \end{pmatrix} \qquad \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2 \\ 6 \end{pmatrix}$ 

- 9. A triangle XYZ, X(-1, -1), Y(-2, -4)Z(-6, -9) is reflected in the line X axis followed by a reflection in line X = Y. Find the image of the final image
- 10. Triangle ABC is the image of triangle PQR under a transformation  $\mathbf{M} = \begin{pmatrix} 2 & 4 \\ 0 & 2 \end{pmatrix}$  where P, Q, R map onto A, B, C respectively. Given the points P (5, -1) Q (6, -1) and R(4, -0.5) draw the triangle ABC on the grid provided.
  - b) Triangle ABC in (a) above is to be enlarged by scale factor 2 with centre at (11, -6) to map onto  $A^1B^1$  and  $C^1$ . Construct and label triangle  $A^1B^1$  and  $C^1$  on the same grid.
  - c) By construction, find the coordinates of the centre and the angle of rotation which can be used to rotate triangle  $A^IB^IC^I$  onto triangle  $A^{II}B^{II}C^{II}$  whose coordinates are (-3, -2), (-3, -6) and (-1, -2) respectively.



- Triangle ABC with an area of 15 cm<sup>2</sup> is mapped onto triangle A<sup>I</sup>B<sup>I</sup>C<sup>I</sup> using matrix  $M = \begin{pmatrix} 2 & -3 \\ 1 & 1 \end{pmatrix}$ . Find the area of triangle A<sup>I</sup>B<sup>I</sup>C<sup>I</sup>.
- 12. **T** is a transformation represented by the matrix  $\begin{bmatrix} 5x & 2 \\ -3 & x \end{bmatrix}$  under **T** a square whose area is  $10\text{cm}^2$  is mapped onto a square of area  $110\text{cm}^2$ . Find the possible values of **X**
- 13. Triangle A<sup>1</sup>B<sup>1</sup>C<sup>1</sup> is the image of  $\triangle$  ABC under a transformation represented by the matrix  $M = \begin{pmatrix} 3 & 2 \\ 9 & 5 \end{pmatrix}$

If the area of triangle A<sup>1</sup>B<sup>1</sup>C<sup>1</sup> is 54cm<sup>2</sup>. Determine the area of triangle ABC

14. Find the matrix B such that AB = I and  $A = \begin{bmatrix} 3 & 2 \\ -1 & 3 \end{bmatrix}$ . Hence find the point of intersection of the lines 3x + 2y = 10 and 3y - 4 = x.

#### 48. Formulae and variation

- 1. P varies as the square of R. R. varies as the square of T. When P = 18, R = 3 and T = 5. Express P in terms of T hence find P when T = 10.
- 2. Make r the subject of the formula.

$$v = \sqrt{\frac{r}{r+c}}$$

- 3. X varies as the cube of Y and inversely as square root of Z, X = 6 when Y = 3 and Z = 25.
  - (a) Find;
    - (i) An expression connecting X,Y,Z
    - (ii) X when Y = 7 and Z = 9
    - (iii) Y when X = 8 and Z = 16
  - b) If Y is increased by 20% and Z is decreased by 36%, find the percentage increase in X
- 4. Make **b** the subject of the formula;

$$K = \underline{a} \underline{b}$$
  
 $b - \underline{a}$ 

- 5. Find a quadratic equation whose roots are  $2.5 + \sqrt{3}$  and  $2.5 \sqrt{3}$ , expressing it in the form  $ax^2 + bx + c = 0$  Where a, b and c are integers
- 6. A quantity **Z** varies directly as the square of x and inversely as the square root of y. If **x** increases by 20% and **y** decreases by 36%, find the percentage change in **Z**
- 7. The fourth terms of a G.P is 48 and the seventh term is 384. Find the common ratio and hence calculate the sum of the first six terms
- 8. A quantity **P** varies directly as the square of **Q** and inversely as quantity **R**. If P = 2 when Q = 4 and R = 6, find **P** when Q = 8 and R = 4

9. **B** varies partly as the square of **M** and partly as the inverse of **N**. **B**, **M** and **N** are such that when M=2,  $N=\frac{1}{2}$ , B=96 while when M=3, N=2, B=46. Write an expression for B in terms of **M** and **N**.



10. Solve for **x** and **y**.

$$\frac{3x}{y-1} = 1$$

$$(2x + 2) : (y - 5) = 1 : 2$$

- $P = \left(\frac{x-1}{x+2}\right)$ 11. Make  $\mathbf{x}$  the subject of the formula..
- 12. Make **d** the subject of the formula given that:-

$$a^2 = \sqrt{\frac{1+d^2+b}{b^2}}$$

- **Z** varies jointly as the square of **x** and inversely as the square of **y**. When  $\mathbf{x} = 10$  and 13.  $\mathbf{v} = 4$  then  $\mathbf{z} = 15$ 
  - (a) Find z in terms of x and y
  - (b) Find the value of x when z = 8 and v = 12
- A quantity **R** partly varies as **n** and partly as the square root of **n**. When  $\mathbf{n} = 9$  **R** = 42 and 14. when  $\mathbf{n} = 25$   $\mathbf{R} = 100$ . Find  $\mathbf{R}$  when  $\mathbf{n} = 16$ .
- 15. Make **b** the subject of the formula.

$$a = \underbrace{\frac{bd}{b^2 + d}}$$

- 16. **P** varies party as **Q** and partly as the square root of **Q**. When  $\mathbf{Q} = 4$ ,  $\mathbf{P} = 22$  and when  $\mathbf{Q} = 9$ ,  $\mathbf{P} = 42$ . Find the value of  $\mathbf{P}$  when  $\mathbf{Q} = 25$ .
- 18.

Make 
$$\bf C$$
 the subject of the formula  $\bf b = \sqrt{k-aC}$  hence find the value of  $\bf C$  when  $\bf K=1$ ,  $\bf a=4$  and  $\bf b=2$ 

- 18. The velocity of water flowing through a pipe is inversely proportional to the square of the radius of the pipe. If the velocity of the water is 30cm/s when the radius of the pipe is 2cm. Find the velocity of water when the radius of the pipe is 4cm
- 19. Make x the subject of the formula

$$P = 3 \sqrt{\frac{xy}{z + x}}$$

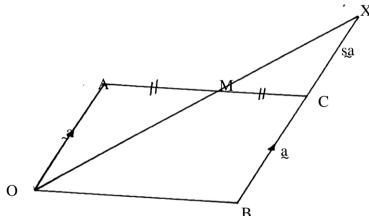
- 20. Three quantities x, y and z are such that x varies partly as y and partly as the inverse of the square of Z. When  $\mathbf{x} = 6$ ,  $\mathbf{y} = 3$  and z = 2. When z = 8, z = 5 and z = 1. Find the value of x when y = 10 and z = 8
- 21. The eleventh term of an AP is four times the second term. If the sum of the first seven terms of the AP is 175, find the first term and the common difference

5.

- The resistance of an electrical conductor is partly constant and partly varies as the temperature. When the temperature is 20°C, the resistance is 55 ohms. When the temperature is 28°C, the resistance is 58 ohms. Find the resistance when the temperature is 60°C
- 23. Expand  $1-\frac{1}{2}$  (2x) 1 up to the term in x<sup>3</sup>. Hence or otherwise evaluate (0.98) to 4 d.p.

### 49. Sequence and series

- 1. The area covered by Mau forest is 40,000 km<sup>2</sup> at present. If the human encroachment rate is estimated to be 2 % every 10 years. Calculate the area of the forest encroached in 30 years.
- 2. Three consecutive terms of geometric progression are  $3^{2x+1}$ ,  $9^x$  and 81 respectively. Calculate:
  - (a) The value of x
  - (b) Find the common ratio
  - (c) Calculate the sum of the first 10 terms of this series
  - (d) Given that the fifth and the seventh terms of this G.P forms the first two consecutive terms of arithmetic sequence, calculate the sum of the first 20 terms of this sequence
- 3. How many terms of the sequence -12 + -10 + -8 .....should be added to give a sum of 338?
- 4. An arithmetic progression whose first term is 2 and whose n<sup>th</sup> term is 32 has the sum of its n terms equal to 357. Find **n**



In the figure OACB is parallelogram in which M is the mid-point of AC and OM produced meets BC also produced at X.

Given OA = a and OB = b

- a) Express OC in terms of a and b
- b) Find the values of r and s such that OX = rOM and CX = sBC
- c) Hence determine the ratio BC:BX
- 6. For the series  $29 + 23 + \dots + (-91)$ , find;
  - (a) The number of terms in the above series
  - (b) The sum of the series
- 7. (a) Given that 5, a, b, and 7 are in arithmetical progression, find the value of a and b
  - (b) If 5, P, Q,  $^{135}/_{8}$  are in geometrical progression. Find the value of P and Q
  - (c) Prove that the sum of the first 12 terms of the first series in (a) is approximately equal to the sum of the first 6 terms of the second series (b) above
- 8. An aeroplane flew East for 640km then turned and flew on a bearing of 050°. After 2.5hrs flying at 324km/hr, it was necessary to fly to the original point because of technical hitch.

How much shorter is it going to cover flying straight to the starting point than retracing its former route?



- 9. A ball falls vertically from a height of 15m. Each time it bounces back to 50% of the height achieved on the previous bounce. Find the distance covered after 6 such bounces
- 10. Find the sum of the first 51 terms of the series: -22, -19, -16......
- 11. Olunga saves shs.100 on his son's first birthday. He saves shs.200 on the second birthday and Shs.400 on the third birthday and so on doubling the amount on every birthday. How much will he be saving on the boy's 10th birthday.
- 12. A self-help group intended to purchase a dry cleaning machine worth shs.720,000. The members were required to contribute equal amounts to pay for the machine. The group recruited 20 more members consequently, each member paid shs.3000 less that what he would have contributed.
  - (a) find the original number of members
  - (b) find the amount required from each member to contribute after the recruitment
- 13. Find the number of terms in the following sequence  $8, 4, 2, \frac{1}{2}, \dots, \frac{1}{512}$
- 14. An arithmetic progression has the first term a and the common difference d
  - a) Write down the third, ninth and twenty fifth terms of the progression in terms of  $\mathbf{a}$  and  $\mathbf{d}$
  - b) The arithmetic progression above is increasing and that the third, ninth and twenty fifth terms form the first three consecutive terms of a geometric progression. The sum of the seventh and twice the sixth terms of the arithmetic progression is 78.

Calculate:

- i) The first term and common difference of the arithmetic progression
- ii) The sum of the first nine terms of the arithmetic progression
- 15. The difference between the fourth and the seventh terms of an increasing arithmetic progression

#### 50. Vectors 2

In the figure alongside  $\overrightarrow{OA} = a$ ,  $\overrightarrow{OB} = b$ . T lies on AN such that AN: TN = 13:6. M lies on AB such that AM:  $\overrightarrow{MB}$ =1:3 and N lies on OB such that OB: BN = 7:-5.~

B (a) Express in terms of a and b in the simplest form (i)  $\overrightarrow{AN}$ (iii)  $\overrightarrow{AM}$ 

- (b) Show that O, T and M are collinear and state the ratio of OT: TM
- 2. A point (-3, 4) divides **AB** internally in the ratio 3:5. Find the coordinates of point **A** given that point **B** is (6, -5)
- 3. Given that O is the origin, OA = 3i + 2j 4k and OB = 6i + 11j + 2k. If **x** divides AB in the ratio1:2, find the modulus of OX to 2d.p
- 4. a) Expand  $(2 \frac{1}{5}x)^5$

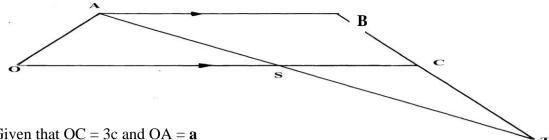




6.

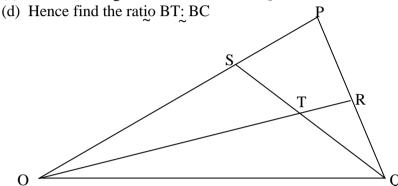
5. In the figure OABC is a trapezium in which 3 AB = 20C. S divides OC in the ratio 2:1 and AS produced meets BC produced at T





Given that OC = 3c and OA = a

- (a) Express AS and BC in terms of a and c
- (b) Given further that AT = hAS and BT = KBC where h and k are constants
  - (i) Express AT in two ways in terms a, c, h and k
- (c) The obtuse angle between the lines PQ



In the figure above, OPQ is a triangle in which  $OS = \frac{3}{4}$  OP and PR: RQ = 2 : 1. Lines OR and SQ meet at T.

- (a) Given that OP = P and OQ = q, express the following vectors in term of p and q ГП
  - (i) PQ
  - (ii) OR
  - (iii) SQ
- (b) You area further given that ST = m SQ and OT = n OR. Determine the values of m and n

## 51.Binominial expansion

- (a) Expand  $(1-3x)^{5}$ (b) use your expansion to estimate the value of  $(0.997)^{5}$  Correct to 4 d.p. 1.
- (i) Expand  $\left(5 + \frac{X}{2}\right)$  upto the term in  $X^3$ 2. correct to one decimal place (ii) Use your expansion to estimate the value of
- (a) Expand (3 + 2x)<sup>6</sup> up to the fourth term 3.
  - (b) Use your expansion to estimate:  $(3\sqrt{3})^6$
- Two dice are thrown once and their sum noted. Find the probability that the sum is odd 4.
- Find the length PR in a triangle PQR having  $PQ = \frac{5}{2}$  cm, QR = 8.4 cm angle  $QPR = 35^{\circ}$ 5. and angle PRQ =  $75^{\circ}$  leaving your answer correct to decimal places
- (a) Use binomial expansion to evaluate  $(2+3)^5$  up to the fifth term 6.
  - (b) By expressing 9.5 in the form (2 + 3), use the expansion in (a) above to calculate  $(9.5)^5$



- 7. Use the expansion of  $(x 0.2)^5$  to find the exact value of  $9.8^5$
- 8. Solve for  $\mathbf{x}$  in the equation;

$$\log (x + 24) = 2 \log 3 + \log (9 - 2x).$$

- 9. Expand  $1 + \frac{x}{12}$  in ascending powers of **x** upto the fourth term.

  Use the four terms to evaluate  $\begin{bmatrix} 5/4 \end{bmatrix}$  to 4 decimal places.
- 10. (a) Expand and simplify the binominal expression  $(1 + \frac{1}{2}x)^8$ 
  - (b) Use the expansion up to the fourth term to evaluate  $(1.05)^8$  to 2 decimal places
- 11. Expand  $(3 + x)^4$  in ascending powers of x. Use the first three terms of the expansion to evaluate  $(3.02)^4$ , correct to 3 decimal places

#### 52. Probability

- 1. A bag contains 3 black balls and 6 white ones. If two balls are drawn from the bag one at a time, find;
  - (a) The probability of drawing a black ball and a white ball.
    - (i) Without replacement.
    - (ii) With replacement.
  - (b) Drawing two white balls.
    - (i) Without replacement.
    - (ii) With replacement.
- 2. A cupboard has 7 white cups and 5brown cups all identical in size and shape.

There is a blackout in the town and Mrs. Bett has to select three cups one after another without replacing the previous ones.

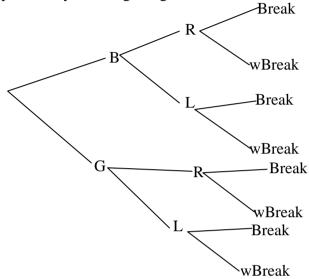
- (a) Draw a tree diagram for the information
- (b) Calculate the probability that she chooses;
  - (i) Two white cups and one brown cup
  - (ii) Two brown cups and one white cup
  - (iii) At least one white cup
  - (iv) three cups of the same colour
- 3. A two digit number is formed from the first four prime numbers.
  - a) Draw the table to show the possible outcomes, if each number can be used only once.
  - b) Calculate the probability that a number chosen from the digit numbers is an even number
- 4. The probability that a boy goes to school by bus is  $\frac{1}{3}$  and by matatu is  $\frac{1}{2}$ . If he uses a bus, the probability that he is late to school is  $\frac{1}{5}$  and if he uses a matatu, the probability of being late is  $\frac{3}{10}$ . If he uses other means of transport, the probability of being late is  $\frac{1}{20}$ 
  - (a) Draw a probability tree diagram to represent this information
  - (b) What is the probability that he will be late for school
  - (c) What is the probability that he be late for school if he does not use a matatu
  - (d) What is the probability that he is not late for school
- 5. One day during inspection in a certain secondary school, it was discovered that there was a probability of <sup>2</sup>/<sub>5</sub> that a students had shaggy hair, if a student had shaggy hair, there was a probability of <sup>1</sup>/<sub>2</sub> that he had torn uniform. But if he had properly combed hair, there was a probability of <sup>1</sup>/<sub>4</sub> that he had a torn uniform. If a student had torn uniform there was a probability of <sup>4</sup>/<sub>5</sub> that he had unpolished shoes. Otherwise there was a probability of <sup>3</sup>/<sub>5</sub> that he had polished shoes.
  - a) Represent this information in a probability tree diagram
  - b) Find the probability that:-

- i) a student had all the three faults
- ii) a students had exactly two faults
- iii) a students had no faults at all

A shop is stocked with plates which are from two suppliers **A** and **B**. They are brought in the ratio of 3:5 respectively. 10% of plates from **A** are defective and 6% of plates from **B** are de

In a science class  $^2$ /3 of the class are boys and the rest are girls. 80% of the boys and 90% of the girls are right handed and the rest are left handed. The probability that a right handed student will break a test-tube in any session is  $^1$ /10 and the corresponding for the left handed student is  $^3$ /10, their probability being independent of the student sex .

a) Complete the probability tree diagram given below



- b) Using the tree diagram, find the probability that:
- i) A student chosen from the class is left handed
- ii) A test-tube is broken by a left handed student
- iii) A test-tube is broken by a right handed student
- iv) A test-tube is not broken in any session
- 8. Students who performed well in an examination are to be given an outing. A student has to throw two dice. If he gets a sum greater than 8, he gets a two-days outing, otherwise he gets a one day outing.
  - (a) Find the probability that a student gets a two-day outing
  - (b) A student who qualifies for a two-day outing throws a die and a coin to decide whether he gets pocket money for the two days or for only one day. If he gets a head and a multiple of 3 he gets pocket money for two days. Find the probability that he is given a two-day outing but given pocket money for only one day
  - (c) If a student gets a one-day outing, he throws a die to decide if he gets pocket money or not. If he gets a number greater than 4 he gets the pocket money. Find the probability that:-
    - (i) A student gets pocket money for two days
    - (ii) A student gets pocket money
- 9. A bag contains 6 red beads and 4 white ones. Two beads are selected from the bag at random without replacement.
  - (a) Draw a tree diagram to represent the above information.
  - (b) Calculate the probability that:
    - (i) Both beads are white.
    - (ii) Both beads are of the same colour.
    - (iii) At least a red bead is picked.
    - (iv) The two beads are of different colours.



- 10. A bag contains blue, green and red pens of the same type in the ratio 8:2:5respectively. A pen is picked at random without replacement and its colour noted.
  - a) Determine the probability that the first pen picked is;
    - (i) blue
    - (ii) either green or red.
  - b) Using a tree diagram, determine the probability that;
    - (i) the first two pens picked are both green.
    - (ii) Only one of the first two pens picked is red.
  - c) (i) Draw the probability space for the possible outcomes when a coin is tossed and a die thrown simultaneously
    - (ii) Determine the probability of getting a head and an even number.
- 11. A box contains five red balls and four black balls all identical. Three balls are drawn without replacement from the box at random;
  - (a) Draw a tree diagram to show the situation
  - (b) use the tree diagram to find the probability that;
    - (i) the balls picked are of the same colour
    - (ii) more red balls were picked
    - (iii) at least a black ball was picked
    - (iv) atmost 1 red ball was picked
- 12. A bag contains 10balls of which 3 are red, 5 are white and 2 are green. Another bag contains 12balls of which 4 are red, 3 are white and 5 are green. A bag is chosen at random and then a ball chosen at random from the bag. Find the probability that the ball so chosen is red
- 13. In a certain science class  $^2/_3$  of the class are boys and the rest girls.  $^4/_5$  of the boys and  $^9/_{10}$  of the girls are right handed, and the rest are left handed. The probability that a right handed student will break a test-tube in any session is  $^1/_{10}$  and the corresponding probability for a left handed student is  $^3/_{10}$ , these probabilities being independent of the student's sex.
  - (a) Represent this information on a tree diagram
  - (b) Using the diagram above;
    - (i) determine the probability that a student chosen at random form the class is left handed
    - (ii) determine the probability that a student chosen at random from the class is right handed and will break a test tube in any session
  - (c) determine the probability that a test tube is broken in any session
- 14. A box contains 5 red biro pens, 4 black biro pens and 6 green biro pens. If three pens are picked once at random, find the probability that:
  - (i) all the biro pens are red
  - (ii) the biro pens are of the same colour
  - (iii) the biro pens are one of each colour
  - (iv) none of the biro pens is red
- 15. The probability that Chebet goes to bed on time  $\frac{3}{4}$ . If she goes to bed on time, the probability that she wakes up on time is  $\frac{5}{6}$ , otherwise her probability of waking up on time is  $\frac{1}{3}$ .
  - (a) (i) Find the probability of Chebet getting to bed on time and waking up on time by use of diagram
    - (ii) Waking up late
  - (b) If Chebet wakes up late, her probability of getting to class on time is  $\frac{1}{5}$  otherwise, her probability of getting to class on time is  $\frac{3}{5}$ .
    - (i) Find the probability of Chebet getting to bed on time and gets to class late
    - (ii) Getting to bed late and get to class on time



#### 53. Compound proportions, mixtures and rates of work

- Three business partners Georgina, Gilbert and Akumu decided to buy a plot worth shs.510,000. They contributed shs.30000; as a deposit in the ratio 2:3:5 respectively. They paid the balance in two months by contributing equal amounts. After one year, they sold the plot for a profit of 20% and invested the initial capital in another business. The profit was shared in the ratio 1:2:3; respectively. Find how much each partner
  - (a) contributed towards the deposit
  - (b) paid to clear the balance
  - (c) received as a profit
- 2. Twelve men take 20days to complete a piece of work. How long would 16 men take to do the same piece of work?
- 3. Mr. Kitur bought grades of tea; Grade A costs shs.109 per kg and a kg of Grade B costs shs.81.50. In what ratio must he mix the two grades in order to make a profit of 20% by selling the mixture at Kshs.112.80per kg?
- 4 Mogutu and Onacha working together can do a piece of work in 6days. Mogutu working alone takes 5days longer than Onacha. How many days does it take Onacha to do the work alone?
- Given the curve  $y = 2x^3 + \frac{1}{2}x^2 4x + 1$ , find the equation of the normal to the curve at  $(1, -\frac{1}{2})$
- A and **B** are connected by the equation  $\mathbf{B} = \mathbf{K}\mathbf{A} + \mathbf{M}$  where **K** and **M** are constants. The table below shows the values of **A** and corresponding values of **B**

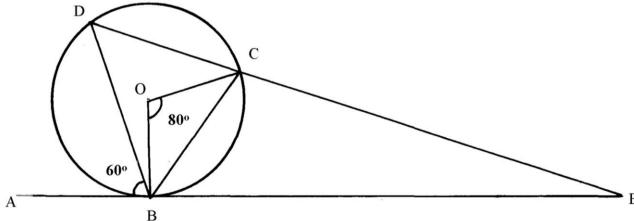
A	1.5	3.0	4.5	6.0	7.5
В	8	11	14	17	20

- a) Draw a suitable straight line on the grid provided
- b) State the values of K and M, hence express B in terms of A
- The latitude and longitude of two stations **P** and **Q** are (47°N, 25°W) and (47°N, 70°W) respectively. Calculate the distance in nautical miles between **P** and **Q** along the latitude 47°N
- A coffee blender mixes 6 parts of types **A** with 4 parts of type **B**. If type A costs Kshs. 72 and type **B** costs him Ksh.66 per kg respectively at what price should he sell the mixture in order to make a profit of 5%. Give your answer to the nearest ten cent.
- 9 (a) (i) Paint **A** costs shs.150 per litre while **B** costs shs.160 per litre. In what proportion must **A** be mixed with **B** to produce a mixture costing shs.156 per litre
  - (ii) What must be the selling price of the mixture if a profit of 12% is to be realized?
  - (b) A cylindrical water tank can be filled to a depth of 2.1m by a pipe  $\mathbf{P}$  in 2 hours. Pipe  $\mathbf{Q}$  takes 7 hours to fill the tank to the same level. Pipe  $\mathbf{R}$  can empty this amount of water in 6hours. Initially, the tank is empty. Pipes  $\mathbf{P}$  and  $\mathbf{Q}$  are turned on at 8.45a.m and pipe  $\mathbf{R}$  at 9.45a.m. Find the depth of water in the tank at 11.45a.m
- Two grades of tea leaves one costing sh.420 per kilogram and the other costing sh. 470 per kilogram are to be mixed in order to produce a blend worth sh.455 per kilogram. In what proportion should they be mixed?
- 11. The internal radius of a pipe is 0.35m. Water flows through the pipe at the rate of 45cm per second. Calculate the amount of water that passes through the pipe in 2 ½ hours in litres

- In 2000 the total cost of manufacturing an item was ksh1250 and this was divided among the costs of material, labour and transport in the ratio of 8:14:13. In 2003 the cost of material was doubled, labour cost increased by 30% and transport costs increased by 20%
  - a) Calculate the cost of manufacturing this item in 2003
  - b) In 2004 the cost of manufacturing the same item was ksh1981 as a result of increase in labour costs only. Find the percentage increase in labour costs of 2004
- 13. Brand **A** tea costing Kshs.80 per kg is mixed with Brand **B** tea costing Kshs.100 per kg such that the mixture is sold at Kshs.114 making a profit of 20%. Find the ratio of **A:B**
- 14. In what proportion must teas of Kshs.76 and Kshs.84 per kg be mixed to produce a tea costing Kshs.81 per kg
- 15. Onyango bought 3 brands of tea **P**, **Q** and **R**. the cost price of the three brands were shs.25, shs.30 and shs.45 per kilogram respectively. He mixed the three brands in the ratio 5:2:1 respectively After selling the mixture, he made a profit of 20%
  - (a) How much, profit did he make per kilogram of the mixture?
  - (b) After one year, the cost price each brand was increased by 12%.
  - (i) For how much did he sell one kilogram of the mixture to maintain 20% profit. Give your answers to the nearest 5cts.
  - (ii) What would have been his percentage profit if he sold one kilogram of the mixture at shs.40.25?
- 16. A mixture contains two powders X and Y with masses in the ratio 3:11. If the mixtures Cost Shs.6.70 per kg and powder x costs Shs.5.60 per kg. Find the cost of 1kg of powder Y

## **54.** Graphical Methods

- 1. The equation of a circle is given by  $x^2 + 4x + y^2 5 = 0$ . Find the centre of the circle and its radius.
- The equation of a circle is  $x^2 + y^2 + 6x 10y 2 = 0$ . Determine the co-ordinates of the centre of the circle and state its radius
- 3. In the diagram below ABE is a tangent to a circle at B and DCE is a straight line. If ABD =  $60^{\circ}$ , BOC =  $80^{\circ}$  and O is the centre of the circle, find with reasons  $\angle$ BEC



4. Obtain the centre and the radius of the circle represented by the equation:  $x^2 + y^2 - 10y + 16 = 0$ 



Complete the table below, for the function  $y = x^3 + 6x^2 + 8x$ 

X	-5	-4	-3	-2	-1	0	1
$\mathbf{x}^3$	-125		-27	-8		0	1
$6x^2$		96	54		6	0	6
8x	-40		-24			0	8
у			3	0		0	15

- (a) Draw a graph of the function  $y = x^3 + 6x^2 + 8x$  for  $-5 \le x \le 1$  and use the graph to estimate the roots of the equation  $x^3 + 6x^2 + 8x = 0$
- (b) Find which values of **x** satisfy the inequality  $x^3 + 6x^2 + 8x 1 > 0$
- 6. Sketch the curve of the function  $y = x^3 3x + 2$  showing clearly minimum and maximum points and the y intercept.
- 7. Show that  $4y^2 + 4x^2 = 12x 12y + 7$  is the equation of a circle, hence find the co-ordinates of the centre and the radius
- 8. Two variables R and P are connected by a function  $R = KP^n$  where K and n are constants.

The table below shows data involving the two variables

P	3	3.5	4	4.5	5
R	36	49	64	81	100

- (a) Express  $\mathbf{R} = \mathbf{K}\mathbf{P}^{\mathbf{n}}$  in a linear form
- (b) Draw a line graph to represent the information above
- (c) Find the values of constants **K** and **n**
- (d) Write down the law connecting **R** and **P**
- (e) Find the value of P when R = 900
- 9. A circle of radius 3cm has the centre at (-2, 3). Find the equation of the circle in the form of  $x^2 + y^2 + Px + qy + c = 0$
- 10. In an experiment, the values of two quantities V and T were observed and the results recorded as shown below.

V	0	2	4	6	8	10
T	0.49	0.30	0.24	0.20	0.16	0.137

It is known that **T** and **V** are related by a law of the form  $T = \underbrace{a}_{b+V}$ 

where  $\mathbf{a}$  and  $\mathbf{b}$  are constants.

- a) Draw the graph of  $\underline{I}$  against V  $\underline{T}$
- b) Use your graph to find;
  - i) The values of **a** and **b**.
  - ii) V when T = 0.38
- iii) **T** when V = 4.5
- 11. Find the equation of the tangent to the curve  $y = 2x^3 + x^2 + 3x 1$  at the point (1, -5) expressing you answer in the form y = mx + c
- 12. Given that :-  $243 = (81)^{-1} x (\frac{1}{27})^{x}$  determine the value of x

13. Show that  $3x^2 + 3y^2 + 6x - 12y - 12 = 0$  is an equation of a circle hence state the radius and centre of the circle



14. (a) Fill in the table below for the function  $y = -6 + x + 4x^2 + x^3$  for  $-4 \le x \le 2$ 

Х	-4	-3	-2	-1	0	1	2
-6	-6	-6	-6	-6	-6	-6	-6
х	-4	-3	-2	-1	0	1	2
$4x^2$			16			4	
$x^3$							
у							

- (b) Using the grid provided draw the graph for  $\mathbf{v} = -\mathbf{6} + x + 4x^2 + x^3$  for  $-4 \le x \le 2$
- (c) (i) Use the graph to solve the equations:-
  - (i)  $x^3 + 4x^2 + x 4 = 0$
  - (ii)  $-6 + x + 4x^2 + x^3 = 0$
  - (iii)  $-2 + 4x^2 + x^3 = 0$
- 15. The table below shows the results obtained from an experiment to determine the relationship between the length of a given side of a plane figure and its perimeter

Length of side t (cm)	1	2	3	4	5
Perimeter P(cm)	6.28	12.57	18.86	21.14	31.43

- (a) On the grid provided, draw a graph of perimeter **P**, against t
- (b) Using your graph determine;
  - (i) the perimeter of a similar figure of side 2.5cm
  - (ii) the length of a similar figure whose perimeter is 9.43cm
  - (iii) the law connecting perimeter p and the length t
- (c) If the law is of the form  $P = 2k\iota + c$  where k and c are constants, find the value of k
- In an experiment with tungsten filament lamp, the reading below of voltage (V) current (I), power (P) and resistance (R)were obtained. It was established that **P** was related to **R** by a law  $P = a R^n 0.6$ . Where **a** and **n** are constants.

V	1.30	2.00	2.80	4.40	5.70
I	1.50	1.80	2.10	2.50	2.90
P	0.73	2.05	3.28	7.44	10.62
R	0.89	1.13	1.33	1.78	1.99

Plot a suitable line graph and hence use it to determine the value of **a** and **n** 

- 17. Find the gradient of a line joining the centre of a circle whose equation is  $x^2 + y^2 6x = 3 4y$  and a point P(6,7) outside the circle..
- 18. a) Complete the table below for the function  $y = -x^3 + 2x^2 4x + 2$ .

X	-3	-2	-1	0	1	2	3	4
-x <sup>3</sup>	27	8		0		-8		
$2x^2$	18	8	2	0				
-4x		8		0				-16
2	2	2	2	2	2	2	2	2
у		26		2		-6		-46

- b) On the grid provided below draw the graph of  $-x^3 + 2x^2 4x + 2$  for  $-3 \le x \le 4$ .
- c) Use the graph to solve the equation  $-x^3 + 2x^2 4x + 2 = 0$ .
- d) By drawing a suitable line on the graph solve the equation.  $-x^3 + 2x^2 5x + 3 = 0$ .



- 19. Determine the turning point of the curve  $y = 4x^3 12x + 1$ . State whether the turning point is a maximum or a minimum point.
- 20. (a) Complete the table below for the equation of the curve given by  $y = 2x^3 3x^2 + 1$

									<i>J</i> •		
X	-2	-1.5	-1	-0.5	0	0.5	1	1.5	2	2.5	3
$2x^3$	-16		-2		0		2		16		
$-3x^2$	-12			0.75	0	-0.75					-27
1	1				1						
y	-27	-12.5			1						13.5

- (b) Use the table to draw the graph of the function  $v = 2x^3 3x^2 + 1$
- c) Use your graph to find the values of x for :-
- (i) y > 0
- (ii) The roots of the equation  $2x^3 3x^2 + 1 = 0$
- (iii)  $2x^3 3x^2 = 9$
- 21. Find the radius and the centre of a circle whose equation is:

$$2x^2 + 2y^2 - 6x + 10y + 9 = 0$$

## **55.Matrices and Transformations**

- 1. Given triangle ABC with vertices A (-6, 5), B(-4, 1) and C(3, 2) and that A(-6, 5) is mapped onto A<sup>1</sup>(-6, -4) by a shear with y-axis in variant. On the grid provided below;
  - (i) draw triangle ABC
  - (ii) draw triangle A<sup>1</sup>B<sup>1</sup>C<sup>1</sup>, the image of triangle ABC, under the shear
  - (iii) determine the matrix representing the shear
  - (b) Triangle  $A^1B^1C^1$  is mapped onto  $A^{11}B^{11}C^{11}$  by a transformation defined by the matrix  $\begin{bmatrix} -1 & 0 \\ \frac{3}{2} & -1 \end{bmatrix}$ 
    - (ii) Describe fully a single transformation that maps A<sup>11</sup> B<sup>11</sup>C<sup>11</sup>
- 2. (a) Under a certain rotation A( 2,0) is mapped onto  $A^1(-4,2)$  and B(0,5) is mapped onto  $B^1(-9,0)$ 
  - (i) On the grid provided plot the lines AB and A<sup>1</sup>B<sup>1</sup> on the same axes
  - (ii) Hence determine by construction the co-ordinates of the centre and angle of rotation
  - (b) Under a quarter positive turn about the origin O, A<sup>1</sup> is mapped onto A<sup>11</sup> and B<sup>1</sup> is mapped onto B<sup>11</sup>. Determine the co-ordinates of A<sup>11</sup> and B<sup>11</sup>
  - (c) Describe fully a single transformation which would map A to  $A^{11}$  and B to  $B^{11}$
- 3. A transformation **T** is represented by the matrix  $\begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$  and transformation  $\begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$  by the

matrix. Given that a rectangle has co-ordinates at A (1,2) B(6,2), C(6,4) and D (1,4) and that under **T** the image of ABCD is A<sub>1</sub>B<sub>1</sub>C<sub>1</sub>D and under **U** the image of A<sub>1</sub>B<sub>1</sub>C<sub>1</sub>D is A<sub>2</sub>B<sub>2</sub>C<sub>2</sub>D<sub>2</sub>:

- (a) Find the co-ordinates of  $A_1B_1C_1D_1$  and  $A_2B_2C_2D_2$
- (b) On the grid provided, plot ABCD,  $A_1B_1C_1D_1$  and  $A_2B_2C_2D_2$
- (c) Describe the transformation represented by:-
  - (i) U
  - (ii) UT
- (d) If  $A_2B_2C_2D_2$  were to be transformed by a transformation represented by the matrix to map onto  $A_3B_3C_3D_3$ . What would be the area of  $A_3B_3C_3D_3$
- 4. The vertices of a quadrilateral are A(2,2) B(8,2), C (8,6) and D(6,4) under a rotation the images of vertices A and D are A(0,8) and D1(-2, 12).
  - (a) On the grid provided and using the same axes draw the quadrilateral ABCD and the

points A<sup>1</sup> and D<sup>1</sup>

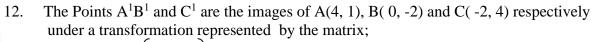
- (b) Determine the centre and angle of rotation
- (c)Locate the points  $B^1$  and  $C^1$  under the rotation and complete the quadrilateral



- A translation maps the point P(5, -3) onto  $P^{1}(2, -5)$ 
  - (a) Determine the translation vector T
  - (b) A Point R<sup>1</sup> is the image of R(-2, -3) under the same translation in (a) above, find the magnitude of P<sup>1</sup>R<sup>1</sup>
- Triangle ABC has vertices at A(0, -1), B(4, 3) and C(2,2).
  - (a) Find the coordinates of image triangle  $A^1B^1C^1$  of triangle ABC under translation vector
  - (b) Given that triangle A<sup>11</sup>B<sup>11</sup>C<sup>11</sup> is the image of triangle A<sup>1</sup>B<sup>1</sup>C<sup>1</sup> under an enlargement scale factor 3, centre O(0,0), find the coordinates of A<sup>11</sup>, B<sup>11</sup> and C<sup>11</sup>
  - (c) If the area of triangle A<sup>1</sup>B<sup>1</sup>C<sup>1</sup> is 24 cm<sup>2</sup>, calculate the area of triangle A<sup>11</sup>B<sup>11</sup>C<sup>11</sup>
  - (d) Find the matrix that maps triangle A<sup>11</sup>B<sup>11</sup>C<sup>11</sup> onto triangle ABC
- 7. a) The triangle ABC where A (2,-1) B (1, 2) and C (4, 4) is reflected in the line X = 4 to give triangle  $A_1B_1C_1$ . Draw the two triangles on the graph provided and state the co-ordinates of  $A_1B_1C_1$ 
  - b) Draw the triangle A<sub>2</sub> (5,6), B<sub>2</sub> (2,7) and C<sub>2</sub> (0,4). Given that triangle A<sub>2</sub>B<sub>2</sub>C<sub>2</sub> is the image of triangle A<sub>1</sub>B<sub>1</sub>C<sub>1</sub> under rotation, determine the centre and angle of this rotation
  - c) Show the image of triangle A<sub>2</sub>B<sub>2</sub>C<sub>2</sub>, under an enlargement centre (0, 6) scale factor -1
- 8. (a) Find the co-ordinates for the image of point P(6, -2) under the transformation defined by:  $x^{1} = x 3y$   $y^{1} = 2x$ 
  - (b) (i) A quadrilateral ABCD has vertices A(4, -3), B(2, -3), C(4, -1) and D(5, -4). On the grid provided, draw the quadrilateral ABCD
    - (ii)  $A^1B^1C^1D^1$  is the image of ABCD under a rotation through  $+90^\circ$  about the origin. On the same axes, draw  $A^1B^1C^1D^1$ under the transformation
  - (c)  $A^2B^2C^2D^2$  is the image of under  $A^1B^1C^1D^1$  under another transformation by the matrix (i) Determine the co-ordinates of  $A^2B^2C^2D^2$  and plot it on the same axes
  - (ii) Describe the transformation that maps  $A^1B^1C^1D^1$  onto  $A^2B^2C^2D^2$
  - (d) Find a single matrix of transformation that would map  $A^2B^2C^2D^2$  onto ABCD
- 9. (a) Triangle **XYZ** has vertices **X**(2, -1) **Y**(4, -1) and **Z** (4,2). Triangle XYZ maps onto triangle  $X^1Y^1Z^1$  under transformation  $T_1 \neq 1$  . Draw triangles XYZ and its image  $X^1Y^1Z^1$  on the grid provided
  - (b) Another triangle  $X^{11}Y^{11}Z^{11}$  is the image of  $X^1Y^1Z^1$  after transformation  $T_2$  = Draw triangle  $X^{11}Y^{11}Z^{11}$  on the same set of axes
  - (c) Find the single transformation matrix T that maps triangle XYZ on to the final image  $X^{11}Y^{11}Z^{11}$
  - (d) Given that the area of triangle XYZ is  $15 \text{cm}^2$ , find the area of the triangle  $X^{11}Y^{11}Z^{11}$
- 10. The quadrilateral A (2,1), B (4,1), C (4,4) and D (2,4) is mapped onto A'B' C'D' by a matrix  $M_1$  such that  $A^1$  (8,7),  $B^1$  (14,7),  $C^1$  (14,16) and  $D^1$  (8,16).
  - a) Draw both ABCD and A<sup>1</sup>B<sup>1</sup> C<sup>1</sup>D<sup>1</sup> on the same plane
  - b) Find the matrix of transformation that mapped ABCD onto A'B' C'D' and describe it fully
  - c)  $A^1B^1$   $C^1D^1$  underwent another matrix transformation at N which is a translation that gave the image  $A^{11}$   $B^{11}$   $C^{11}$   $D^{11}$ , Where  $A^{11}$  (7,9),  $B^{11}$  (13,9),  $C^{11}$  (13,18) and  $D^{11}$  (7,18). The transformation N is a translation . Find the translation
  - d) Draw A<sup>11</sup> B<sup>11</sup> C<sup>11</sup> D<sup>11</sup> on the same axes where ABCD and A<sup>1</sup>B<sup>1</sup> C<sup>1</sup>D<sup>1</sup> were drawn
- 11. a) On the grid provided. Plot the points A(2, -1) B (0, -3) C(2, -4) and D (4, -2) and join them to

form a quadrilateral ABCD. What is the name of this quadrilateral?

- b) The points A<sup>1</sup> (1, 2) B<sup>1</sup> (3, 0) C<sup>1</sup> (4, 2) and D<sup>1</sup> (2, 4) are the images of ABC and D under certain transformation T<sub>1</sub>. On the same grid draw quadrilateral A<sup>1</sup>B<sup>1</sup>C<sup>1</sup>D<sup>1</sup> and describe transformation T<sub>1</sub> fully.
  - c) The points  $A^{11}(-2, -4)$   $B^{11}(-6, 0)$   $C^{11}(-8, -4)$  and  $D^{11}(-4, -8)$  are the images of  $A^1B^1C^1D^1$  under transformation  $T_2$ . On the same grid draw quadrilateral  $A^{11}B^{11}C^{11}D^{11}$  and describe the transformation  $T_2$  fully.
  - d) On the same grid draw quadrilateral A<sup>111</sup> B<sup>111</sup> C<sup>111</sup> D<sup>111</sup>, the image of A<sup>11</sup> B<sup>11</sup> C<sup>11</sup> D<sup>11</sup> under a reflection in the x-axis. State the co-ordinates of A<sup>111</sup> B<sup>111</sup> C<sup>111</sup> D<sup>111</sup>.





$$\mathbf{M} = \begin{pmatrix} -1 & 1 \\ 2 & -3 \end{pmatrix}$$

- (a) Write down the coordinates of A<sup>1</sup> B<sup>1</sup> and C<sup>1</sup>
- (b) A<sup>11</sup> B<sup>11</sup> and C<sup>11</sup> are the images of A<sup>1</sup> B<sup>1</sup> and C<sup>1</sup> under another transformation whose Matrix is:

Naturalis:  

$$N = \begin{pmatrix} 2 & -1 \\ 1 & 2 \end{pmatrix}$$
Write down the coordinates of A<sup>11</sup> B<sup>11</sup> and C<sup>11</sup>

- (c) Transformation **M** followed by **N** can be represented by a single transformation **P**. Determine the matrix for **P**
- (d) A matrix **P** is given by  $\begin{bmatrix} 8 & 7 \\ 4 & 5 \end{bmatrix}$ Find P<sup>-1</sup>
- 13. Triangle  $A^1B^1C^1$  is the image of triangle ABC under a transformation represented by matrix  $T = \begin{bmatrix} 1 & 3 \\ 2 & 2 \end{bmatrix}$  If the area of triangle  $A^1B^1C^1$  is 25.6cm<sup>2</sup>, find the area of the object
- 14. A point P(2, -4) is mapped into  $P^1(4, 0)$  under a translation. Determine the image of point Q(-1, 2) under the same translation
- 15. The points A (2, 6), B (1, 1), C (2, 3) and D (4,0) are the vertices of quadrilateral ABCD.

  (a) On graph paper plot the points A, B, C, and D and join them to form quadrilateral ABCD.
  - (b) The points A, B, C and D are the images of A<sup>1</sup>, B<sup>1</sup>, C<sup>1</sup> and D<sup>1</sup> respectively under an enlargement centre the origin and scale factor -2. On the same grid draw the image quadrilateral A<sup>1</sup> B<sup>1</sup> C<sup>1</sup> D<sup>1</sup>.
  - (c) The points  $A^{11}B^{11}C^{11}$  and  $D^{11}$  are the images of ABCD respectively under reflection in the x axis. On the same grid, locate the pints  $A^{11}B^{11}C^{11}$  and  $D^{11}$  and draw the second image quadrilateral  $A^{11}B^{11}C^{11}D^{11}$ .
  - (d) Quadrilateral A<sup>111</sup> B<sup>111</sup> C<sup>111</sup> D<sup>111</sup> is the image of ABCD under a certain transformation T. Describe transformation T fully.

16. T is a transformation represented by the matrix  $\frac{10 \text{ cm}^2}{10 \text{ cm}^2}$ . Under T, a square of area  $\frac{10 \text{ cm}^2}{10 \text{ cm}^2}$ . Find the values of x

#### 56. Statistics II

1. The table below shows the masses to the nearest kg of a number of people.

The table belov	w shows u	ic masses to	the hearest i	kg of a flui	noci oi peo	pic.		
Mass (kg)	50 - 54	55 – 59	60 - 64	65 - 69	70 - 74	75 - 79	80 - 84	
Frequency	19	23	40	28	17	9	4	ĺ

- a)Using an assumed mean of 67.0, calculate to one decimal place the mean mass.
- (b) Calculate to one decimal place the standard deviation of the distribution.
- 2. Use only a ruler and pair of compasses in this question;

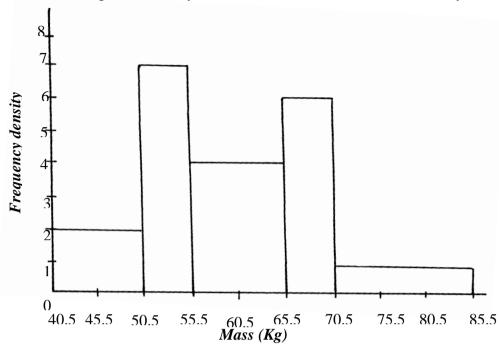
3.

- (a) construct triangle ABC in which AB = 7cm, BC = 6cm and AC = 5cm
- (b) On the same diagram construct the circumcircle of triangle ABC and measure its radius



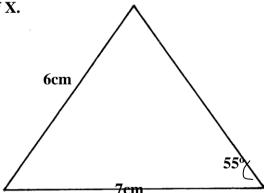
(c) Construct the tangent to the circle at C and the internal bisector of angle BAC. If these lines meet at D, measure the length of AD

Below is a histogram drawn by a student of Got Osimbo Girls Secondary School.



- a) Develop a frequency distribution table from the histogram above.
- b) Use the frequency distribution table above to calculate;
  - i) The inter-quartile range.
  - ii) The sixth decile.
- 4. ABC is a triangle drawn to scale. A point **x** moves inside the triangle such that
  - i)  $AX \le 4$  cm
  - ii) BX > CX
  - iii) Angle BCX  $\leq$  Angle XCA.

Show the locus of X.



5. The following able shows the distribution of marks of 80 students

Marks	1-10	11-20	21-30	31-40	41-50	51-60	61-70	71-80	81-90	91-100
Frequency	1	6	10	20	15	5	14	5	3	1

- (a) Calculate the mean mark
- (b) Calculate the semi-interquartile range





Marks	5-9	10-14	15-19	20-24	25-29	30-34	35-39
No. of students	2	13	31	23	14	X	1

- a) Find X
- b) State the modal class
- (c) Using a working mean of 22, calculate the; i) Mean mark
  - ii) Standard deviation
- (a) Using a ruler and a pair of compasses only construct triangle POR in which PO = 5cm,  $PR = 4cm \text{ and } \angle PQR = 30^{\circ}$ 
  - (b) Measure; (i) RQ
    - (ii) ∠POR
  - (c) Construct a circle, centre O such that the circle passes through vertices P, Q, and R
  - (d) Calculate the area of the circle
- 8. The ages of 100 people who attended a wedding were recorded in the distribution table below

Age	0-19	20-39	40-59	60-79	80-99
Frequency	7	21	38	27	7

- a) Draw the cumulative frequency
- b) From the curve determine: i) Median
  - ii) Inter quartile range
  - iii) 7<sup>th</sup> Decile
  - iv) 60<sup>th</sup> Percentile
- 9. The marks obtained by 10 students in a maths test were:-

25, 24, 22, 23, x, 26, 21, 23, 22 and 27

The sum of the squares of the marks,  $\Sigma x^2 = 5154$ 

- (a) Calculate the:
- (i) value of x
- (ii) Standard deviation
- (b) If each mark is increased by 3, write down the:-
  - (i) New mean
  - (ii) New standard deviation
- 10. 40 form four students sat for a mathematics test and their marks were distributed as follows:-

Marks	1 – 10	11- 20	21- 30	31 – 40	41 – 50	51 – 60	61 – 70	71 – 80	81 – 90	91 - 100
No. of										
students	1	3	4	7	12	9	2	1	0	1

- a) Using 45.6 as the working mean, calculate;
  - i) The actual mean.
  - ii) The standard deviation.
- b) When ranked from first to last, what mark was scored by the 30<sup>th</sup> student? (Give your answer correct to 3 s.f.)
- 11. The table below shows the distribution of marks scored by pupils in a maths test at Nyabisawa Girls.

Marks	11 - 20	21 - 30	31 - 40	41 - 50	51 - 60	61 - 70	71 - 80	81 - 90
Frequency	2	5	6	10	14	11	9	3

- a)Using an Assumed mean 45.5, calculate the mean score.
- b) Calculate the median mark.
- c) Calculate the standard deviation.
- d) State the modal class.

2. The table below shows the marks scored in a mathematics test by a form four class;

Marks	20-29	30-39	40-49	50-59	60-69	70-79	80-89
No. of students	4	26	72	53	25	9	11

- (a) Using an assumed mean of 54.5, calculate:-
  - (i) The mean
  - (ii) The standard deviation
- (b) Calculate the inter quartile range

#### 57. Loci

- 1. (a) Using a ruler, a pair of compasses only construct triangle XYZ such that XY = 6cm, YZ = 8cm and  $\angle XYZ = 75^{\circ}$ 
  - (b) Measure line XZ and ∠XZY
  - (c) Draw a circle that passes through X, Y and Z
  - (d) A point M moves such that it is always equidistant from Y and Z. construct the locus of M and define the locus
- 2. (a) (i) Construct a triangle ABC in which AB=6cm, BC = 7cm and angle ABC =  $75^{\circ}$

#### Measure:-

- (i) Length of AC
- (ii) Angle ACB
- (b) Locus of P is such that BP = PC. Construct P
- (c) Construct the locus of Q such that Q is on one side of BC, opposite A and angle  $BQC = 30^{\circ}$
- (d) (i) Locus of P and locus of Q meet at X. Mark x
  - (ii) Construct locus R in which angle BRC 120°
  - (iii) Show the locus S inside triangle ABC such that  $XS \ge SR$
- 3. *Use a ruler and compasses only for all constructions in this question.* 
  - a) i) Construct a triangle ABC in which AB=8cm, and BC=7.5cm and ∠ABC=112½°
    - ii) Measure the length of AC
  - b) By shading the unwanted regions show the locus of P within the triangle ABC such that
    - i)  $AP \leq BP$
    - ii) AP > 3cm

Mark the required region as P

- c) Construct a normal from C to meet AB produced at D
- d) Locate the locus of  $\mathbf{R}$  in the same diagram such that the area of triangle ARB is  $\frac{3}{4}$  the area of the triangle ABC.
- 4. On a line AB which is 10 cm long and on the same side of the line, use a ruler and a pair of compasses only to construct the following.
  - a) Triangle ABC whose area is  $20 \text{ cm}^2$  and angle ACB =  $90^\circ$
  - b) (i) The locus of a point P such that angle APB =  $45^{\circ}$ .
    - (ii) Locate the position of P such that triangle APB has a maximum area and calculate this area.



- A garden in the shape of a polygon with vertices A, B, C, D and E. AB = 2.5m, AE = 10m, ED = 5.2M and DC = 6.9m. The bearing of **B** from **A** is 030° and **A** is due to east of **E** while **D** is due north of E, angle EDC = 110°,
  - a) Using a scale of 1cm to represent 1m construct an accurate plan of the garden
  - b) A foundation is to be placed near to CD than CB and no more than 6m from A,
    - i) Construct the locus of points equidistant from CB and CD.
    - ii) Construct the locus of points 6m from A
  - c) i) shade and label **R**, the region within which the foundation could be placed in the garden
    - ii) Construct the locus of points in the garden 3.4m from AE.
    - iii) Is it possible for the foundation to be 3.4m from AE and in the region?
- 6. a) Using a ruler and compasses **only** construct triangle PQR in which QR= 5cm, PR = 7cm and angle PRQ = 135°
  - b) Determine < POR
  - c) At P drop a perpendicular to meet QR produced at T
  - d) Measure PT
  - e) Locate a point **A** on **TP** produced such that the area of triangle AQR is equal to oneand -a - half times the area of triangle PQR
  - f) Complete triangle AQR and measure angle AQR
- 7. Use ruler and a pair of compasses only in this question.
  - (a) Construct triangle ABC in which AB = 7 cm, BC = 8 cm and  $\angle$ ABC =  $60^{\circ}$ .
  - (b) Measure (i) side AC (ii) ∠ ACB
  - (c) Construct a circle passing through the three points A, B and C. Measure the radius of the circle.
  - (d) Construct  $\triangle$  PBC such that P is on the same side of BC as point A and  $\angle$  PCB =  $\frac{1}{2}$   $\angle$  ACB,  $\angle$  BPC =  $\angle$  BAC measure  $\angle$  PBC.
- 8. Without using a set square or a protractor:-
  - (a) Construct triangle **ABC** in which **BC** is 6.7cm, angle **ABC** is 60° and ∠**BAC** is 90°.
  - (b) Mark point **D** on line **BA** produced such that line AD = 3.5 cm
  - (c) Construct:-
    - (i) A circle that touches lines **AC** and **AD**
    - (ii) A tangent to this circle parallel to line AD

Use a pair of compasses and ruler only in this question;

- (a) Draw acute angled triangle **ABC** in which angle **CAB** =  $37\frac{1}{2}$ °, **AB** = 8cm and **CB** = 5.4cm. Measure the length of side **AC** (**hint**  $37\frac{1}{2}$ ° =  $\frac{1}{2}$ **x** 75°)
- (b) On the triangle **ABC** below:
  - (i) On the same side of AC as B, draw the locus of a point X so that angle Ax C =  $52\frac{1}{2}$ °
  - (ii) Also draw the locus of another point  $\mathbf{Y}$ , which is 6.8cm away from  $\mathbf{AC}$  and on the same side as  $\mathbf{X}$
- (c) Show by shading the region **P** outside the triangle such that angle  $APC \ge 52 \frac{1}{2}$ ° and **P** is not less than 6.8cm away from **AC**





### 58. Trigometric ratios 3

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- 1. The table below gives some values of  $y = \sin 2x$  and  $y = 2 \cos x$  is the range given.
  - (a) Complete

Xº	-225	-180	-135	-90	-45	0	45	90	135	180	225
$y - \sin 2x^3$	-1.0		1.0			0			-1.0		1.0
$y = 2\cos x^3$	-1.4		-1.4			2.0			-1.4		-1.4

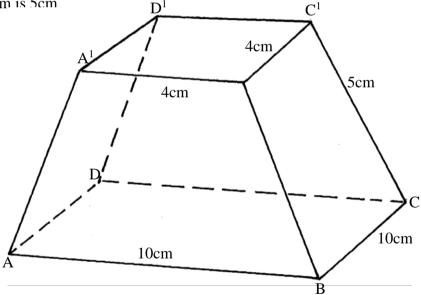
- (b) On the same axes, draw the graphs of  $y = \sin 2x$  and  $y = 2 \cos x$ .
- (c) Use your graph to find in values of x for which  $\sin 2x 2 \cos x = 0$ .
- (d) From your graph
  - (i) Find the highest point of graph  $y = \sin 2x$ .
  - (ii) The lowest point of graph  $y = 2 \cos x$ .
- 2. (a) Copy and complete the table below for  $y = 2\sin(x + 15)^{\circ}$  and  $y = \cos(2x 30)^{\circ}$  for  $0^{\circ} \le x \le 360^{\circ}$

X	0	30	60	90	120	150	180	210	240	270	300
$y = 2\sin(x+15)$											
$y = \cos(2x-30)$											

(b) On the same axis draw the graphs:

$$y = 2\sin(x + 15)$$
 and  $y = \cos(2x - 30)$  for  $0^{\circ} \le x \le 360^{\circ}$ 

- (c) Use your graph to:
  - (i) State the amplitudes of the functions  $y = 2\sin(x + 15)$  and  $y = \cos(2x 30)$
  - (ii) Solve the equation  $2\sin(x+15) \cos(2x-30) = 0$
- 3. The diagram below shows a frustum of a square based pyramid. The base ABCD is a square of side 10cm. The top A<sup>1</sup>B<sup>1</sup>C<sup>1</sup>D<sup>1</sup> is a square of side 4cm and each of the slant edges of the frustum is 5cm



Determine the:

- i) Altitude of the frustrum
- ii) Angle between AC1 and the base ABCD
- iii) Calculate the volume of the frustrum
- 4 (a) Compete the table below:

$$y = 3\sin(2x + 15)^{\circ}$$

X	-180	-150	-120	-90	-60	-30	0	30	60	90	120

y	0.8		-0.8		0.8	21	



- (b) Use the table to draw the curve  $y = 3\sin(2x + 15)$  for the values  $-180^{\circ} \le \theta \le 120^{\circ}$
- (c) Use the graph to find:
  - (i) The amplitude
  - (ii) The period
  - (iii) The solution to the equation:-

Sin 
$$(2x + 15)^{\circ} = \frac{1}{3}$$

- 5. Make **q** the subject of the formula in  $\frac{A}{B} = \sqrt{\frac{P + 3q}{q 3p}}$
- 6. a) Complete the table below for the functions  $y = \cos(2x + 45)^{\circ}$  and  $y = -\sin(x + 30^{\circ})$  for  $-180^{\circ} \le x \le 180^{\circ}$ .

	-180	-150	-120	-90	-60	-30	0	30	60	90	120	150	180
$y = Cos(2x + 45^{\circ})$	0.71		-	-0.71			0.71		1			0.97	
			0.97						0.97				
$y = -\sin(x + 30^{\circ})$	0.5	0.87			0.5			-0.87		-0.87			0.5

- b) On the same axis, draw the graphs of  $y = \cos(2x + 45)^{\circ}$  and  $y = -\sin(x + 30)^{\circ}$
- c) Use the graphs drawn in (b) above to solve the equation.

$$\cos (2x + 45)^{\circ} + \sin(x + 30)^{\circ} = 0$$

- 7. Without using tables or calculators evaluate  $\frac{\sin 60^{\circ} \cos 60^{\circ}}{\tan 30^{\circ} \sin 45^{\circ}}$  leaving your answer in surd form.
- 8. (a) Complete the table below for the functions  $y = 3 \sin x$  and  $y = 2 \cos x$

								J					
X	0	30	60	90	120	150	180	210	240	270	300	330	360
3sin	X		2.6	3			0	-1.5	-2.6	-3		-1.5	
2cos	SX	1.7	1.0			-1.7	-2	-1.0			1.0	1.7	2

- (b) Using a scale of 2cm to represent 1 unit on the y- axis and 1cm to present  $30^{\circ}$  on the x-axis, draw the graphs of  $y = 3\sin x$  and  $y = 2\cos x$  on the same axes on the grid provided
- (c) From your graphs:
  - (i) State the amplitude of  $y = 3\sin x$
  - (ii) Find the values of x for which  $3\sin x 2\cos x = 0$
  - (iii) Find the range of values of x for which  $3\sin x \ge 2\cos x$
- 9. (a) Fill in the following table of the given function:-

x	0	90	180	270	360	450	540	630	720	810
sin ½x	0			0.71					0	
$3\sin(1/2x+60)$					-2.6					2.6

- (b) On the grid provided draw the graph of the function  $y = \sin \frac{1}{2}x$  and  $y = 3\sin \left(\frac{1}{2}x + 60\right)$  on the same set of axes
- (c) What transformation would map the function  $\mathbf{v} = \sin \frac{1}{2}x$  onto  $\mathbf{v} = 3 \sin \left(\frac{1}{2}x + 60\right)$
- (d) (i) State the period and amplitude of function :  $y = 3 \sin(1/2x + 60)$ 
  - (ii) Use your graph to solve the equation:  $3\sin(1/2x + 60) \sin(1/2x = 0)$
- 10. a) Complete the table below giving your answer to 2 decimal places

Xº	0°	30°	60°	90°	120°	150°	180°
2sinx°	0	1		2			
1 – Cos x°			0.50	1			2



b) On the grid provided, using the same axis and scale draw the graphs of :-

 $y = 2\sin x^{o}$ , and  $y = 1-\cos x$  for

 $0^{\circ} \le x \le 180^{\circ}$ , take the scale of

2cm for 30° on the x-axis

2cm for 1 unit on the y-axis

- c) use the graph in (b)above too solve the equation  $2\sin x + \cos x^{\circ} = 1$  and determine the range of values of for which  $2\sin x^{\circ} = 1-\cos x^{\circ}$
- 11. Solve the equation  $2 \sin (x + 30) = 1$  for  $0 \le x \le 360$ .
- 12. (a) Complete the table below, giving your values correct to 1 decimal place

	0	10°	20°	30°	40°	50°	60°	70°	80°	90°	100°	11	120	130	140	150	160	170°	180°
X	0											$\mathbf{0_o}$	0	0	0	0	0		
10	0	-	3.4	5.0		7.7		9.4	9.8	10	9.8	9.4		7.7		5.0	3.4		0
sin																			
X																			

- (b) Draw a graph of  $y = 10 \sin x$  for values of x from  $0^{\circ}$  to  $180^{\circ}$ . Take the scale 2cm represents  $20^{\circ}$  on the x-axis and 1cm represents 1 unit on the y axis
- (c) By drawing a suitable straight line on the same axis, solve the equation:  $500 \sin x = -x + 250$
- 12. Complete the table below for the functions  $y = \cos x$  and  $y = 2\cos(x 300)$  for  $\theta \le x \le 3600$

х	0°	30°	60°	90°	120°	150°	180°	210°	240°	270°	300°	330°	360°
$\cos x$	1	0.87	0.5		-0.5	-0.87	-1.0		0.5	0		0.87	1
$2\cos(x +$	1.73		0	-1.0		-2.0	-	-1.0		1	1.73	2.00	1.73
30°)							1.73						

- (a) On the same axis, draw the graphs of y cos x and y  $2\cos(x 30)$  for  $0 < x < 360^\circ$ .
- (b) (i) State the amplitude of the graph  $y = \cos x^{o}$ .
  - (ii) State the period of the graph  $y = 2 \cos(x + 30^{\circ})$ .
- c) Use your graph to solve

$$Cos x = 2cos(x+30^{\circ})$$

13. Solve the equation  $\sin(2\theta + 10) = -0.5$ 

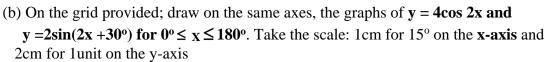
for 
$$0 \le \theta \le 2\pi^c$$

14. Solve the equation

$$4 \sin 2x = 5 - 4 \cos^2 x$$
 for  $0^{\circ} \le x \le 360^{\circ}$ 

15. (a) Complete the table given below by filling in the blank spaces

X	0	15	30	45	60	75	90	105	120	135	150	165	870
4cos 2x	4.00		2.00	0	-2.00	-3.46	-4.00	-3.46	-2.00	0	2.00		4.00
$2 \sin (2x + 30^{\circ})$	1.00	1.73	2.00	1.73		0	-1.00	-1.73	-2.00	-1.73		0	1.00

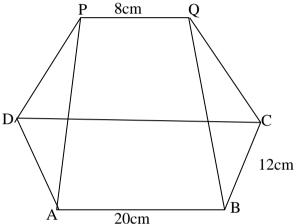




- (c) From your graph:-
  - (i) State the amplitude of  $\mathbf{v} = \cos 2\mathbf{x}$
  - (ii) Find the period of  $y = 2\sin(2x + 30^{\circ})$
- (d) Use your graph to solve:  $4\cos 2x - 2\sin (2x + 30) = 0$

## 59. Three dimensional geometry

1. The figure below represents a plan of a roof with a rectangular base ABCD. AB = 20cm and BC=12cm. the ridge PQ = 8cm is centrally placed. The faces ADP and BCQ are equilateral triangles. **N** is the mid-point of BC

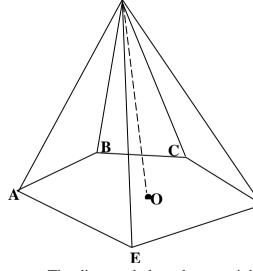


Calculate:

(a) QN

2.

- (b) The altitude of **P** above the base
- (c) The angle between the planes ABQP and ABCD
- (d) (i) Locus P and locus Q meet at X. Mark X
  - (ii) Construct locus R in which angle BRC is 120°
  - (iii) Show that locus inside triangle ABC such that  $XS \ge R$



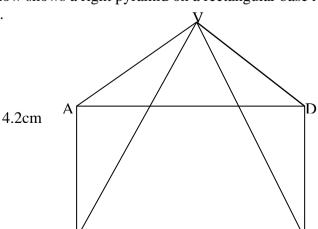
The diagram alongside shows a right pyramid whose base is a regular pentagon of side 10cm.VA=B=VC=VD=VE=18.2cm and O is the centre of the pyramid. Calculate;

- (a) height of the pyramid
- (b) area of the pentagon
- (c) angle between the face VAB and the base of the pyramid
- (d) The pyramid is a container filled with orange juice.

Calculate the amount of juice in it.

(e) find the surface area of the face VCD

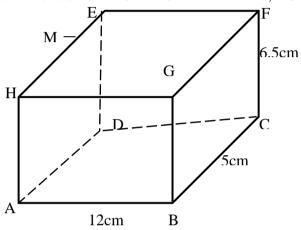
3. The diagram below shows a right pyramid on a rectangular base ABCD measuring 7.5cm by 4.2cm.





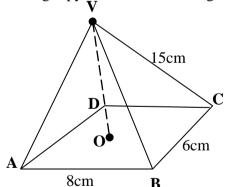
If the volume of the pyramid is 52.5cm<sup>3</sup>, **find**:-

- (i) The height of the pyramid
- (ii) The length of a slanting edge correct to 1decimal place
- (iii) The angle between AV and CV
- (iv) The obtuse angle between the edges AB and VD
- 4. The figure below is cuboid ABCDEFGH. AB = 12cm, BC=5cm, CF = 6.5cm



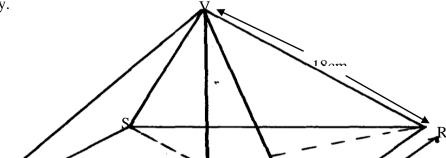
#### Calculate:

- (a) the length BD
- (b) the angle AF makes with the base ABCD
- (c) the angle DHGC makes with the base ABCD
- (d) **M** is the mid-point of HE. Calculate the length of line MC and the angle line MC makes with the base ABCD
- 5. The figure below is a right pyramid with a rectangular base ABCD and vertex V.



O is the centre of the base and M is a point on OV such that  $OM = \frac{1}{3} OV$ , AB = 8 cm, BC = 6 cm and VA = VB = VC = 15 cm. Find;

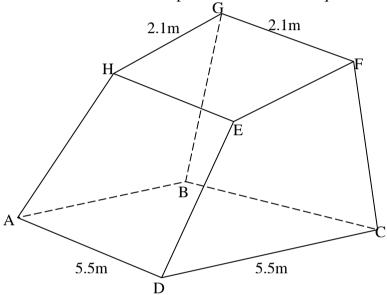
- i) The height OV of the pyramid.
- ii) The angle between the plane BMC and base ABCD.
- 6. The figure below represents a right pyramid with vertex V and a rectangular base PQRS, VP=VQ=VR=VS=18cm, PQ=16cm and QR=12cm. M and O are the midpoints of QR and PR respectively.





Find:

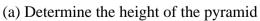
- a) the length of the projection of the line VP on the plane PQRS
- b)the size of the angle between line VP and the plane PQRS
- c) the size of the angle between plane VQR and PQRS
- 7. Mayoni Municipal Council wishes to construct a monument on the grounds. The monument is designed to be in the shape of a frustrum of a right pyramid. The base of the frustrum is a square of side 5.5meters while the top of the frustrum is a square of side 2.1cm



If the perpendicular distance between faces ABCD and EFGH is 7cm;

- (a) find the surface area of the monument frustrum
- (b) The monument is to be painted on all surface excluding the base. Paint is sold in 4 litre tins each costing Kshs.640/=. It is estimated that an area 10m² is painted by ½ litre of paint, find the cost of painting the monument.
- 8. The figure below is a pyramid of a rectangular base PQRS of length 12cm and width 9cm.

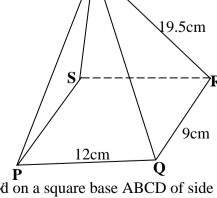
The slanting edge has a length of 19.5cm



(b) The angle PO makes with base PQRS

D

- (c) The angle POS makes with QOR
- (d) The volume of the pyramid
- 9. The diagram below shows a right solid pyramid on a square base ABCD of side 12cm and slanting height of 24cm



 $\mathbf{C}$ 



#### Calculate:

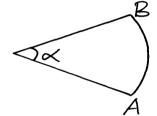
- a) To two decimal place the height (VO) of the pyramid
- b) the volume of the pyramid
- c) the total surface area of the pyramid
- 10. The base of a pyramid consists of a regular pentagon **ABCDE**, **4.5cm** a side. The vertex of the pyramid is  $\mathbf{V}$  and  $\mathbf{VA} = \mathbf{VB} = \mathbf{VC} = \mathbf{VD} = \mathbf{VE} = \mathbf{6.4cm}$ .
  - (a) Sketch the general view of the pyramid
  - (b) Calculate:
    - (i) The angle between **VA** and the base
    - (ii) The angle between face **VCD** and the base
- 11. The positions o two towns A and B on earths surface are (60°N, 139°E) and (60°N, 41°W) respectively
  - a) Find the difference in longitude between A and B
  - b) Given that the radius of the earth is 6370km, calculate the distance between A and B in KM
  - c) Another town C is 420km East of town B and on the same latitude A and B find the longitude of town C

## 60. Longitudes and latitudes

- 1. The latitude and longitude of two stations **P** and **Q** are (47°N, 25°W) and (47°N, 70°W) respectively. Calculate the distance in nautical miles between **P** and **Q** along the latitude 47°N
- 2. A pane leaves an airport **P** (10°S, 60°E) and flies due north at 800km/hr. By taking radius of the earth to be 6370-km and 1 nautical mile to be 1.853km,
  - (a) Find its position after 2hrs
  - (b) The plane turns and flies at the same speed due West to reach **Q** longitude 12°W. Find the distance it has traveled due in West nautical miles
  - (c) Find the time it has taken
  - (d) If the local time at **P** was 1300hrs when it reached **Q**. Find the local time at **Q** when it landed at **Q**
- 3. Bot juice company has two types of machines, A and B, for juice production
  - Type A machine can produce 800 litres per day while type B machine produces 1600 litres per day. Type A machine needs 4 operators and type B machine needs 7 operators
  - At least 8000 litres must be produced daily and the total number of operators should not exceed
  - 41. There should be 2 or more machines of each type. Let x be the number of machines of type A and y the number of machines for type B,
  - a) Form all inequalities in x and y to represent the above information
  - b) On the grid provided below, draw the inequalities and shade the wanted regions
  - c) Use the grid in (b) to determine the least number of operators required for the maximum possible production

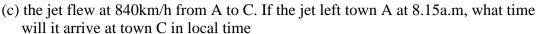
- 4. Points **R** and **S** are two points on the surface on a latitude 48°S. The two points lie on longitudes 30°W and 150°E respectively. By taking the earth's radius to be 6370km, calculate.
  - (a) The distance from  $\bf R$  to  $\bf S$  along a parallel of latitude.
  - (b) An aeroplane flies at an average speed of 2 80km/h from R to S along a great circle through the South Pole. Calculate the total time taken.
  - (c) The local time of R when the local time of R is 2.15m.
  - (d)Another point Q is 600Nm North of R .Find the location of Q
  - A jet flies from 34°N, 12°E to (34°E, 24°E) in 1 ½ hrs. Find its average speed in knots  $\bf P$  and  $\bf Q$  are two points on a geographical globe of diameter 50 cm. They both lie on a parallel latitude 50° North.  $\bf P$  has longitude 90° West and  $\bf Q$  has longitude 90° East. A string  $\bf A\bf B$  has one end at point  $\bf P$  and another at point  $\bf Q$  when it is stretched over the North pole. Taking  $\pi = 3.142$ ;
    - (i) Calculate the length of the string.
    - (ii) If instead the string is laid along the parallel of latitude 50°N with **A** at point **P**, calculate the longitude of point **B**
    - (iii) State the position of **B** if the string is stretched along a great circle of **P** towards the South pole if point **A** is static at **P**.
- 7. Two points **A**(70°, 15°E) and **B** lie on the same circle of latitude on the earths surface. Given that the shortest distance between the two points along the circle of latitude is 2133.6km. Giving coordinates to the nearest degree, find the location of **B**.

(Take  $\pi = \underline{22}$  and radius of earth = 6380km)



- 8. The position of two towns **A** and **B** on the earth's surface are (36°N, 49°E) and (36°N, 131°W) respectively (Earth's radius =6370km and  $\pi = ^{22}/_{7}$ ):-
  - (a) Find the longitudinal difference between the two towns
  - (b) Calculate the distance between the towns:-
    - (i) Along a circle of latitude (in km)
    - (ii) Along the great circle in km and nautical miles
  - (c) Another town C, is 840km due East to town B. Locate the position of town C
- 9. **P, Q** and **R** are points on the surface of the earth such that **P** (60°N, 20°W), **Q** (60°S, 20°W) and **R**(60°N, 80°E) find:
  - a) The shortest distance between **P** and **Q** on the surface of the earth in kilometres and nautical miles(**nm**)
  - b) The length of latitude 60°N and hence the length of the minor arc **PR** in kilometres
  - c) The distance from **P** to the North Pole
- 10. A jet flies from town **X** (50°S, 20°E) directly to **Y**(50°S, 28°W) and then due South for 1200m to **Z** 
  - (a) (i) Find the latitude of **Z** 
    - (ii) Calculate the distance XY along a parallel of latitude 50°S in km
  - (b) (i) Given that the average speed of the jet is 400 knots, calculate the time taken to reach **Z** from **X** to the nearest 0.1hour
    - (ii) Find the time of arrival at **Z** given that the plane left **X** at 7.40a.m. Take  $\pi = {}^{22}/_{7}$  and radius of the earth to be 6370km
- 11. A jet on a rescue mission left town A(35°S, 15°E) to town B(45°N, 15°E) and then to town C(45°N, 45°W). If 10 subtends 60nm and the radius of the earth is 6370km. Find; (a) the distance in nautical miles from A to C via B correct to 4 s.f

(b) the distance in kilometers from A to B to the nearest km





## 61. Linear programming

A man bakes two types of cakes, queen cakes and marble cakes. Each week he bakes **x** queen cakes and **y** marble cakes. The number of cakes baked are subject to the following conditions;  $30x + 20y \le 4800$ ,  $30x + 40y \ge 3600$  and 10x > 30y

He makes a profit of shs.10 on each queen cake and shs.12 on each marble cake.

- (i) Draw a graph to represent the above information on the grid provided
  - (ii) From the graph, determine how many cakes of each type he should make to maximize his weekly profit
  - (iii) Calculate the maximum profit
  - (iv) If he is to make a weekly profit of at least shs.600, find the least number of marble cakes he should bake
- 2. A company produces shirts and jerseys using two types of machines. Every shirt made requires 2 hours on machine **A** and 2 hours on machine **B**. Every Jersey made requires 3hours on machine **A** and I hour on machine **B**. In one day the time limit on machine **A** is 24hours but that on machine **B** is 12hrs. The number of Jerseys produced must not be more than the shirts produced in one day. The company makes a profit of shs.200 on each shirt and shs.200 on each Jersey. The company produces **x** shirts and **y** jerseys per day
  - (a) Write down four inequalities which must be satisfied by  $\mathbf{x}$  and  $\mathbf{y}$  and represent these inequalities on a grid
  - (b) Find the values of  $\mathbf{x}$  and  $\mathbf{y}$  which will give the company maximum daily profit and also state the maximum profit
- 3. A trader makes two types of chair, ordinary and special chairs. The cost of each ordinary chair is shs.300 while each special chair costs shs.700. He is prepared to spend not more than shs.21,000. It is not viable for hi m to make less than 20 chairs. Ordinary chairs must be less than twice the special chairs but more than 15. By taking the number of ordinary chairs as **x** and special chairs as **y**:
  - (a) Write down all the inequalities in x and y
  - (b) Draw the inequalities on the grid provided
  - (c) He sells a special chair at a profit of shs.140 while ordinary chairs at a profit of shs.120; Determine the maximum possible profit
- 4. A school has to take 384 people for a tour. There are two types of buses available.
  - Type X and type Y. Type X can carry 64 passengers and type Y can carry 48 passengers. They have to use at least 7 buses.
  - a) Form all linear inequalities which will represent the above information
  - b) On the grid provided, draw the inequalities and shade the un-wanted region.
  - b) The charges for hiring the buses are;

Type X: shs.25,000

Type Y: shs.20,000

Use your graph to determine the number of buses of each type that should be hired to minimize the cost.

- 5. A shoe maker makes two types of shoes **A** and **B**. He takes 3 hours to make one pair of type **A** and **4** hours to make one pair of type **B**. He works for a maximum of 120 hours to make **x** pairs of type **A** and **y** pairs of type **B**. It costs him Kshs. 400 to make a pair of type **A** and Kshs.150 to make a pair of type **B**. His total cost does not exceed kshs.9000. He must make at least 8 pairs of type **A** and **12** pairs of type **B**.
  - (a) Write down four inequalities representing the information above

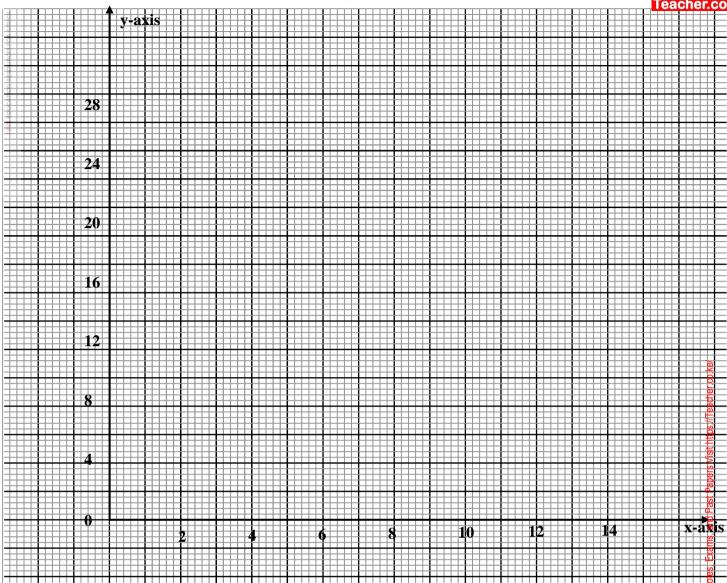
- (b) On the grid provided represent the inequalities and shade the unwanted regions
- (c) The shoe maker makes a profit of kshs.40 on each pair of type **A** and kshs.70 on each pair
- A theatre has a seating capacity of 250 people. The charges are shs.100 for an ordinary seat and shs.160 for a special seat. It costs shs.16,000 to stage a show and the threatre must make a profit. There is never more than 200 ordinary seats and for a show to take place at least 50 ordinary chairs must be occupied. The number of special seats is always less than twice the number of ordinary seats.
- a) taking **x** to be the number of ordinary seats and **y** the number of special seats, write down all the inequalities representing the information above.
- b) On the grid provided, draw the graph to show the inequalities in (a) above
- c) Determine the number of seats of each type that should be booked in order to maximize the profit.
- 7. A man sells two types of ice creams in cups and sticks. He can store less than ten packets in his cooling box. He sells more cups than sticks but less than 3 items as many cups as sticks. He also knows that he will sell more than 3 packets of sticks. His profit is shs.3.00 on a packet of cups and shs.2.00 on a packet of sticks.
  - (a) Form inequalities to represent the above information:

(Let x – packets of cups and

y – packets of sticks)

- (b) On the grid provided graph the inequalities to satisfy the required condition
- (c) How many packets of cups and sticks should the man put in his box to give him the highest profit?
- 8. A shopkeeper bought 50 pangas and 30 jembes :-
  - (a) From a wholesalers for shs.4,260. He had bought half as many jembes and 5 pangas less, he would have paid shs.1290 less. Had the shopkeeper bought form wholesaler **B**, he would have paid 10% more a panga and 15% less for a jembe. How much would he have saved if he had bought the 50pangas and 30 jembes from wholesalers **B**
  - (b) The price of a suit if marked at shs.5000. A discount
- 9. The games master whishes to hire two matatus for a trip. The operators have a Toyota which carries 10passengers and a Kombi which carries 20 passengers. Altogether 120 people have to travel. The operators have only 20litres of fuel and the Toyota consumes 4 litres on each round trip and the Kombi 1 litre on each round trip. If the Toyota makes **x** round trips and the kombi **y** round trips;
  - (a) write down four inequalities in x and y which must be satisfied

b) represent the inequalities graphically on the grid provided



- (c) The operators charge shs.100 for each round trip in the Toyota and shs.300 for each round trip in the kombi;
- (i) determine the number of trips made by each vehicle so as to make the total cost a Minimum
- (ii) find the minimum cost
- 10. The velocity of a particle Vm/s moving in a straight line after t seconds is given by  $V = 3t^2 3t 6$ . Find the distance covered by the particle between t = 1 and t = 4seconds

### 62. Differentiation

- 1. A particle moves in a straight line from a fixed point. Its velocity Vm/s after t seconds is given by  $V = 9t^2 6t + 2$  calculate the distance traveled by the particle during the  $2^{nd}$  second. (4 mks)
- 1. A particle moves such that  $\mathbf{t}$  seconds after passing a given point  $\mathbf{O}$ , its distance  $\mathbf{S}$  metres from  $\mathbf{O}$  is given by  $\mathbf{S} = \mathbf{t}$  ( $\mathbf{t} \mathbf{2}$ ) ( $\mathbf{t} \mathbf{1}$ )
  - (a) Find its velocity when  $\mathbf{t} = 2$  seconds
  - (b) Find its minimum velocity
  - (c)Find the time when the particle is momentarily at rest

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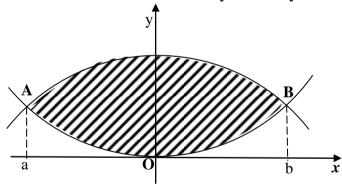
The table below gives the values of x and y for the curve  $y=x^2+1$ 

X	0	1	2	3	4	5	6	7	8	9	10
y	1	2		10	17		37	50		82	

- a) Complete the table
- b) Use the mid- ordinate rule to estimate the area enclosed by the curve  $y = x^2 + 1$ . Use five coordinates
- c) Using integration, calculate the actual area in (a) above
- d) Calculate the percentage error in the estimated area
- 3. The gradient function of a curve is given by the expression 2x + 1. If the curve passes through the point (-4, 6); find the equation of the curve
- 4. A particle **P** moves in a straight line so that its velocity, Vm/s at time t seconds where  $t \ge 0$  is given by  $v = 28 + t 2t^2$

#### Find:

- (a) the time when **P** is instantaneously at rest
- (b) the speed of  $\mathbf{P}$  at the instant when the acceleration of  $\mathbf{P}$  is zero
- (c) Find the acceleration of **P** when the article is instantaneously at rest
- (d) Find the distance covered by the particle during the  $3^{rd}$  second, when at t = 0 D = 5M
- 5. A particle **K** moves a long a straight line 50 cm long. At time  $\mathbf{t} = 0$ , **k** is at **A** and **t** seconds later its velocity **vcm/s** is given by  $\mathbf{v} = \mathbf{15} + \mathbf{4t} \mathbf{3t}^2$ .
  - a) Write down the expression for;
    - i) The acceleration of  $\mathbf{K}$  at time  $\mathbf{t}$  seconds.
    - ii) The distance of **K** from **A** at time **t** seconds.
  - b) i) Find **t** when **K** is instantaneously at rest.
    - ii) How far is **K** from **A** at this time?
  - c) Find the period of time during which the acceleration of **P** is positive.
- 6. The diagram below shows the sketch of the curve  $y = x^2$  and  $y = -x^2 + 8$  intersecting at A and B:-



- (a) Find the value of **a** and **b** hence find the coordinates of A and B
- (b) Find the area enclosed by  $\mathbf{x} = \mathbf{a}, \mathbf{x} = \mathbf{b}$ , the axis and:
  - (i) the curve  $\mathbf{v} = x^2$
  - (ii) the curve y = -x + 8
- 7. The distance from a fixed point of a particle in motion at any time **t** seconds is given by :-  $S = t^3 \frac{5}{2}t^2 + 2t + 5$  metres

Find its:

- (a) Acceleration after t seconds
- (b) Velocity when acceleration is zero
- A particle moves in a straight line. It passes through point **O** at  $\mathbf{t} = \mathbf{0}$  with a velocity  $\mathbf{v} = 5$  m/s. The acceleration  $\mathbf{a}$  m/s<sup>2</sup> of the particle at time  $\mathbf{t}$  seconds after passing through **O** is given by  $\mathbf{a} = 6\mathbf{t} + 4$ 
  - (a) Express the velocity v of the particle at time t seconds in terms of t.

- (b) Calculate the velocity of the particle when t = 4.
- (c) (i) Express the displacement s by the particle after t seconds in terms of t.
  - (ii) Calculate the distance covered by the particle between t = 1 and t = 4.



- 9 . The displacement  $\bm{S}$  metres of a particle moving along a straight line after  $\bm{t}$  seconds is given by.  $S=3t+\underline{3t^2}-2t^3$ 
  - a) Find its initial acceleration
  - b) Calculate:
  - i) The time when the particle was momentarily at rest
  - ii) Its displacement by the time it came to rest momentarily
  - c) Calculate the maximum speed attained
- 10. Find the equation to the tangent to the curve:  $y = 4x^3 - 2x^2 - 3x + 5$  at the point (2, 23)
- 11. A farmer wanted to make a trough for cows to drink water. He had a metal sheet measuring 240cm by 120cm and 1cm thick. The density of the metal is 2.5g/cm<sup>3</sup>. A square of sides 30cm is removed from each corner of the rectangle and the remaining part folded to form an open cuboid.
  - (a) Sketch the sheet after removing the squares for the four corners, showing all the dimensions
  - (b) Calculate:-
    - (i) The area of the metal which forms the cuboid
    - (ii) The mass of the empty cuboid in Kilograms
  - (b) The cuboid is filled with water whose density is 1g/cm<sup>3</sup>. Calculate the mass of the cuboid when full of water
- 12. A rectangular sheet of cardboard is 8cm long and 5cm wide. Equal squares are cut away at each corner and the remainder is folded so as to form an open box. Find the maximum volume
- 13. (a) Find the equation of the normal to the curve :-  $y = x^3 2x 1$  at (1, -2)
  - (b) Determine the nature of the turning points to the curve  $y = x^3 3x + 2$ ; Hence in the space provided below, sketch the curve
- 14. A particle moves in a straight line so that its velocity, v/m/s at time t seconds where  $t \ge 0$  is given by  $v = 28 + t 2t^2$

Find:-

- (a) The time when **P** is instantaneously at rest
- (b) The speed of  $\bf P$  at the instant when the acceleration of  $\bf P$  is zero
- (c) Given that **P** passes through the point **O** of the line when t = 0;
  - (i) Find the distance of **P** from **O** when **P** is instantaneously at rest
- 15. A particle moves such that **t** seconds after passing a given point **O**, its distance **S** metres

from O is given by S=t (t-2) (t-1)

- (a) Find its velocity when  $\mathbf{t} = 2$  seconds
- (b) Find its minimum velocity
- (c)Find the time when the particle is momentarily at rest
- (d) Find its acceleration when  $\mathbf{t} = 3$ seconds



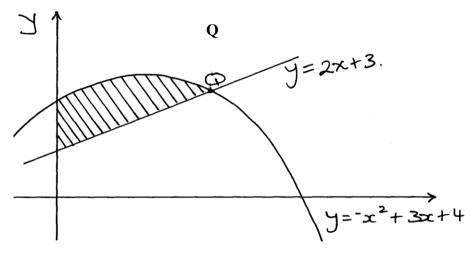
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# 63.Approximation of area

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Use trapezoidal rule to estimate the area bounded by the curve  $y = 8 + 2x - x^2$  for  $-1 \le x \le 3$  using 5 ordinates

- (a) Using trapezoidal rule, estimate the area under the curve  $y = \frac{1}{2}x^2 2$  between x = 2 and x = 8 and x-axis. Use six strips
- (b) (i) Use integration to evaluate the exact area under the curve
  - (ii) Find the percentage error in calculating the area using trapezoidal rule
- (a) Using trapezoidal rule, estimate the area under the curve  $y = \frac{1}{2}x^2 2$  between x = 2 and x = 8 and x-axis. Use six strips
- (b) (i) Use integration to evaluate the exact area under the curve
  - (ii) Find the percentage error in calculating the area using trapezoidal rule
- The figure below shows the graphs of y = 2x + 3 and  $y = -2x^2 + 3x + 4$



- (a) determine the co-ordinates of Q, the intersection of the two graphs
- (b) Find the exact area of the shaded region
  - 5. The table below shows some values of the function;  $y = x^2 + 2x 3$  for  $-6 \le x \le -3$

x	-6	-5.75	-5.5	-5.25	-5	-4.75	-4.5	-4.25	-4.0	-3.75	-3.5	-3.25	-3
у	21	18.56		14.06		10.06	8.25		5		2.25	1.06	0

- (a) complete the table
- (b) using the completed table and the mid-ordinate rule with six ordinates, estimate the area of the region bounded by the curve;  $y = x^2 + 2x 3$  and the lines y = 0, x = -6 and x = -3
- (c) (i) by integration find the actual are of the region in (b) above
  - (ii) Calculate the percentage error arising from the estimate in (b)
- Complete the table below for  $y = 5x^2 2x + 2$ . Estimate the area bounded by the curve, the x axis, the lines x = 2 and x = 7 using the trapezoidal rule with strips of unit length.

X	2	2.5	3	3.5	4	4.5	5	5.5	6	6.5	7
y	18			56.25	74		117			200.25	

# 6. Integration

1. Evaluate:-

$$\int_{2}^{5} \frac{x^2 - 3x + 2}{x - 2} \, \mathrm{d}x$$



2. Find the values of **a** which satisfy the integral  $\int_{0}^{4} (x^2 + 1) dx = 2a$ 

# Answers section I & II

## 1. L.C.M

Size of the land = 
$$(2^3 \times 3 \times 5 \times 7 \times 13) + 7$$
) aces  
=  $10920 + 7 = 10,927$  aces

2.

2	30	45	54
3	15	45	27
3	5	15	9
3	5	5	3
5	5	5	1
	1	1	1

Least volume of 
$$x = 2 \times 33 \times 5 + 21$$
  
=  $270 + 21 = 291$ 

### 3. L.C.M. of 30, 36 and 45

2	30	36	45	
2	15	18	45	
2 3	15	9	45 45	
3	5	3	15	
5	5	1	5	
	1		1	

L.C.M. = 
$$2^2 \times 3^2 \times 5 = 180$$
  
The number  $m = 180 + 7 = 187$ 

4. 
$$x^{2} + x = x(x + 1)$$

$$x^{2} - 1 = (x + 1)(x - 1)$$

$$x^{2} - x = x(x - 1)$$

$$x(x+1)(x-1)$$

$$x^{3} - x$$

### 2. Integers

1. 
$$X > -1$$
$$X \ge 3$$

2. 
$$2x 2^3 x 8^x x 8^2 = 128$$

$$2x \div 2^{3} \times 2^{3} \times x \times 8^{2} = 128$$
Let  $2^{x}$  be  $y$ 

$$\frac{y}{8} \times y^{3} \times 64 = 128$$

$$\frac{8y}{8} = 128/8$$

$$y^{4} = 16$$

$$y^{4} = 24$$

$$\therefore y = 2$$

$$A1$$

$$-5 \times 6 \div 2 + (-5)$$

$$-12 - 3 = 4$$

$$4 \times 4 + 15$$
Numerator  $16 + 15 = 31$ 
Denominator  $-5 \times 3 + -5 = 31$ 

$$-15 + -5$$

$$-15 + -5$$

$$= -20$$

$$\frac{31}{-20}$$

$$= -1^{11}/20$$

4. 
$$= \frac{(-8) - (-4)}{-9 + 15} + \frac{(-16) + (-6)}{46 - 13}$$

$$= \frac{-12}{6} + \frac{-22}{33}$$

$$= -2 - \frac{2}{3}$$

$$= -2 \frac{2}{3}$$

$$P^{-1} = \begin{pmatrix} 4 & -3 \\ 1 & -2 \end{pmatrix}$$

$$-\frac{1}{5} \begin{pmatrix} 4 & -3 \\ 1 & -2 \end{pmatrix} = \begin{pmatrix} \frac{4}{5} & \frac{-6}{5} \\ \frac{1}{5} & \frac{1}{5} \end{pmatrix}$$

$$P^{-1} R = \begin{pmatrix} -4/_5 & -3/_5 \\ -1/_5 & =2/_5 \end{pmatrix} \qquad \begin{pmatrix} -1 & 3 \\ 0 & 2 \end{pmatrix}$$

$$= \begin{pmatrix} 4/_5 & {}^{-6}/_5 \\ & & \\ 1/_5 & {}^{1}/_5 \end{pmatrix}$$

6. 
$$\frac{-8 \div 2 + 12 \times 9 - 4 \times 6}{56 \div 7 \times 2}$$

$$= \frac{-4 + 108 - 24}{16}$$

$$\frac{80}{16}$$

$$= 5$$

# 3. Fractions

1. 
$$\frac{1}{2}x\frac{7}{2} = \frac{3}{2}x\frac{1}{5} = \frac{3}{4}x\frac{5}{5}xX$$
  
 $\frac{7}{2} + \frac{3}{2}x\frac{11}{5} = \frac{15}{5}$ 

**B**1

$$2/5 ÷ \frac{1}{2} 0f^{4}/9 - \frac{1}{10}$$

$$= \frac{2}{5} ÷ \frac{1}{2} X^{4}/9 - \frac{11}{10}$$

$$= \frac{2}{5} x^{9}/2 - \frac{11}{10}$$

$$= \frac{9}{5} - \frac{11}{10} = \frac{18 - 11}{10} = \frac{7}{10}$$

$$^{1}/_{8} - ^{1}/_{6} X^{3}/_{8} = ^{1}/_{8} - ^{1}/_{16}$$
  
=  $^{2-1}/_{16} = ^{1}/_{16}$ 

$$\frac{\frac{2}{5} \div \frac{1}{2} \circ f^{4} - 1^{1}}{\frac{1}{8} - \frac{1}{6} \circ f^{3}} = \frac{\frac{7}{10}}{\frac{1}{16}}$$

$$= \frac{7}{10} X^{16}/1$$

 $= \frac{56}{5} = 11^{1}/5$ 

M1

$$\frac{3}{7}X^{7}/3 = 1$$
  
 $\frac{9}{7}X1 = \frac{9}{7}$ 

$$\frac{3}{4} + \frac{9}{7} = 21 + 36 = 57$$

28 28

$$\frac{9}{7} - \frac{3}{8} = 72 - 21 = 51 \text{ x}^{2}/_{3} = \frac{17}{28}$$
 M1

$$\frac{57}{28} x^{28}/_{17} = 3 \frac{6}{17}$$
 A1

$$= \frac{7}{10} \times \frac{16}{1}$$

$$=\frac{56}{5} = 11\frac{1}{5}$$

5. 
$$\frac{3}{8} \left( \frac{38}{5} - \frac{55}{36} x^{12} \right)$$

$$\frac{3}{8} x^{59}/15 = \frac{59}{40} = \frac{119}{40}$$

6. Numerator

$$\frac{(9/5 X^{25}/18) \div 5/2 X 24}{7/3 - (1/4 x 12) \div 5/3}$$

$$9/5 x^{25}/18 = 5/2 \div 5/3 x 24$$

$$\frac{5}{2} x \frac{3}{5} x 24 = 36$$

$$7/3 - \frac{1}{4} \times 12 \div \frac{5}{3}$$

$$7/3 - 3 \times 3/5$$

$$\therefore 36 = 67.50$$

$$^{8}/_{15} = 67 \frac{1}{2}$$
  
 $^{7}/_{3} - 3 x^{3}/_{5}$ 



Let X be money raised Teachers house =  $\frac{1}{7}x$ Classrooms =  $\frac{2}{3}x^{6}/7 = \frac{4}{7}x$ Remainder =  $\frac{1}{3}x^{6}/7 = \frac{2}{7}x$   $\frac{2}{7}x = 300000$ x = Shs.1050000

# 4. Decimals

- 1. a) 471331.512
  - b) 7.273352
- 3.  $\frac{38 \times 23 \times 27 \times 100 \times 100000}{114 \times 575}$  = 36For elimination of decimals For correct answer only

4. 
$$\frac{84 \times 132 \times 35}{-287 - 560}$$

$$41 \qquad 4 \qquad 16$$

$$= \frac{99}{41} \qquad 1$$

5. 
$$\frac{12 \times 0.25 - 12.4 \div 0.4 \times 3}{\frac{1}{8} \text{ of } 2.56 + 8.68}$$

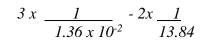
$$\frac{3 - 31 \times 3}{0.32 + 8.68}$$

$$\frac{-90}{9}$$

$$= -10$$

# 5. Squares and square roots

1. (a) (i) 24.78(ii) 0.0316(b) 24.78 - 0.0316 = 24.75 M1 A1





 $3 \times 8.575 - 2 \times 0.07224$  = 25.725 - 0.14448 = 25.58052 = 25.58

3. <u>153 x 1.8</u> 0.68 x 0.32

$$\sqrt{\frac{158 \times 18000}{68 \times 32}} = \sqrt{\frac{9 \times 9000}{4 \times 16}}$$

$$\sqrt{\frac{9 \times 9 \times 10^{3}}{4 \times 16}} = \frac{9 \times 10^{3}/2}{8}$$

$$4 \times 16 \qquad 8$$

 $1.125 \times 10^{3}/_{2}$ 

# 6. Algebraic expressions

1. Let the daughter's age 5yrs ago be x Mother 4x

come;

Daughter = x + 9

Mother = 4x + 9

$$4x + 9 = \frac{5}{2}(x + 9)$$

$$4x + 9 = 2.5x + 22.5$$

$$1.5x = 13.5$$

$$x = 9$$

Mother = 41yrs

$$14 + 41 = 55$$

2. 
$$B.P = 160 \times 50 = 24000$$
  
 $S.P = ((160 \times 8) - (20 + 12)) \times 180$   
 $8$   
 $= 28080$   
 $Profit = 28080 - 24000 = Shs.4080$ 

3. 
$$a) 6a + 7a - 2b - 4b + 2$$
  
=  $13a - 6b + 2$ 

$$b) \underbrace{2x - 2}_{2x} - \underbrace{3x + 2}_{4x} = \underbrace{2(2x - 2) - (3x + 2)}_{4x}$$
$$= \underbrace{4x - 3x - 4 - 2}_{4x}$$
$$= \underbrace{x - 6}_{4x}$$

4. 
$$6u^{2}y^{2} + 13uy - 5 = (2uy + 5)(3xy - 1)$$
$$3u^{2}y^{2} - 13uy + X = (uy - 4)(3xy - 1)$$
$$\underline{(2xy + 5) \quad (3xy - 1)}$$
$$(uy - 4) \quad (3xy - 1)$$
$$= \underline{2xy + 5}$$
$$Uy - 4$$

#### 5. a) From x + y and $x^2 = y^2 = 34$

$$X = 8 - y$$

Substituting for x in  $x^2 - y^2 = 34$ 

$$(8-y)(8-y) + y^2 = 34$$

$$64 - 8y - 8y + y^2 + y^2 = 34$$

$$64 - 16y + 2y^2 = 34$$

$$2y^2 - 16y + 64 - 34 = 0$$

$$2y^2 - 16y + 30 = 0$$

$$y^2 = 8y + 15 = 0$$

$$y(y-3)-5(y-3)=0$$
 (y-5) (y - 3)

y is either 5 or 3

$$but x - y = 8$$

x is either 5 Or 3

$$\therefore x^2 + 2xy + y^2 = 32 + 2 \times 3 \times 5 + 25$$
$$= 9 + 30 + 25 = 64$$

b) 
$$2xy = 2 \times 3 \times 5 = 30$$

c) 
$$x^2 - 2xy + y^2 = 9 - 2 \times 3 \times 5 + 25 = 4$$

d) 
$$x = y = 8$$
 and  $x^2 + y^2 = 34$ 

$$x = 8 - y$$

$$(8-y)^2 + y^2 = 34$$

$$y^2 - 8y + 15 = 0$$

$$y^2 - 3y - 5y + 15 = 0$$

$$y(y-3) - 5(y-3)$$

$$(y-3) = o \ y = 3$$

$$(y-5) = 0$$
  $y = 5$ 

$$x + 3 = 8$$
,  $x = 5$  or  $x + 5 = 8$ 

$$x = 3$$

 $\therefore$  x is either 3 or 5

y is either 3 Or 5

6. 
$$\underline{6x^2 + 35x - 6}$$

$$2x^2 - 72$$

$$= \frac{6x(x - + 6) - 1(x + 6)}{2(x^2 - 36)}$$

$$2(x^2-36)$$

$$= (6x-1)(x+6)$$

$$2(x-6)(x+6)$$

$$= \underline{6x-1}$$

7.

$$2(x-6)$$

$$\frac{2}{5}(3x-2) - \frac{3}{4}(2x-2)$$

$$= 8(3x-2) - 9(2x-2)$$

12

$$= 24 x - 16 - 18x + 18$$

$$= 6x + 2$$

12

$$= 2(3x+1)$$

12

$$=$$
  $\frac{3x+1}{5}$ 

8. Numerator:



X

124x - 2x

385

 $\mathbf{X}$ 

$$4y^2 - x^2 = (2y + x)(2y - x)$$

Denominator:

$$2x^{2} + 4yx + 3yx - 6y^{2}$$

$$= (2x^{2} - 4yx) + (3yx - 6y2)$$

$$= 2x(x-2y) + 3y(x-2y)$$

$$= (2xx+3y)(x-2y)$$
Combining:  $(2y + x)(2y-x)$ 

$$(2x+3y)(x-2y)$$

$$- 2x + 3y \text{ or } -2x - 3y$$

$$2y + x \qquad 2y + x$$

9. 
$$\frac{3(x+y) - (x-y)}{X^2 - y^2}$$
$$= \frac{3x + 3y - x + y}{x^2 - y^2}$$
$$= \frac{2(x+2y)}{x^2 - y^2}$$

10. 
$$x^2 + 2x - 5 = 3x + 1$$
  
 $x^2 - x - 6 - 6 = 0$   
 $(x+2)(x-3) = 0$   
 $x = -2 \text{ or } x = 3$   
When  $x = -2$ ,  $y = 3x - 2 + 1 = -5$  Point  $(-2, -5)$   
When  $x = 3$ ,  $y = 3x + 3 + 1 = 10$  Point  $(3, 10)$ 

11. (a) 
$$y(y+2)$$
  
 $y(y^2-y-60)$   
 $y(y+2) = y+2$   
 $y(y^2-y-6) = (y+2)(y-3)$ 

(b) 
$$y + 2 = \frac{1}{4}$$
  
 $(y + 2) (y-3)$   
 $4y + 8 = y^2 - y - 6$   
 $y^2 - 5y - 14 = 0$   
 $(y-7)(y+2) = 0$   
 $y=7$   
 $y=-2$ 

12. 
$$\frac{104.6}{2.4} = 44 \times 2$$

$$\frac{63.9}{2.4} = 26 \times 2$$

$$2.4$$

$$= 88 + 54 = 142$$

13. 
$$3(25x^2 - 9y^2)$$
  
  $3(5x + 3y)(5x - 3y)$ 

14. i) 
$$d = 8.4$$
  $r = \frac{1}{2}$ 

$$6^{th} jump = 8(\frac{1}{2})^{6-1}$$

$$= 0.2625 = 0.26cm$$

$$ii) 56 = 9.4 (1 - (\frac{1}{2}) 6$$

$$1 - \frac{1}{2}$$
=  $\frac{8.4 \times 63 \times 2}{64}$ 
=  $16.54 \text{ cm}$ 



- 15. Factorizing the numerator  $= p(p^2 q^2) + q(p^2 q)$   $= (p+q) (p^2 q^2)$  = (p+q) (p+q) n(p-q)Factorising the denominator (p+q) (p+q)Numerator = p qDenominator
- 17.  $(x-3) (AX^{2} + BX + C) = x^{3} 7x 6$   $AX^{3} + BX^{2} + CX 3AX^{2} 3BX 3c = x^{3} 7x 6$  A = 1 B 3A = 0  $B 3 \times 1 = 0$  B = 3 -3c = -6 c = 2
- 18. a)  $8(2^2)^y = 6 \times 2^y - 1$  $let t = 2^y$  $8t^2 = 6t - 1$  $8t^2 - 4t - 2t + 1 = 0$ (4t-1)(2t-1)=0 $t = \frac{1}{4} or \frac{1}{2}$  $\therefore t = 2^y = \frac{1}{4} = 2^{-2}$  $\therefore y = -2$ 0r  $t = 2^y = \frac{1}{2} = 2^{-1}$  $\therefore y = -1$  $\therefore y = -2 \ 0r - 1$ b) Numerator =  $2x^2 - 98$  $=2(x^2-49)$ = 2(x+7)(x-7) $Denominator = 3x^2 - 16x - 35$  $= 3x^2 - 21x + 5x - 35$ = 3x(x-7) + 5(x-7)= (x-7)(3x+5) $\therefore 2x^2 - 98 \quad \div$  $\underline{x+7} = \underline{2(x+7)(x-7)} \times \underline{(3x+5)}$  $3x^2 - 16x - 3$  3x + 5 (3x + 5)(x - 7) (x + 7)



19. 
$$\frac{(2x-y)(2x+y)}{(x-3y)(2x-y)} \sqrt{2x+y}$$

$$\frac{2x+y}{x-3y} \sqrt{2x-y}$$

20. 
$$P^{2} - 2pq + q^{2} = (p-q)^{2}$$

$$P^{3} - pq^{2} + p^{2}q - q^{3}$$

$$= p(p^{2} - q^{2}) + q(p^{2} - q^{2})$$

$$= (p+q)(p^{2} - q^{2})$$

$$(p-q)^{2} = (p-q)^{2} \checkmark$$

$$(p+q)(P^{2} - q^{2}) \qquad (p+q)^{2}(p-q)$$

$$= p-q^{1}$$

$$(p+q)^{2}$$

21. Let the numbers be a and b
$$a + b = 15 - x3$$

$$5a - 3b = 19 \times 1$$

$$3a + 3b = 45$$

$$5a - 3b = 19$$

$$8a = 64$$

$$a = 8$$

$$b = 7$$

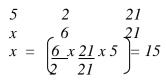
22. 
$$\frac{3(2x-5) - 4(1-x) - 6(x-4)}{12}$$

$$\frac{6x - 15 - 4 + 4x - 6x + 24}{12}$$

$$\frac{4x - 5}{12}$$

# 7. Rates Ratio and percentages

1. Men cottages days



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 $more \ men = 15 - 5 = 10$ 

- 3. a) i) In 1 hr; Tap A fills  $\frac{1}{3}$
- 2. = 2(18.5 + 12.5)Max Perimeter = 62 cmWorking Perimeter = 2(18 + 12)= 60 cm $\% error = \underline{2} X 100 = 3.33\%$ 60 B - 1/4 Capacity filled in 1  $hr = \frac{1}{3} + \frac{1}{4}$  $= \frac{7}{12}$  $^{7}/_{12} = 1 \ hr$  $1 = 1 \times 1 \times \frac{12}{7}$  $= 1 \frac{5}{7} hrs.$  $ii) \frac{1}{3} + \frac{1}{4} - \frac{1}{6} = \frac{5}{12} \implies in \ one \ hr$  $\frac{5}{12} = 1hr$  $1 = 1 \times 1 \times \frac{12}{5}$
- 4. (a)  $\frac{144000 144000}{n 5} R$   $= \frac{720,000}{n(n-5)}$ 
  - (b) 720,000 = 2400 n(n-5) 300 = n(n-5)  $n^2 - 5n - 300 = 0$  (n-20)(n+15) = 0Either n = 20, n = -15 m = 20

 $= 2^{2}/_{5} hrs$ 

(c) contributed = 
$$\frac{144000}{20}$$
 = 7200  
(d) % increase =  $\frac{2400}{7200}$  x 100  
 $\frac{7200}{33.33\%}$ 

5. (a) In 1 hour 
$$\frac{1}{1} + \frac{1}{1} + \frac{1}{1}$$
 of the tank will be filled
$$40 \quad 15 \quad 20$$

$$= \frac{17}{120}$$
In 5 hours =  $\frac{17}{120}$  x 5
$$= \frac{17}{120}$$

(b) In two hours taps x and y

$$\begin{pmatrix}
\frac{1}{40} & + \frac{1}{15} \\
40 & 15
\end{pmatrix}$$
 $x \ 2$  of the tank to be filled
$$= \underbrace{11}_{60}$$
In 7 hours = 
$$\begin{pmatrix}
\frac{11}{60} & + \frac{17}{24} \\
60 & 24
\end{pmatrix}$$

$$= \underbrace{\frac{107}{120}}$$

(c) Remaining fraction = 
$$1 - \frac{107}{120}$$
  
=  $\frac{13}{40}$ 

In  $\underline{1}$  hour proportion, time taken  $\underline{40}$ 

$$= \underline{13} \quad x \quad 40h$$

$$120$$

$$= 4^{1}/_{3}$$

Time taken =  $7 + 4^{1}/_{3}$  = 11 hrs 20 min. Tank will be full at 8.00 + 11hrs 20 min 1920 hrs or 7.30 p.m

6. Let Philip take x days to finish the job alone.

$$\frac{1}{x} + \frac{1}{x+5} = \frac{1}{6}$$

$$6(x+5) 6x = x(x+5) \sqrt{6x+30+6x} = x^2+5$$

$$x^2 - 7x - 30 = 0$$

$$(x-10) (x+3) = 0 \sqrt{6x+30}$$

$$x = 10 \text{ and } x = -3$$

7. 
$$16$$
 9 14  
 $X$  7 12  
 $X = 16 \times 9 \times 14$   
 $7 \times 12$   
 $= 24men$   
 $= 24men = 24 - 6$ 

= 8men

8. a) Let the original no. of people be xOriginally each would contribute  $\frac{180000}{X}$ 

New contribution per person



$$30x^{2} - 90x - 5400 = 0$$

$$3x^{2} - 9x - 540 = 0$$

$$X^{2} - 3x - 180 = 0$$

$$(x-15) (x + 12) = 0$$

$$X = 15 \text{ or } -12$$
Original number of people 15

$$b) \qquad \frac{180000}{15} = \frac{180000}{15}$$

c) Original contribution per person
Shs.12000
New contribution per person
= 180000 = 15000
12
% increase
15000 - 12000 X 100%
12000
3000 X 100%

= 25%

9. a) cost of running the business
$$\frac{20}{100} \times 43200$$

$$= Shs.8640$$

12000

Ratio of contribution 40000 : 64000 5 : 8

> Mue received ½ X 6480 = Shs.3240 8/13 X 28080 = Shs. 17280 = Shs.20320

c) Konie received Shs.3240 + 10800 = 14040

 $\frac{14040}{1800} = 7.8$  = 7 cows

11.



From equation (i) 
$$5B + 30G = Kshs.117000$$
 (dividing through by 5)  
=  $(B + 6G = 23400) \times 4$   
=  $4B + 24G = 93600 \dots (iii)$ 

Equation (ii) 
$$-q(iii) = 4B + 24G = 94750 - 4B + 24G = 93600$$
  
 $G = 1150$ 

.: 1 goat costs Kshs.1150

Substituting in (i)

5B + 30 (1150) = 117000

5B + 34500 = 117000

5B = 825000

B = Kshs.16500

#### b) Abduls selling price

Bull 
$$^{140}/_{100}$$
 x  $^{16500} = 23100$  x  $^{5} = Kshs.115,500$ 

$$Goat^{130}/_{100} \times 1150 = 1495 \times 30 = Kshs.44850$$

Ali's selling price

Bulls  $^{150}/_{100}x$  16500 = 24750 x 4 = Shs.99000

Goats 
$$\frac{140}{100}$$
 x  $1150 = 1610$  x  $25 = Shs.40250$ 

$$Total 99000 + 40250 = Kshs.139,250$$

Profit made

$$Abdul$$
 \_\_\_\_\_  $Kshs. (160350 - 117000) = Kshs. 43350$ 

Ali Kshs. 
$$(139250 - 94750) = Kshs.44500$$

Ali made more profit by Kshs.1150/=

#### 12. Original costs

$$T = \frac{8}{24} x = \frac{x}{3}$$

$$L = \frac{4}{24}x = \frac{x}{6}$$

$$R = \frac{12}{24}x = \frac{x}{2}$$

New 
$$T = \frac{x}{3} x 1.12 = 0.3733x$$
  
 $L = \frac{x}{6} x 1.18 = 0.1967x$   
 $R = \frac{x}{2} x 1.4 = 0.7x$   
Therefore % change  
 $(0.3733x + 0.967x + 0.7x) - x x 100$   
 $X$ 

$$= 0.27 \times 100$$
  
= 27%



13. Let Mary's yrs be x

Mothers age =  $2\frac{1}{2}x$ 4yrs ago Mary was x - 44yrs ago mother was  $2\frac{1}{2}x - 4$ 

$$\frac{2\frac{1}{2}x - 4}{x - 4} = \frac{3}{1}$$

$$\frac{5}{2}x - 3x = -12$$

$$-\frac{1}{2}x = -12$$

$$x = 24yrs$$
mother's age is =  $(\frac{5}{2}x + 24)$ 
= 60yrs

15.. Ratio 
$$K: B = 3:4$$
a) Kongo got  $\frac{3}{5}$  x  $\frac{35}{100}$  x  $\frac{31}{100}$  = 27195/=

Beatrice got  $\frac{4}{7}$  x  $\frac{35}{100}$  x  $\frac{181300}{100}$  =  $\frac{36260}{7}$ 
b) Kongo got  $\frac{3}{7}$  x  $\frac{60}{100}$  x  $\frac{181300}{100}$  +  $\frac{9000}{7}$ 
Beatrice got  $\frac{4}{7}$  x  $\frac{60}{100}$  x  $\frac{181300}{100}$  +  $\frac{120000}{7}$ 
=  $\frac{182,160}{100}$ 

16. Let no. be mn  

$$M + n = 9...(i)$$
  
 $10m + n$ , reversed  $10n + m$   
 $10n + m - 10m + n = 27$   
 $1n - 9m$ 

17. 
$$V1 = \pi r^{2}$$

$$h$$

$$R = 130r = 1.3r$$

$$H = \underline{80}h = 0.8h$$

$$100$$

$$V_{2} = \pi R^{2}h = (1.3r)^{2} \times 0.8h$$

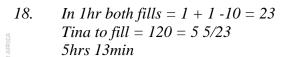
$$= 1.352V_{1}$$
% change =  $\underline{V_{2} - V_{1}} \times 100$ 

$$V_{1}$$

$$= (\underline{1.352 - 1}) V_{1} \times 100$$

$$V_{1}$$

$$0.352 \times 100 = 35.2\%$$





19. 
$$16$$
 9 14  
 $X$  7 12  
 $X = 16 \times 9 \times 14$   
 $7$  12  
 $= 24men$   
 $Extra\ men = 24 - 6$   
 $= 8men$ 

20. a) Expenses = 
$$\underline{30}$$
 x 600,000  
 $100$   
=  $sh. 180,000$   
Business =  $\underline{15}$  x 420,000  
 $100$   
=  $sh. 63,000$   
Rest of profit =  $357,000$   
Ratio  $160:200:240$   
4: 5: 6

(i) Langat received = 
$$sh \pm x 357,000$$
  
 $15$   
=  $sh 95,200$   
(ii) Korir received =  $sh \pm x 357,000$   
 $15$   
=  $sh 119,000$ 

(iii) Koech received = 
$$sh \frac{6}{15}$$
 x 357,000  
= 142,800

(b) 
$$\% = \frac{119,000}{600,000} \times 100$$
  
= 19.83

b) 
$$\frac{5}{4}$$
 x  $400 = 500$ 

22. Alcohol 
$$A = {}^{25}/_{120}$$
  
 $= 30 cm^3$   
Alcohol in  $B = {}^{20}/_{100} x 180$   
 $= 36 cm^3$   
Results =  $36 + 30$   
 $120 + 180$   
 $= 66 x 100$   
 $300 = 22\%$   
Remaining =  $300 - x$   
Volume of alcohol =  $(300 - x) x^{22}/_{100} = 66 - 0.22x$   
Total volume of alcohol =  $66 - 0.22x + x$ 

$$= 66 + 0.78x$$

% 
$$alcohol = \underline{66 + 0.78x \times 100} = 35$$
  
 $300$   
 $= 66 + 0.78x = 105$   
 $0.78x = 39$   
 $x = 50$ 



24. 
$$a:b = 1:2$$
  
 $b:c = 3:4$   
 $a:b = 3:6$   
 $b:c = 6:8$   
 $\therefore a:b:c = 3:6:8$ 

# 8. Length

1. 
$$\frac{3x + 2y)(5x - 3y)}{(5x - 3y)(x - y)}$$
$$= \frac{3x + 2y}{x - y}$$

2.

$$3N + \frac{1}{2}(R-M)$$

$$= 3 \begin{pmatrix} \frac{2}{3} & 1 \\ 2 & 4 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} -1 - 2 \\ 0 & 0 \end{pmatrix} \qquad \begin{pmatrix} 3 & 0 \\ 1 & 4 \end{pmatrix}$$

$$= \begin{pmatrix} 2 & 3 \\ 6 & 12 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} -4 & 2 \\ 1 & 4 \end{pmatrix}$$

$$= \begin{pmatrix} 2 & 3 \\ 6 & 12 \end{pmatrix} + \begin{pmatrix} -2 & 1 \\ 0.5 & -2 \end{pmatrix} = \begin{pmatrix} 0 & 4 \\ 6.5 & 10 \end{pmatrix}$$

1. 
$$M \times m \text{ value} = \underline{2.655 + 6.415}$$
  
 $6.405 - 2.655$   
 $= \underline{9.07}$   
 $3.75$   
 $= 2.4187$ 

2. (a) Number of tiles = 
$$\underline{10.5 \times 6}$$
 to cover the room 0.3 x 0.3 = 700 tiles

(b) (i) 15 x 700 tiles  

$$15 \times 700$$
 cartons  
20  
 $Cost = 15 \times 700 \times 800$   
 $20$   
 $Cost = Kshs. 420,000$ 



Selling price = 
$$\frac{112.5}{100}$$
 x 422600  
= Kshs. 475, 425

3. 
$$\underline{AC} = 10 = AC = 8.66$$

$$Sin 60^{\circ}$$

$$\angle A70^{\circ}, \ \underline{BC} = 10 = BC = 8.91$$

$$Sin 70^{\circ}$$

$$Area = \frac{1}{2}x \ 8.66 \ x \ 8.91 \ sin 50^{\circ}$$

$$= 27.28$$

4. 
$$S = \frac{1}{2}(170 + 190 + 210)$$
  
 $S = 285$   
 $Area = 285(285 - 170)(285 - 190)(285 - 210)$ 

$$= 2865 \times 115 \times 95 \times 75$$

$$= 15281m^{2}$$

$$10,000$$

$$= 1.528ha$$

5. LCM of 30, 50 and 35 mins  

$$30 = 2 \times 3 \times 5$$
  
 $35 = 5 \times 7$   
 $50 = 2 \times 52$   
L.C.M =  $2 \times 3 \times 5 = 1050$   
Into hrs ( $\underline{1050}$ ) hrs =  $17.5$ hrs  
 $\underline{60}$   
Next wail together at 7:18  
 $+\underline{17:30}$   
 $\underline{24:48}$   
= at 1. 48 a.m on Tuesday

6. Maize - 
$$\frac{1}{4}x\frac{2}{1} = \frac{1}{3}$$
  
Remainder -  $\frac{2}{3} - \frac{1}{6} = \frac{3}{2} = \frac{1}{2}$   
 $\frac{3}{6} = \frac{6}{6}$   
Beans -  $\frac{4}{5}x\frac{1}{2} = \frac{2}{5}$   
carrrots -  $\frac{1}{5}x\frac{1}{2} = \frac{1}{10}$   
Let total area of farm be x acres  $\frac{1}{1}x = 0.9$   
 $\frac{1}{10}$   
 $x = 0.9 \times 10 = 9$  acres

## 10. Volume and capacity

L.s.f. = 
$$\frac{18}{24} = \frac{3}{4}$$
  
A.s.f =  $\frac{9}{16}$   
v.s.f =  $\frac{27}{64}$   
 $\frac{h}{3.2} = \frac{3}{4} \Rightarrow 4h = 3h + (3 \times 3.2)$   
 $h = 9.6$ 

(i) surface area of small cone:

$$L = \sqrt{9^2 + 9.6^2} = 13.16m$$

$$S.A = (3.142 \times 9 \times 13.6) = 384.581$$
Curved area of frustrum
$$= \frac{7}{1} \times \frac{3.142 \times 9 \times 13.16}{9}$$

$$= 289.4$$

$$Top area = (3.142 \times 9^2) = 254.5cm$$

$$\therefore Total area = 543.9m^2$$

(ii) Volume of smaller cone =  $3.142 \times 9^2 \times 9.6$  3= 814.41Volume of frustrum =  $(37 \times 814.41)$  27=  $1116.043m^3$ = 1116043LLitres used per day=  $(15 \times 15 \times 40) + (116 \times 65) = 16540L$ No. of days = 111604316540 = 67.5days

2. 
$$L.S.F = \frac{3}{2} = \frac{28 + h}{2}$$
  
 $56 + 2h = 3h$   
 $h = 56cm$   
 $Volume = \frac{1}{3}r^{2}H - \frac{1}{3}r^{2}h$   
 $= \frac{1}{3}x^{\frac{22}{7}}x^{\frac{15}{x}}15x^{\frac{56}{3}} - \frac{1}{3}x^{\frac{22}{7}}x^{\frac{10}{x}}x^{\frac{10}{x}}x^{\frac{28}{3}}$   
 $= \frac{13200 - 29331}{3}$   
 $= \frac{10.2667}{3}$ 

(b) Slant height = 
$$152 + 562 = 3361$$
  
=  $57.97cm$   
Curved surface  $-RL-rl$ 

3. 
$$2.6 \times 4.8 \times 3.2 = 39.936m^3$$
  
 $1m^3 = 1000 litres$   
 $39.936m^3 = 39.936 \times 1000$   
 $= 39936 \ litres$ 

4. The top surface of the frustrum is-2/3 way up the vertical height of the original one.  $\Rightarrow VX: XY = 1/3h: h = 1:3$  Using similar triangle we have

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```
R = VX = 1
       VY 3
R:R = 1:3
\underline{r} = \underline{1} \implies R = 3r
R 3
R = 3x7 = 21cm
(c)height of removed cone is <sup>1</sup>/<sub>3</sub> height of original cone
         h = \frac{1}{3} \times 45 = 15cm
volume of removed cone = \frac{1}{3} r^2 h
                            = 1 \times 22 \times 7 \times 7 \times 15
                            = 770cm^3
         Now L. S. F = \frac{1}{3}
         V. S. F = (1/3)^3 = 1/27
         Hence ratio of volumes = 1:27
         Volume of original cone = 27x Vol. of small cone
                                              = 770 \times 27 = 20790 \text{cm}^3
                  Capacity of frustrum
         = vol. of original cone - vol. of removed cone
         = 20790 - 770 = 20020 cm^3
         20200
         1000 = 20 l
```

(d) capacity of tank = 
$$\underline{150 \times 120 \times 80}$$
  
 $1000 = 1440l$   
No. of buckets =  $\underline{1440}$   
 $20 = 72buckets$ 

5.  $Mass\ of\ water = 1\ x\ 3000\ cm^3 = 3000\ g$   $Mass\ of\ alcohol = 0.8\ x\ 1200 = 9600g$   $Mass\ of\ mixture = 12,600g$  $Volume\ of\ mixture = 15,000\ cm^3$ 

Density of mixture = 
$$\frac{12600}{15000}$$
  
=  $\frac{0.84g/cm^3}{}$ 

- 6. (a) Vol. of  $tank = 22 \times 144 \times 1.7 = 5.236$ Vol. of  $milk = \frac{3}{5} \times 5.236 = 3.146m^3$ Vol. in liters =  $3.1416 \times 1000 = 3141.6$ litres
  - (b) (i) Vol. of packet ( $^{1}/_{3}$  x 10 sin 60) x 13.6 = 26.97 x 13.6 = 3.66.75cm<sup>3</sup> = 367cm<sup>3</sup>
  - (ii) No. packets =  $(3141.6 \times 1000)$ 367
  - (iii) Amount = 8560.2 x 20 = 171204.3597 = Shs.171,204.40

#### 



11. Mass, weight and density

Density = 
$$300 \times 1,000,000$$
  
 $20 \times 1000$   
1

 $=15,000 \text{ kg/m}^3$ 

2. 
$$D = \frac{M}{V}$$
 $Mas = D \times V$ 
 $= \frac{1g \times 2500 \text{cm}^3}{\text{cm}^3}$ 
 $= 2500g.....(i)$ 
 $Mass = 0.8 \times 8000$ 
 $= 6400g.....(ii)$ 
 $total\ mass = (2500 + 6400)g$ 
 $= 8900g$ 
 $Density\ of\ mixture = \frac{8900g/\text{cm}^3}{10500}$ 

### *12. Time*

- 1. Time between Monday 0545hr and Friday 1945 = 4x 24 + 14 = 110 hrsTime lost = 0.5 x 110 = 55 min. Time in 12 hr system (1945 - 55 - 1200)6.50 p.m.
- 2. Time between Monday 0445h and Friday 1845h =  $4 \times 24 + 14 = 110h$ Time lost =  $0.5 \times 110$ = 55minTime shown in 12 hour system 1845 - 55 = 1750 h= 5.50 p.m
- 3. (a)  $1600h 830h = 7hrs \ 30min \ or \ 7 \frac{1}{2} \ hours$ 
  - (b) Average speed =  $\frac{300}{7\frac{1}{2}}$ = 40 km/h

## 13. Linear

1. The diagram below shows the graphs of  $Y = \frac{3}{10}x - \frac{3}{2}$ , 5x + 6y = 30 and x = 2

By shading the unwanted region, determine and label the region R that satisfies the three inequalities;



$$Y \ge \underline{3}x - \underline{3}$$
,  $5x + 6y \ge 30$  and  $x \ge 2$  (2 mks)  
 $10 \quad 2$   
 $L_1 y = \underline{3}x - \underline{3}$  at (0, 0)  
 $10 \quad 2$   $0 \ge 2$  \*

Picking 
$$P(0,0)$$
  
 $0 \ge -\frac{3}{2}$   
 $2$   
 $L_2 \ 5x + 6y = 30$   
 $At \ (0, 0) \ 5x + 6y \ge 30$   
 $0 \ge 30 \ *$ 

3. Let the cost of a biro be b

Pencil be p  $2b + 5p = 120 \times 3$   $3b + 2p = 114 \times 2$  6b + 15p = 360 6b + 4p = 228 11p = 132 P = 121 2b + 60 = 120 2b = 60 b = 30The cost of 1 biro is 30/=

4. Let son's present age be n yrs
Father's age is 2n yrs
Ten years ago: son's age  $\Rightarrow n$ -10
Father's age  $\Rightarrow 2n$ -10
Son's present age = 30yrs
Father's present age = 2x 30 = 60yrs

The cost of 1 pencil is 12/=

5. 
$$2x + 21 > 15 - 2x$$
  
 $4x > 0.6$   
 $x > -1 \frac{1}{2}$   
 $\Rightarrow -1 \frac{1}{2} < x \le 3$   
Values are -1, 0, 1, 2, 3.

$$15 - 2x \ge x + 6$$
$$-3 \ x \ge -9$$
$$x \le 3$$

$$y = -2x + 4$$
  
gradient of h line is  $\frac{1}{2}$   
Equation  $\frac{y+4}{x+1} = \frac{1}{2}$   
 $2y+8=x+1$   
 $2y-x+7=0$ 

$$2s + 3t = 1750$$
  
 $3s + 2t = 1500$   
 $4s + 6t = 3500$   
 $9s + 6t = 4500$   
 $2t = 1500 - 600$   
 $t = 450$   
 $t = 450$   
 $t = 450$   
Shirt =  $t = 1000$   
 $t = 450$   
 $t = 450$ 

8. Let 
$$r = 3.818181...$$
  
 $100r = 381.818181$   
 $99r = 378 = 42$   
 $99$   $11$   
 $= 3^{9}/_{11}$ 

9. (a) Let cost of pencils be x and biro pens to be y
$$4x + 6y = 66$$

$$2x + 5y = 51$$

$$4x + 6y = 66$$

$$4x + 10y = 102$$

$$4y = 96$$

$$y = 24$$

$$Correct substitution$$

$$\therefore x = 3$$

$$Pencils = shs.9$$

$$Biro pens = 3$$

(b) 
$$9p + 3b = 228...(i)$$
  
 $b - y = 4$   
 $b = 4 + r$ ......(ii)  
substituting for b in ......(i)  
 $p^2 + 5p - 288 = 0$   

$$p = \frac{-5 \pm \sqrt{25 - 4 \times 1 \times -228}}{2 \times 1}$$
 $P = 13$  (to the nearest whole no.)  
 $b = 4 + 13 = 17$ 

10. 
$$3x-2(x+2) = 21$$
  
 $X = 25$   
Large No = 25 + 2 = 27  
 $\therefore$  product = 25 x 27 = 695

11. 
$$x-20 + 3x = 180^{\circ}C$$
 Attempt to get x by using  $t+e = 180^{\circ}$   
 $4x = 200$   $e = (2n-4)90$   
 $n$   
number of sides 145



12. 5x + 4y = 6160 4(3x + y = 2800) -7x = -5040 x = 720 y = 640 4(720) + 2(640) = 4160

13. 2x + 3y = 390 5x + 2y = 810 15x + 6y = 2430 4x + 6y = 780 11x = 1650 x = 150A pair of trouser = sh150 A shirt = sh30

## 14. Equations

- 1. Through A/C in Kenya 1000000 X 76.84 = Shs.7684000 through A/C in UK 1000000 X 115.70 = Shs.7,562,091.15 1.53 Through UK less by 768400 - 7562091.85 = 121,908.85
- 2.  $6000 turn \____ 6000 X 84.15$  = Kshs.504900 Balance = 504900 - 300000 = 204900  $\therefore sterling pound = \frac{204900}{121.47}$ = 1686.8
- 3. In Rand =  $\frac{2800265}{10.0166}$  = 279562.4264  $\frac{10.0166}{10.0166}$  Expenses = (115,700 + 97000 + 53689) = 266389 Rand Remainder = 279562.4264  $\frac{266,389.000}{13,174.4264}$ Amount in Kshs. = 13174.4264 x 9.9399 = 130,942.50
- 4. Kshs.  $(3000 \times 1.89) = 5670$ Remain = 5670 - 4695 = 75Francs =  $(\underline{975}) = 500$ 1.95
- 5. Amount in dollars =  $75 \times 40 = 3,000$ Amount in Ksh =  $3000 \times 81.40 = 244,200/=$ Less commission 4,000

Total received sh 240,200



```
Hong Kong 8105,000 \times 9.74 = ksh.1022700

Amount spent in Kenya = 403879

Balance = 1,022,600 - 403,879 = 618,821

Amount in South Africa = 618821

12.11 = 51100rands
```

12.11 = 51100rand 500000 J yen into Kshs.=  $(\underline{500000} \times 66.5)$  100= Kshs. 330,250Amount spend in Kenya= Kshs. 16200Remained with Kshs. (330250 - 16200)= Kshs. 314,040Kshs. 314040 into Euros: =  $(\underline{314040})$  78.15= 4,018.554063Euros He left Kenya with = 4,019 Euros (nearest Euro

9. 1UK £ = 125.30  $9000 UK £ = 125.30 \times 9000$  = 1,127,700  $Commission = 5/100 \times 1,127,700 = 56,385$  He got 1,071,315  $Expenditure = \frac{3}{4} \text{ of } 1,071,315 = 803,486.25$   $Amt. \ left = 267,828.75$   $In \ US $ = \frac{267,828.75}{63.20}$   $= 4237.7966 \qquad \simeq 4237 \ US $$ 

10. 1 sterling pound = Kshs.120 ? = Kshs.100000 100000/<sub>120</sub> = 833.3 sterling pounds 1 sterling pound = 1.79 U.S dollars 833.3 = ? = 833.3 x 1.79 = 1491.7 dollars 1 U.S dollar = Kshs.78 1491.7 dollars = Kshs? 1491.7 x 78 = 116350 Kenya shillings



11. Amount received in Kenya shillings

$$= \sum 50,000 \text{ x Shs.} 120.7131$$

 $\Sigma = Kshs.6035655$ Amount received in sterling pound

$$= 1 \sum x K shs. 6035655$$

$$120.9294 = \Sigma 49910.568$$

12.  $Sh(20000 \times 147.86) = sh.2957200$   $To \ US \ Dollars = \underline{44700}$ 74.5

= 6000

He received 6000 US Dollars

13. a) 
$$6a + 7a - 2b - 4b + 2$$
  
=  $13a - 6b + 2$ 

$$b) \underbrace{2x - 2}_{2x} - \underbrace{3x + 2}_{4x} = \underbrace{2(2x - 2) - (3x + 2)}_{4x}$$
$$= \underbrace{4x - 3x - 4 - 2}_{4x}$$
$$= \underbrace{x - 6}_{4x}$$

#### 15. Commercial arithmetic

1. 
$$2x - 3y + 6 = 0$$
$$-3y = -2x - 6$$
$$y = \underline{2}x + 2$$
$$3$$
When  $y = 0$   $x = -3$ 
$$x = 0$$
  $y = 2$ 

 $\therefore$  Co-ordinate of y – intercept is (0,2)

" 
$$x$$
 – intercept is (-3,0)

$$\therefore \angle CAO = tan^{-1} \underline{2}$$

$$= 33.69^{\circ}$$

$$\therefore \angle \theta = 180 - 33.69^{\circ}$$
$$= 146.31^{\circ}$$

2. Point 
$$y(4+-2, \frac{7+-1}{2}) = (1, 3)$$
  
 $grad AB = \frac{7+1}{2} = \frac{8}{2}$ 

$$grad xy = -\frac{3}{4}$$

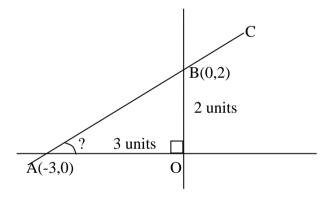
$$grad xy = -\frac{3}{4}$$

$$y - 3 = -\frac{3}{4}$$

$$x-2$$

$$y = -\frac{3}{4}x + \frac{15}{4}$$

3. 
$$Y = 3x - 1$$
  
 $M = 3$   
 $M_1m_2 = -1$   
 $M_2 = -\frac{1}{3}$ 



$$\frac{y-3}{x-2} = -\frac{1}{3}$$

$$3y-9 = -x+2$$



$$3y - 9 = -x + 2$$

$$3y = -x + \frac{11}{3}$$

$$3$$

$$Y = \frac{x}{3} + \frac{11}{3}$$

Pt T is  $\frac{1+5}{2}$ ,  $\frac{4+10}{2} = (-2, 7)$ grad. of grid  $xy = \frac{10-4}{-5-1} = \frac{14}{-6} = \frac{-7}{3}$ ∴ grad of  $L_2 = \frac{3}{7}$ Take a general pt P(x,y) on  $L_2$ 

$$\Rightarrow \frac{y-7}{x-2} = \frac{3}{7}$$

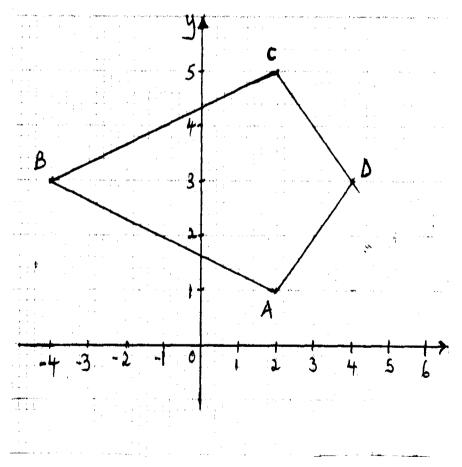
$$\Rightarrow 7y - 49 = 3x + 6$$

$$7y = 3x + 55$$

$$Or \ y = \frac{3x}{5} + \frac{55}{5}$$

Equation of L<sub>2</sub>

5. a, b



(c) Name: a kite

6. (a) Grad of line 
$$QP = \frac{4-2}{1-3} = \frac{2}{-2} = -1$$

Grad of line QR = 1

Take a pt Q(1,4) and T(x,y) on line QR

$$y-4=1$$

x-1

$$y - 4 = x - 1$$

 $y = x + 3 \dots equ$ . of QR

(b) 
$$y = x+3$$
 ...(i) Equ of QR  
 $y = 3x - 7$  ...(ii) Equ. of Pr

Solving simultaneously ;:

$$x + 3 = 3x - 7$$

$$2x = 10$$

$$x = 5$$

Substituting; y = 8

 $\therefore R$  is the pt (5,8)

(c) 
$$PS = QR = \begin{bmatrix} 5 \\ 8 \end{bmatrix} - \begin{bmatrix} 1 \\ 4 \end{bmatrix} = \begin{bmatrix} 4 \\ 4 \end{bmatrix}$$

$$OS = \begin{pmatrix} 3 \\ 2 \end{pmatrix} + \begin{pmatrix} 4 \\ 4 \end{pmatrix} = \begin{pmatrix} 7 \\ 6 \end{pmatrix}$$

*S is the point* (7,6)

7. a) Gradient 
$$OA = Gradient \ of \ CB$$

$$\frac{-1-0}{2-0} = -\frac{1}{2}$$

$$Gradient \ of \ CB$$

$$\frac{y-3}{0-4} = -\frac{1}{2}$$

$$2y-6=4$$

$$2y=10$$

$$y=5$$

b) i) 
$$AN = ON - OA = \frac{1}{2}OM - OA$$
  
 $OM = OA + \frac{1}{2}AB = (2) + \frac{1}{2}(2)$   
 $= 3$   
 $AN = \frac{1}{2}$   
 $= \frac{1}{2}$   
 $= \frac{1}{2}$   
 $= \frac{1}{2}$ 

ii) 
$$NC = OC - ON$$

$$= \begin{bmatrix} 0 \\ 5 \end{bmatrix} - \begin{bmatrix} 3/2 \\ 1/2 \end{bmatrix} = \begin{bmatrix} -3/2 \\ 1/2 \end{bmatrix}$$

*iii)* 
$$AC = OC - OA = \begin{bmatrix} 0 \\ 5 \end{bmatrix} - \begin{bmatrix} 2 \\ -1 \end{bmatrix} = 2 \begin{bmatrix} -1 \\ 3 \end{bmatrix}$$

c) 
$$AN = \frac{1}{2} \begin{bmatrix} 1 \\ 3 \end{bmatrix}$$

$$NC = \frac{3}{2} \left( -\frac{1}{3} \right)$$



a)  $\triangle$  ABC line AB = 7 cm and BC = 8 cm.

Construction of  $\angle 60^{\circ}$ 

(b)  $AC = 7.6 \pm 0.1$  and

$$\angle ACB = 53 \pm 1^{\circ}$$

(c) 2 sides bisector  $\underline{1}$ Circle drawn radius 4.4.  $\pm 0.1$ 

(d) Bisect  $\angle ACB$ 

Bisection line to cut the circle to identify P

(a) 
$$AB = 7$$
 cm,  $BC = 8$  cm  
 $\angle ABC = 60^{\circ}$ 

(b) 
$$AC = 7.6 \pm 0.1 \text{ cm}$$
  
 $\angle ABC = 53^{\circ} \pm 0.1$ 

(c) Perpendicular bisectors of any two sides. Circle drawn Radius =  $4.4.\pm0.1$ . cm

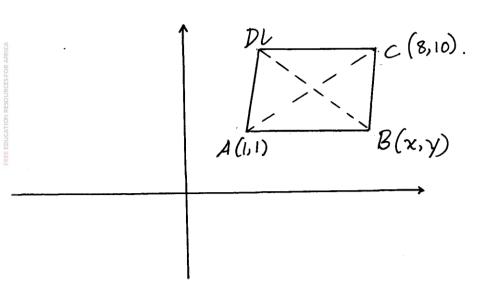
(d)  $\angle ACB$  bisected

Bisection line drawn to cut circle at P

$$\angle BPC = \angle BAC = 67^{\circ}$$

$$\angle PBC = 88 \pm 0.1^{\circ}$$





$$M(\underbrace{1+8, 1+10}_{2}) = M(4.5, 5.5)$$

b) AB: 
$$4x - 5y = -1 \times 2$$
  
BC:  $5x - 2y = 20 \times 5$   
 $8x - 10y = -2$   
 $25x - 10y = 100$   
 $-17x = -102$   
 $x = \frac{102}{17} = 6.0$   
 $24 - 5y = -1$   
 $5y = -25$   
 $Y = 5$   
 $\therefore B(6,5)$   
 $x + 6.0 = 4.5$   $x = 3$   
 $y + 5 = 5.5$   $y = 6$   
 $\therefore D(3,6)$ 

c) 
$$AB = \sqrt{(16-1)^2 + (5-1)^2}$$
  
 $\sqrt{25 + 16}$   
 $\sqrt{41} = 6.40 \text{ (units)}$ 

10. Mid ordinate
Area = 1.2 (6.2 + 4.3 + 2.6)
= 15.72

# 16. Coordinates and graphics

1. Let the exterior 
$$\angle$$
 be  $x$   
 $6.5x + x = 180$   
 $7.5x = 180^{0}$   
 $x = 24$ 

No. of sides = 
$$\frac{360}{24}$$
  
= 15 sides.

3. 
$$\frac{15 b}{2 2} = 60$$

$$15b = 60 \times 4$$

$$b = 16cm (diagonal)$$

$$\Rightarrow = \sqrt{8^2 + 7.5^2}$$

$$\therefore per = 4 \sqrt{8^2 + 7.5^2}$$

$$= 43.86cm$$

(2(8) - 4) 90=  $12 \times 90 = 1080$ 

4. 
$$x^{2} = 7.25^{2} - 5.25^{2}$$
  
 $x = \sqrt{7.25^{2}} - 5.25^{2}$   
 $= 52.5625$   
 $27.5625$   
 $\sqrt{25}$   
 $= 5cm$ 

B

 $x$ 
 $x$ 
 $x$ 

$$BC = 15.25 + 5 = 22.25cm$$
  
 $Arc CD = {}^{90}/_{360} X 3.142 X 2 X 22.25$   
 $= 34.65475$   
 $Perimeter = AB + BC + CD + DE + EA$   
 $= 15.25 + 7.25 + 22.25 + 34.95 + 5.25$   
 $= 84.95cm$ 

5. 
$$AB^2 = 10^2 - 8^2 = 100 - 64$$
  
 $AB^2 = 36$   
 $AB = 6cm$   
 $Cos (90^\circ - x^{\circ) 8}/_{10} = \frac{4}{5}$ 

Attempt to get x by using  $t+e = 180^{\circ}$  e = (2n-4)90 nnumber of sides

6. 
$$x - 20 + 3x = 180^{\circ}C$$
  
 $4x = 200$   
 $x = 50^{\circ}$ 

7. 
$$2x + 40 + x - 25$$
$$3x + 15 + 9 = 180$$
$$3x + 15 = 29$$
$$9 = \frac{1}{2}(3x + 15)$$
$$3x + \frac{3x}{2} = 180 - 15 - \frac{15}{2}$$
$$x = 35^{\circ}$$
$$x = 35 = 10^{\circ}$$
$$\frac{1}{2}(10 + 110) = 60^{\circ}$$

8. 
$$\frac{1260}{90} = 14rt \angle s$$

Sum of interior  $\angle s$  (2n -4) rt  $\angle s$ 

2n-4 = 14n = 9

9 sided polygon

9.  $N = 50 + 40 = 90^{\circ}$ Alternative angles

10.  $5^{3(y+1)} + 5^{3y} = 630$ Let  $x = 5^{3y}$   $5^{3} x 5^{3y} + 5^{3y} = 630$  125x + x = 630 x = 5  $5^{3y} = 5^{1}$  3y = 1  $y = \frac{1}{3}$ 

- 11.  $\frac{360}{n} + 108 = 180 \frac{360}{n}$ 360 + 108n = 180n 360-72n = -720n = 10
- 12. Let exterior angle be x  $\frac{4x}{4} = \frac{180^{\circ}}{4}$   $x = 45^{\circ}$   $n = \frac{360}{4}$ Exterior angle  $n = \frac{360}{45}$  = 8sides
- 13. a) Let  $< BDC = \emptyset$   $A^2 = 5^2 + 8^2 - 2 \times 5 \times 8 \cos \emptyset$   $\cos \emptyset = 89 - 16 = 73 = 0.9125$  80 = 80  $\emptyset = 249$  $1 = 24^{\circ}8$

b) Area of ABD = ½ x 8 x 10 sin 24 °9 ¹ = 40 x 0.4091 = 16.36cm<sup>3</sup> 16.37 16.38

- 14. (a)  $\angle CDF = 100\text{-}60\text{=}40^{\circ}$  (exterior angle of a  $\Delta$ ) (b)  $\angle BDE = 20^{\circ}$  (DE is bisector of BDG)  $\therefore \angle ABD = 20^{\circ}$  (alternate angles)
- 15. 4x + x 30 = 180 $5x = 210^{\circ}$ x = 42 $(x 30)n = 360^{\circ}$  $12n = 360^{\circ}$

$$n = \frac{360^{\circ}}{12}$$
$$n = 30$$



16. 180(n-20) = 1440  $n-2 = \underline{1440} = 8$  180 n = 10Decagon

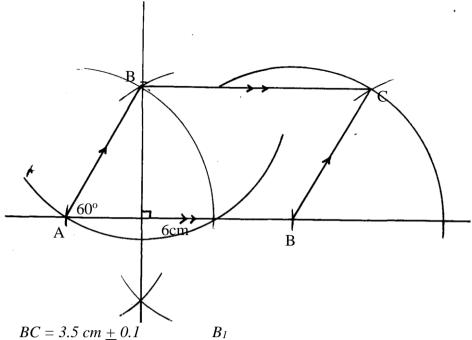
17. 
$$$\therefore 5x + 3x + x = 180^{\circ} < 's \text{ of } \Delta$   
 $9x = 180^{\circ}$   
 $X = 20^{\circ}$   
 $\therefore 5 \times 20 + y = 180$   
 $y = 180 - 120 = 60$$$

18. Let the interior  $\angle$  be x and exterior be y  $\therefore x + y = 180$   $+ \frac{x - y = 132}{2x}$  2x = 312 x = 156  $y = 180 - 156 = 24^{\circ}$ No. of sides  $(n) = 360^{\circ} = 15$  24 = 15 sides

## 17. Geometrical constructions

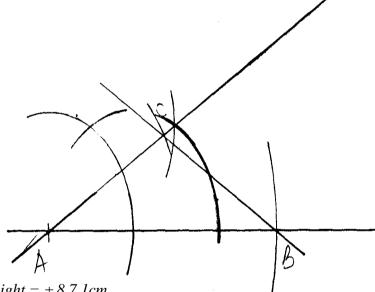
1. 
$$A = 120000 (1 + \frac{8}{100} x^{\frac{1}{4}})^{3}$$
$$120000 (1.02)^{3} = 127344.95$$





- 3.  $BC = 3.5 \ cm \pm 0.1$ 
  - construction of  $\angle CAB$ . B1
  - *B1* completion of triangle.

N/B/Arcs should be seen in order to award the above marks.

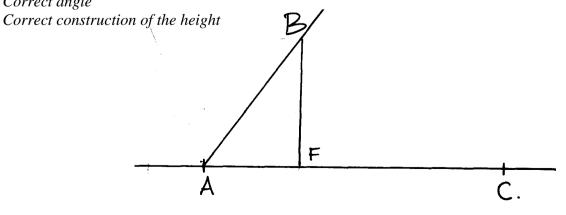


 $Height = \pm 8.7 \ 1cm$ 4.  $(\frac{1}{2} \times 7 \times 8.7) 30.45 \text{cm}^2$ 

2 ±1cm

Give 1m of correct and complete triangle 5.

Correct angle





Marked price = 
$$\frac{100}{90}$$
 x 450 = shs.500  
Cost =  $\frac{100}{25}$  x 450 = shs.360  
Profit =  $500 - 360$   
= shs. 140

# 18. Scale drawing

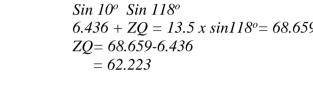
a) 
$$\underline{YZ}_{Sin\ 28^{o}} = \underline{13.5}_{sin\ 100^{o}}$$

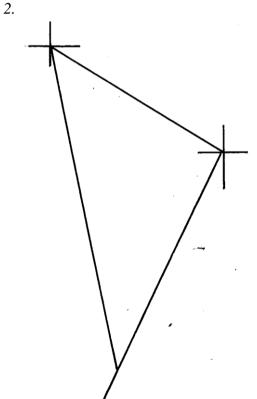
Duration of travel = 8:55a.m - 7.35a.m

=  ${}^{4}/_{3}$ 

Speed =  $\underline{6.436}_{{}^{4}/_{3}}$ 

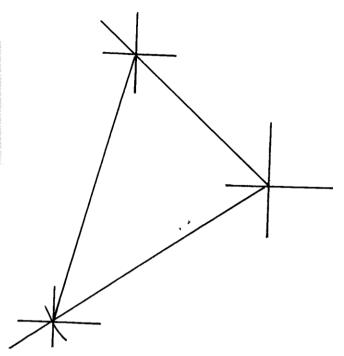
= 4.827km/hr



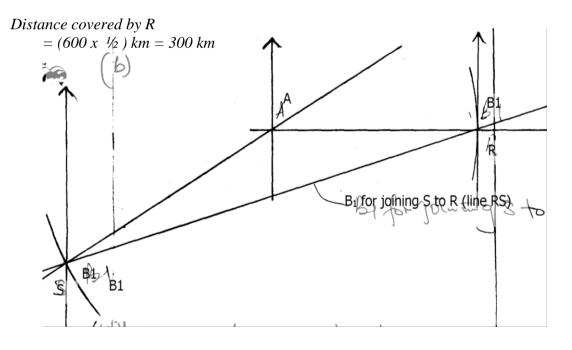


1cm rep 100km





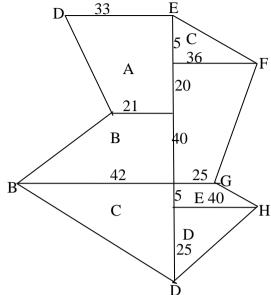
- *b*) *i*)  $049 \pm 1$
- *ii)*  $190 \pm 1$
- c)  $6.7 \pm 0.1$  $670 \pm 10$
- 3. a) (i) Distance covered by  $s = (750 \times \frac{1}{2}) \text{km} = 375 \text{ km}$



- (b) (i) Distance between the two aeroplanes =  $12.5 \times 50 = 625 \pm 5 \text{ km}$
- (ii) Speed =  $\left(\frac{625}{45} \times 60\right)$  km/hr

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## (c) (i) Bearing of S from $R = 225^{\circ}$ (ii) The bearing of R from $S = 72^{\circ}$



Area A: 
$$\frac{1}{2}$$
 x 25 (33 + 21) = 675  
Area B:  $\frac{1}{2}$  x 40 (21 x 42) = 1260

Area C: 
$$\frac{1}{2}$$
 x 30 x 42 = 630

Area D: 
$$\frac{1}{2}$$
 x 25 x 40 = 500

Area E: 
$$\frac{1}{2}$$
 x 5 (40 + 25) = 162.5

Area F: 
$$\frac{1}{2}$$
 X 60 (25 + 36) = 1830

Area G: 
$$\frac{1}{2}$$
 x 5 x 36 = 90  $\sqrt{\phantom{a}}$ 

$$= 5,147.5m^2$$

5. A to 
$$C = 96 \pm 1 \text{ km}$$
  
Bearing =  $300^{\circ}$ 

(i) 
$$62 \pm 1$$
km

#### 6. Graph

c) Average speed of the 
$$2^{nd}$$
 train  
Time taken =  $80 \div 1^{11}/_{12} = 80 \times 12$   
23  
=  $41.74$ km/h

7. 
$$L.S.F = \frac{4}{2000000} = \frac{1}{500000}$$
  
 $A.S.F = \frac{1}{5 \times 10^5} = \frac{1}{2.5 \times 10^{11}}$ 

Area of rectangle =  $(2.4 \times 1.5) \text{ cm}^2$ =  $3.6 \text{ cm}^2$ Actual area =  $3.6 \times 2.5 \times 10^{11} \text{ ha}$  $100 \times 10000$ =  $9 \times 10^5$ = 900,000 ha



a)  $\triangle ABD \ \sqrt{ly \ constructed}$  $\triangle ABP$ 

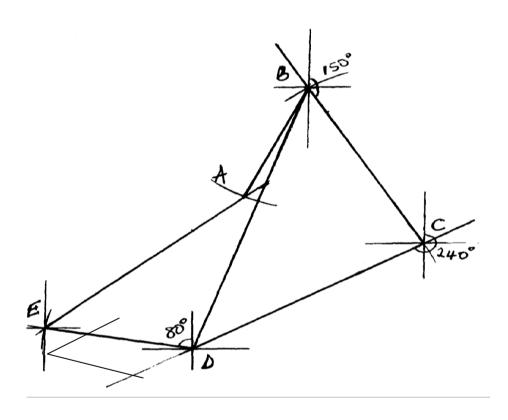
b) i) 
$$AD = 4.5 + 0.1cm$$
  
Distance  $A + D$   
=  $4.5 \times 10 = 45km$ 

ii) Bearing of (i) from B = 241 + 1

*iii) Bearing P from D* = 123 = 2

iv) 
$$Dp = 12.9 + 0.2$$
 am  
Distance  $D + P = 12.9 \times 10$   
 $= 129 \text{ km}$ 

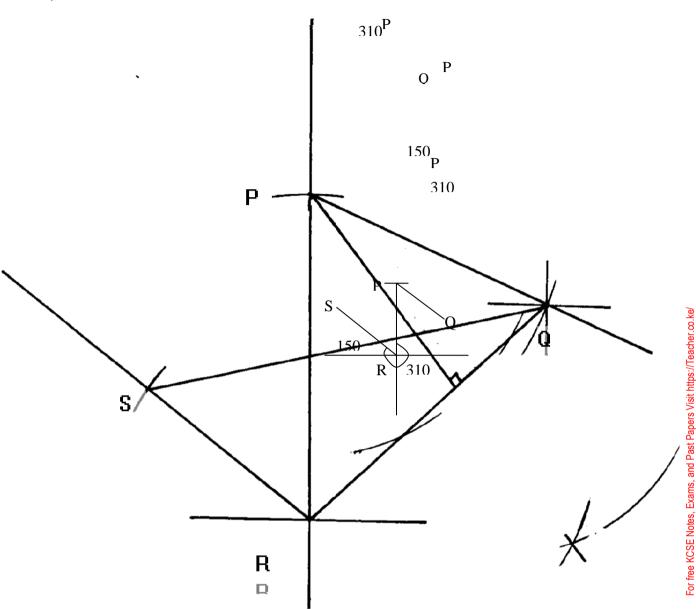
9. a)



b) i) 
$$6.8 + 0.1cm$$
  
Distance  $Ae = 340 + 5 km$ 

$$ii)$$
  $180 + 18 = 198 + 2$ 

10. a)



b) (i) 
$$SP = 7.8 \times 50 = 390 \text{ km} \pm 5 \text{ km}$$
  
(ii)  $S \& Q = 255^{\circ} \pm 1^{\circ}$   
(iii)  $4 \times 50 = 200 \text{ km} + 5 \text{ km}$ 

11. (a) Scale = 
$$50km$$
  
Drawing accurately25^{\circ}  
 $<$ NCT =  $145^{\circ}$   
 $<$ NTY =  $90^{\circ}$   
Lines drawn //

(b)By measurement:

(i) Distance 
$$SY = 6.9 \times 50 = 345 \pm 5 \text{km}$$

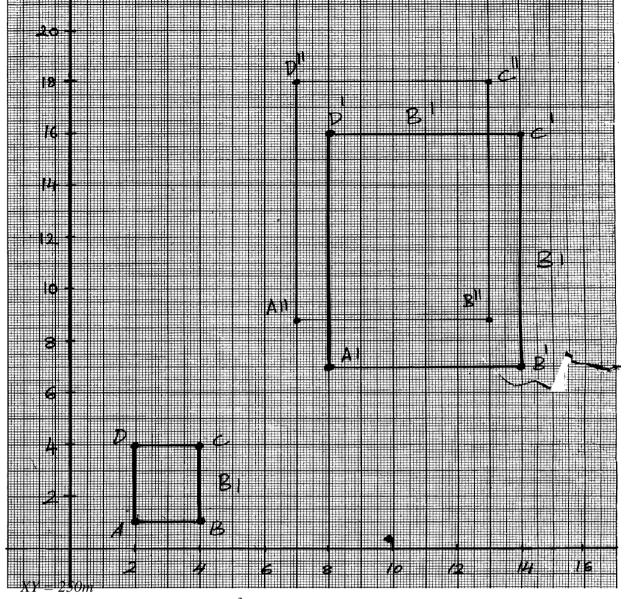
Bearing Y For  $S = 360^{\circ} - 114 = 246 \pm 1^{\circ}$ 

(ii) distance  $ST = 7.9 \times 50 = 39.5 \pm 5km$ 

(iii) distance  $YT = 9.8 \times 50 = 490 \text{ 5km}$ 







Area of  $A = \frac{1}{2} \times 50 \times 60 = 1500 \text{m}^2$ 

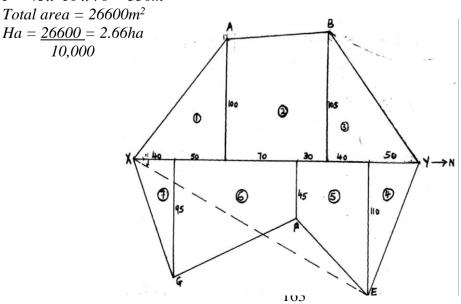
 $B = \frac{1}{2} \times 70 \times 60 = 2100 \text{m}^2$ 

 $C = \frac{1}{2}(60 + 80) \times 120 = 11050m^2$ 

 $D = \frac{1}{2} x 80 x 80 = 3200 m^2$ 

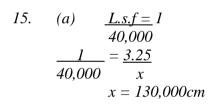
 $F = \frac{1}{2}x \ 10 \ x \ 70 = 350m^2$ 

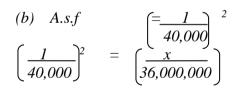
10,000



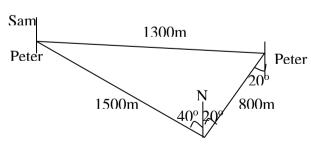
(b) Total area = area (1) + (2) + (3) + (4) + (5) + (6) + (7)  
Area (1) = 
$$\frac{1}{2}x$$
 90  $x$  100 = 4500 $m^2$   
(2) =  $(\underline{100 + 105})10 = 10250m^2$   
2  
(3) =  $\frac{1}{2}x$  90  $x$  105 = 4725 $m^2$   
(4) =  $\frac{1}{2}x$  50  $x$  110 = 2750 $m^2$   
(5) =  $\frac{1}{2}x$  (110 + 45)70 = 5425 $m^2$   
(6) =  $(\underline{45 + 95})$  120 8400 $m^2$   
2  
(7) =  $\frac{1}{2}x$  40  $x$  95 = 1900 $m^2$   
Total area = 37,950 $m^2$   
In hectares =  $(\underline{37950})$  ha = 3.795ha  
10.000

- (c) (i) bearing of E from x is  $0.25 \pm 1^{\circ}$ (ii) Distance  $Ex = (12.8 \ 0.1 \ x \ 20m) = 256 \pm 2m$
- 14. Area  $A = \frac{1}{2}x 170 x 80 = 6800$   $B = \frac{1}{2}x 80 x 80 = 3200$   $C = \frac{1}{2}x 10 x 70 = 350$   $D = \frac{1}{2}x 170 x 130 = 11050$   $E = \frac{1}{2}x 70 x 60 = 2100$ Total  $= 23,500 m^2$



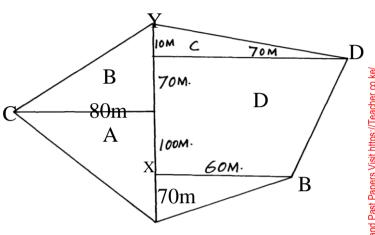


$$x = 0.0225cm^2$$



(a) bearing = 
$$180 + 20 = 200^{\circ}$$
 John

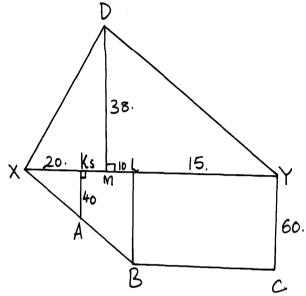
(b) 
$$a^2 = 1500 +$$
  
 $a^2 = b^2 + c^2 - 2bc \cos A$   
 $a^2 = 1500^2 + 800^2 - 2 \times 1500 \times 800\cos 60$   
 $= 2250000 + 640000 - 1200000$   
 $= 1690000$ 



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(c)  $\frac{1300}{\sin 60} = \frac{1500}{\sin 6}$   $\sin 60 \sin c$   $1300 \sin c = 1500 \sin 60$   $\sin 60$  1300 = 0.9993  $\therefore c = 87.79^{\circ}$  c = 87.80

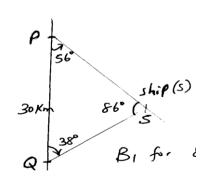
*17*.



A of 
$$\triangle XYD = \frac{1}{2}x50x38 = 950m^2$$
  
A of XBCY =  $\frac{1}{2}(50 + 15)60$   
=  $\frac{1}{2}x65x60$   
=  $1950m^2$   
Total A =  $(950 + 1950)m^2$   
=  $2900m^2$ 

18. 
$$B1 \text{ for } 86^{\circ}$$
  
 $30 = Q5$   
 $Sin 86^{\circ} Sin 56^{\circ}$   
 $QS = 30sin 56^{\circ}$   
 $Sin 86^{\circ}$   
 $= 24.93km$ 

19. 
$$1 cm for 100000 cm$$
  
 $1 cm^2 = (100000 cm)^2$   
 $A rea = 5.4 \times 4.5 \times 100000 \ cm^2$   
 $= \underbrace{5.4 \times 4.5 \times 100000 \times 100000 Km^2}_{100000 \times 100000}$   
 $= 24.3 km^2$ 



= 
$$8.1^{\circ}$$
  
Latitude of  $B = 8.1^{\circ} - 5^{\circ} N$   
=  $3.5^{\circ} S$ 



i) 
$$acc = \frac{40 - 20}{100 - 50}$$
  
=  $\frac{20}{50}$  = 0.4m/s

*ii)* 20 - 40 = -20460 – 400 60

$$= 0.3333 \text{ m/s}^2$$

$$= 0.3333 \text{ m/s}^2$$

70 *60* 

40

100

200 300 400 5

600

*23*.

iii) Area = 
$$\frac{1}{2}$$
 (520 + 300) x 40 x  $\frac{1}{1000}$  = 16.4 km

a) 
$$Tan \ 11.3 = \underline{200}$$
  
 $x$   
 $x = \underline{200}$   
 $Tan \ 11.3 = 100.1m$ 

*b*)

 $D = (10 \times 5) 50m$ 

$$Tan \theta = 7.590$$

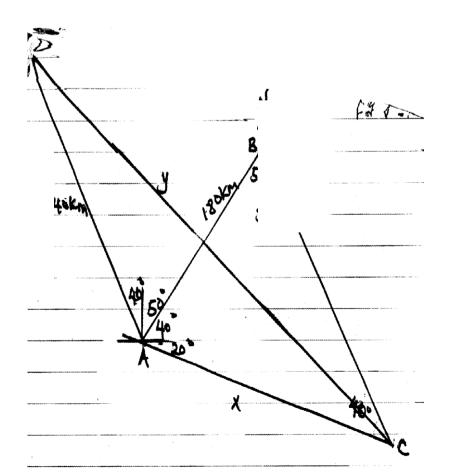
< of depression = 7.590

c) i) 
$$\sqrt{50.9^2 - 49.9^2} = 10.04$$
cm

*ii) Tan*  $\theta = 10.04$ 200

$$= 2.874^{\circ}$$

24. a) Make a sketch to show positive of A, B, C and D



For √ sketch

For  $\sqrt{exp. of x}$ 

For  $\sqrt{ans}$ .

For  $\sqrt{Sub}$ .

 $\sqrt{\cos 150}$ 

For taking sq. root.

For exp. of BC



Use sine rule in  $\triangle ABC$ 

$$\frac{X}{\sin 80^{\circ}} \quad \frac{180}{\sin 40^{\circ}} \Rightarrow x = \frac{180 \sin 80^{\circ}}{\sin 40^{\circ}}$$

$$= 275.8$$

$$Hence \quad AC = 276 \text{ km}$$

(b) Use the cosine rule in 
$$\triangle$$
 AD when  $\angle$ DAC = 150°  
 $y^2 = 240^2 + 276^2 - 2 \times 240 \times 276 \cos 150^\circ$   
 $= 576000 + 76180 - 132 480 (-\cos 30^\circ)$   
 $= 133776 + 114731 = 248507$ 

$$y = \sqrt{248507}$$
  
= 498.5  
Hence CD = 499 km

(c) Using sine rule in  $\triangle ABC$  we have

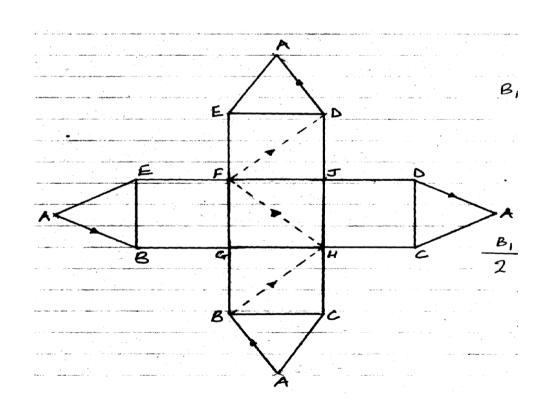
$$\frac{BC}{Sin} = \frac{180}{60^{\circ}}$$

$$\sin 40^{\circ}$$

$$BC = \frac{180 \sin 60}{\sin 40}$$
$$= 242.5$$
$$= 243 \text{ km}$$

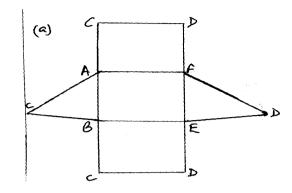
#### 19. Common solids

1. Sketch of the net of the solid (not free hand) base n\must be square, other lengths must be within. Labeling of all verticals with the path correctly shown. AB and DA may be shown one.



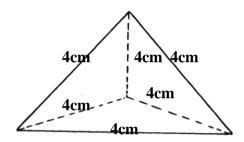


*(a)* 

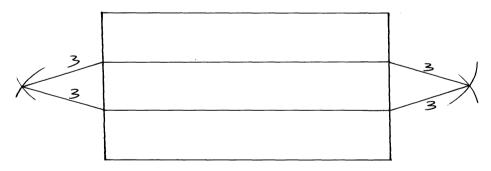


(b) Total surface area  
= 
$$2\sqrt{9 \times 3 \times 4 \times 2} + 10 (6 + 5 + 7)$$
  
=  $29.39 + 180 = 209.4 \text{cm}^2$ 

3.



4.



# 20. Indices

1. 
$$3^{4} x 3^{4x} + 3^{4x} = 246$$
$$3^{4x} (81 + 1) = 246$$
$$\frac{82}{82} x 3^{4x} = \frac{246}{82}$$
$$1$$
$$3^{4x} = 3^{1} \sqrt{4x} = 1$$



$$x = \frac{1}{4}$$

$$5^{2y} x5^{1} = 4^{(5y+1)} - 15$$

$$5^{y} x 5^{y} x 5^{1} = 4 x 5y x 51 - 15$$
Let  $5y = t$ 

$$5t^{2} = 20t - 15$$

$$t^{2} = 20t - 15$$

$$t^{2} - 4t + 3 = 0$$

$$(t-1) (t-3) = 0$$

$$t = 1 \text{ or } 3$$

$$5y = 1 = 5^{0}$$
Or  $5y = 3 \ y = \underline{\log 3}$ 

$$\log 5 = 0.6826$$

3.  $CBD = 90 - 42 = 48^{\circ}$ Angle of triangle add to  $180^{\circ}$   $DOB = 180^{\circ} - 42 = 138^{\circ}$ Opposite angles of cyclic quadrilateral add to  $180^{\circ}$ 

$$DAB = \underline{138}^o = 69^o$$

Angle at circumference is half the nagle substended at centre by same chord

CDA  

$$ABD = 90 - 48 = 42o$$
  
 $ADB = 180 - (69 + 42)$   
 $180 - 111 = 69^{\circ}$   
 $CDA = 90 + 69^{\circ}$  = 159°  
Show  $\triangle ADB$  is asoccesters  
 $\angle DAB = 69^{\circ}$   
 $\angle ADB = 69^{\circ}$   
 $\angle ABD = 42^{\circ}$ 

So two angles are equal hence it is asoccesters

4. 
$$25^{\frac{3}{4}} = (25^{\frac{1}{2}})^{\frac{3}{2}} = 5$$

$$0.9^{2} = (\frac{9}{10})^{2} = \frac{9^{2}}{100}$$

$$2^{2} = 2^{2}$$

$$(\sqrt{5})^{3} \times 9^{2} \times 2^{2}$$

$$(\sqrt{5})^{5} \times 10^{2} \times 3^{3}$$

$$\frac{3 \times 4}{(\sqrt{5})^{2} \times 10^{2}}$$

$$\frac{3}{5} \times 25 = \frac{3}{125}$$

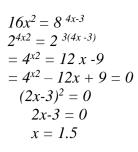
5. 
$$2^{x} = 0.0625 = \underline{625}$$

$$1000$$

$$2x = \underline{1} = 2^{-4}$$

$$16$$

$$\therefore x = -4$$







No 5.627	Log 0.7503
$(0.234)^3$	T. 3692
	$2.8579 \frac{x  3}{}$
8.237	0.4779 <u>0.9158</u>
2.399 x 10 <sup>-3</sup>	3.3800
	= 0.002399

7. 
$$9^{x+1} + 3^{2x+1} = 36$$
$$3^{2x+2} + 3^{2x+1} = 36$$
$$3^{2x}(9+3) = 36$$
$$3^{2x} = 3^{1}$$
$$2x = 1$$
$$x = \frac{1}{2}$$

8. (a) 
$$4p^2 - 3P - 10 = 0$$
  
(b)  $4p^2 - 8p + 5p = 0$   
 $(4p + 5) (p-2) = 0$   
 $p_1 = {}^{-5}/4, p = 2$   
When  $y = {}^{-5}/4,$   
 $4^{-y} = {}^{-5}/4$   
 $y = {}^{1}\log 4 (-5)$   
 $2$   
 $P = 2$   
 $4^{-y} = 2$   
 $2^{-2y} = 2^{1}$   
 $y = {}^{-1}/2$ 

9. 
$$\frac{1}{16^{x}} = \frac{1}{32}$$

$$\left(\frac{1}{2^{4x}}\right)^{x-\frac{1}{4}} = \frac{1}{2^{5}}$$

$$2^{-4x^{2}+x} + x = 2^{-5}$$

$$-4x^{2}+x+5=0$$

$$4x^{2}-x-5=0$$

$$4x^{2}-5x+4x-5=0$$

$$x(4x-5)+1(4x-5)=0$$

$$x=-1 \text{ or } x=\frac{5}{4}$$

J10. 
$$15 (ax)^4 (-2/x^2) = 4860$$
  
 $60a^4 = 4860$   
 $a^4 = 81$ 



# 21. Reciprocals 1. \_\_10\_\_1 \_\_\_-3 1

- 2.  $807 \rightarrow 0.001239$   $0.0591 \rightarrow 16.92$  5(0.001239) + 4(16.92)= 67.69
- 3.  ${}^{1/_{3}} \{ 2 \times 1.5065 + 5 \times 1.2004 \}$  ${}^{1/_{3}} (3.013 + 6.002) (0.3333)$  $= 9.015 \times 0.3333$ = 3.005 (3 dp)
- 4.  $\frac{12 \times 0.25 12.4 \div 0.4 \times 3}{\frac{1}{8} \text{ of } 2.56 + 8.68}$   $\frac{3 31 \times 3}{0.32 + 8.68}$   $\frac{-90}{9}$  = -10
- $\frac{4}{(8.68)^3} + \frac{5}{34.46} \\
  \frac{4}{653.97} + (0.1451)^{1/3} \\
  4(0.1529) + 0.5255 \\
  0.6116 + 0.5255 = 1.1371$
- 7. 3.5932 = 12.91  $\Rightarrow \left(\frac{1}{1.291 \times 10}\right) + 2 \left(\frac{1}{5.26 \times 10^{-1}}\right)$   $= (0.7746 \times 10^{-1}) + 290.1901 \times 10)$  = 0.07746  $+ \frac{3.802}{3.87946}$  3.87946

$$= 1.9695$$

$$= 1.970(4s.f)$$
No s.f rec
$$0.6638 6.638 x 10^{-1} 0.1500 x 10 = 1.5000$$

$$0.833 8.33 x 10^{-1} 0.1200 x 10 = 1.200$$

$$= \frac{1}{3} (2 (105) + (1.2))$$

$$= \frac{1}{3} (3 + 6)$$

$$= \frac{1}{3} x 9 = 3$$

9. 
$$3x1.485 + 13x6.410$$
  
=  $4.455 + 83.33$   
=  $87.785$ 

ALT
$$\frac{30}{6.735} + \frac{130}{1.56} = 30 \times 0.1485 + 130 \times 0.641$$
 $= 4.455 + 83.33$ 
 $= 87.785$ 

## 22. Common logarithms.

0.3178

All logs read correctly

Correct Addn /subst. of logs.

2. 
$$Log y = log B + n log x$$
  
 $n log x = log y - log B$   
 $n = \underline{Log} (\frac{y}{B})$   
 $Log x$ 

3. 
$$= 6 \log_2 4 + 10 \log_3 3$$
$$= 12 \log_2 2 + 10 \log_3 3$$
$$= 12 + 10$$

$$4. \qquad Log \ \frac{2x - 11}{2} = \frac{\log 3}{x}$$

$$(2x-11) = \frac{3}{x}$$
  
 $2x^2 - 11x - 6 = 0$   
 $(2x + 1)(x - 6) = 0$ 

x	=	- 1/2	or 6
x	=	6	

No.	Log
0.5241	T.7194
$(0.5241)^2$	T.7194x2
	<u>T.4388</u> +
83.59	1.9222
	1.3610
0.3563	T.5518
$3\sqrt{0.3563}$	$(3+2.5518) \div 3$
	T.8506
	0.3610 -
	1.8506
$3.239x10^{1}$	1.5104
= 32.4	

7. 
$$H^{3} = \frac{3d(L-d)}{10L}$$

$$3dL - 10H^{3}L = 3d^{2}$$

$$L(3d - 10H^{3}) 3d^{2}$$

$$L = \frac{3d^{2}}{3d - 10H^{3}}$$

8. No. Log
6.195 0.7920
11.82 
$$\underline{1.0726}$$
1.8646
83.52  $\underline{1.9218}$ 
 $\overline{1.9428 \times \frac{1}{4}}$ 
4. + 3.9428
0.9676  $\overline{1.9857}$ 

9. 
$$\log y^2(x-1) = \log 9 \ y^2(x-1) = 9 \ \dots (1)$$
  
 $\log (xy) \log 6 \ xy = 6 \dots 2$   
 $from (2) x = \frac{6}{y}$   
 $substitute in (1) y(6-1) = 9$ 

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$$6y - y^{2} = 9$$

$$y^{2} - 6y + 9 = 0$$

$$(y-3)^{2} = 0$$

$$y = 3$$

$$\therefore x = 2$$

5
10.  $\frac{4}{5} \log_{10} 25 + \log_{10} 25x2 - \log 10}{4 \log 2 = \log_{10} 25x2 - 3\log 2}$   $2 \log 10 + 2 \log 5$   $\log 10 \times 100$ 

11.

NO	LOG
0.9895 (0.9895) <sup>2</sup>	1.9954 1.9954 x 2 1.9908
0.004974	3.6968 3.6876÷4
6.598	1.4219 x 3 2.2657 0.8195 –
3.579 X10 <sup>2</sup>	2.2657 2.5538

Use sine rule

12. 
$$\log 3x + 8 - \log 8 = \log (x-4)$$
  
 $\log (3x + 8) = \log (x-4)$   
 $8$   
 $3x + 8 = x - 4$   
 $3x + 8 = 8x - 32$   
 $5x = 40$ 

*13*.

No.	Log
36.72	1.5649
$0.46^2 \longrightarrow$	2(T.6628)
	<u>T.3256</u>
185.4	0.8905
	<u>2.2682</u>
	$2.9223 \times 1 = 3 + 1.6223$
3.474 x 10 <sup>-1</sup>	3 3 3
Or 0.3474	1.5408

14. No

Sin 44.5		1.8457
Tan 14.9	1.4250	2.5686
Cos 82	1.1486 +	
	<u>_1</u>	<u>.2772</u>
		2
10 x 4.351		0.6386



	10 x 4.351	0.63
5.	From square roots 12.25	= 3.5
	3.264 x 1.215 x 3.5 x 107	
	1.088 x 0.4725 x 107	
	2261 x 1215 x25	

$$\sqrt{27} = 3$$

16. 
$$Log_8(x+5) - log_8(x-3) = Log_8 4$$
  
 $Log_8(x+5) = log_8 4$   
 $x-3$   
 $\frac{x+5}{x-3} = 4$   
 $4x-12 = x+5$ 

$$3x = 17$$
$$x = 17 = 5^2/3$$

Or 
$$\log 8 \frac{x+5}{x-3} = \frac{2}{3}$$
  
 $8^{2}/3 = \frac{x+5}{x-3}$   
 $2^{3}(^{2}/_{3}) = \frac{x+5}{x-3}$   
 $2^{2} = \frac{x+5}{x-3} \Rightarrow 4 = \frac{x+5}{x-3}$   
 $4x-12 = x+5 \Rightarrow 3x = 17$   
 $x = \frac{17}{3} = 5^{2}/_{3}$ 



No 6.57 <sup>2</sup>	Log 0.8176 2x
$4.317 \times 10^{1} $ $43.17 + 6.57$	1.6352
49.74 (7.92) <sup>2</sup>	1.6967 0.8987
30.08 2.636 X 10 <sup>-2</sup>	$ \begin{array}{rcl}                                     $
No 6.57 <sup>2</sup>	Log 0.8176
$4.317 \times 10^{1} $ $43.17 + 6.57$	$\frac{2x}{1.6352}$
49.74 (7.92) <sup>2</sup>	1.6967 0.8987 X2
30.08 2.636 X 10 <sup>-2</sup>	$ \begin{array}{rcl}  & 1.7974 \\ 1.4783 & + & 3.2757 \\ & & 2.4210 \\ & = 0.02636 \\ & = 0.0264 (4 d.p) \end{array} $

18. 
$$Log 120 = log 4 + log 3 + log 10$$
  
=  $log 22 + log 3 + log 10$   
=  $2log 2 + log 3 + log 10$   
=  $2(0.30103) + 0.47712 + 1$   
=  $2.07918$ 

19. 
$$Log_{2}(3x-4) = \frac{1}{3} lo_{2} 8x^{6} - log_{2} 4$$

$$Log_{2}(3x-4) = log_{2}(2^{3}x^{6}) - log_{2} 4$$

$$Log_{2}(3x-4) = log_{2} 2x^{2} - log_{2} 4$$

$$Log_{2}(3x-4) - log_{2} \left(\frac{2x^{2}}{4}\right)$$

$$= 3x - 4 = \underline{2}x^{2}$$

$$4$$

$$2x^{2} - 12x + 16 = 0$$

$$x^{2} - 6x + 8 = 0$$

$$x-2x-4x+8=0$$
(x-2) (x-4) = 0
$$x = 2 \text{ or } x = 4$$

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No	Log
5.627	0.7503
$(0.234)^3$	T. 3692
	$2.8579 \frac{x 3}{}$
8.237	0.4779 <u>0.9158</u>
$2.399 \times 10^{-3}$	3.3800
	= 0.002399

21. Det 2 - -3 = 5  
Area of 
$$A^{I}B^{I}C^{I} = 5 \times 15$$
  
= 75 cm<sup>2</sup>

22. 
$$Log 10(6x-2) - log 10 = log 10(x-3)$$
  
 $Log (6x-2) = log (x-3)$   
 $10$   
 $6x-2 = x-3$   
 $10$   
 $6x-2 = 10x-30$   
 $x = 7$ 

23. No. Log 
$$0.07526^2$$
  $2.8766 \times 2 = 3.7532$   $6.652$   $0.8230 = 0.8230$   $4.9302$ 

$$\frac{4.9302}{3} = 6 + \frac{2.9302}{3}$$

$$= 2.9767$$
Antilog = 9.4776 x 10<sup>-2</sup>

$$= 0.094776(accept 0.09478)$$

No.	Log
4.283	<u>0.</u> 6317
$0.009478^2$	3.9767 X 2 +
	<u>5</u> . 9534
	<u>4.</u> 5851 -
Log 9.814	1.9964

$$2.0785 \times 10^{-1} - 1.3177$$

$$= 0.20785$$

# 23. Equations of straight lines

1. a) Length of diagonal = 
$$\sqrt{10^2 + 8^2}$$
  
=  $\sqrt{164}$ 

Vertical height = 
$$\sqrt{16^2 - (\sqrt{164})^2}$$
  

$$2 = 14.66cm$$

b) Height of the slant surfaces 
$$\sqrt{16^2 - 4^2} = \sqrt{240}$$
  $\sqrt{16^2 - 5^2} = \sqrt{231}$  Area of slant surfaces  $(\frac{1}{2}x \ 8x \ \sqrt{240} \ x \ 2) = 124.0 \ cm^2$   $(\frac{1}{2}x \ 10x \ \sqrt{231} \ x \ 2) = 152.0 cm^2$  Area of the rectangular base=  $8x \ 10 = 80 cm^2$  Total surface area =  $356 cm^2$ 

c) Volume  
= 
$$(\frac{1}{3} \times 80 \times 14.66) = 391.0 \text{cm}^3$$

2. Gradient of line 
$$AB = 3 - 3k$$
 $K + 1$ 

Equation of other line can be written as

$$Y = -\frac{3x}{2} + \frac{9}{2}$$

 $\therefore$  its gradient = -3/2

Hence 
$$\frac{3-3k}{K+1} = -\frac{3}{2}$$

$$6-6K = -3k-3$$
  
 $-3K = -9$   
 $K = 3$   
 $A(-1, 9), B(3,3)$ 

3. 
$$M_{1} = 2x - 3x^{2}$$

$$M_{2} = 1 - 2ax$$

$$M_{1} = M_{2} \text{ at } x = \frac{1}{3}$$

$$2x - 3x^{2} = 11 - 2ax$$

$$\frac{2}{3} - 3(\frac{1}{3})^{2} = 1 - 2ax^{1/3}$$

$$\frac{2}{3} - \frac{1}{3} = 1 - \frac{2}{3} a$$

$$\frac{3}{2} = -\frac{2}{3}a$$

$$\frac{9}{4} = a$$

4. 
$$M1 = \frac{5-1}{4-2} = \frac{4}{6} = \frac{2}{3}$$

$$M2 = \frac{-3}{2}$$
  
i.e.  $\frac{-3}{2} = \frac{y-5}{x-4}$ 



$$2 (y-5) = -3 (x-4)$$
  

$$2y-10 - -3x + 12$$
  

$$3x + 2y - 22$$

- 5. Points (3, 0) and (-5, 2)  $M = -\frac{1}{4}$   $y - 0 = -\frac{1}{4}$  x - 3  $y = -\frac{1}{4}x + \frac{3}{4}$
- 7.  $Grad = \frac{2}{3}$   $\frac{y-4}{x+2} = \frac{2}{3}$   $y = \frac{2x}{3} + \frac{16}{3}$ 
  - 8. 3y 5x = 4 Or equivalence

$$5y = 3x - 10$$

$$y = 3x - 2$$

$$5$$

$$Cradient = -5$$

$$3$$

$$5 = y - 3$$

$$x + 1$$

$$3y - 9 = 5x - 5$$

$$L.S.F = 4 = 1$$

$$2000000$$

$$A.S.F = 1$$

$$5x 10^{5}$$

$$2.5 x 10^{11}$$

Area of rectangle = 
$$(2.4 \times 1.5) \text{ cm}^2$$
  
=  $3.6 \text{ cm}^2$   
Actual area =  $3.6 \times 2.5 \times 10^{11} \text{ ha}$   
 $100 \times 10000$   
=  $9 \times 10^5$   
=  $900,000 \text{ha}$ 

10. 
$$2y - 5x = 11$$

$$Y = \frac{5}{2}x + \frac{11}{2}$$

$$g = \frac{5}{2}$$

$$\frac{5}{2}m = -1$$

$$M = \frac{-2}{5}$$

$$\frac{Y - 4}{X + 4} = \frac{-2}{5}$$

$$5y + 2x = 14$$

$$P(x, o)$$

$$5 X o + 2x = 14$$

11.

$$X = 7$$
  
 $Q(o, y)$   
 $5y + 2Xo = 14$   
 $Y = 2.8$   
 $P(7,0)$   
 $Q(0, 2.8)$ 

i) 
$$K(3-7, 4+2)$$
 (-2, 3)  
 $2$   $2$   
 $P(3+1, 4-2)$  = (2,1)

*ii*) 
$$K_1 = \frac{3-1}{2-2} = -\frac{1}{2}$$
  
= 2

12. Gradient of 
$$L1 = \frac{1}{5}$$
  
Gradient of  $L2 = -5$   
 $Y = mx + c$   
 $2 = -5 (1) t c$   
 $2 = -5tc$   
 $C = 7$   
Epuding  $L2$   
 $Y = -5x + 7$ 

13. 
$$3y - 5x = 4 \text{ Or equivalence}$$

$$5y = 3x - 10$$

$$y = \frac{3}{5}x - 2$$

$$\therefore Gradient = \frac{-5}{3}$$

$$5 = \frac{y - 3}{x + 1}$$

$$3y - 9 = 5x - 5$$

14. Gradient = 
$$g = \frac{m-1}{4-2} = \frac{m-1}{2}$$
  
 $3y = 5-2x$   
 $y = \frac{5}{3} - \frac{2x}{3}$   $g_1 = \frac{-2}{3}$   
 $g \times g = \frac{m-1}{2} = \frac{-2}{3}$   
 $g(m-1) = -6$   
 $g(m-1) = -6$ 

15. 
$$L_1 y = -\frac{2}{3} x - \frac{4}{3}$$
 $M_1 = -\frac{2}{3}$ 

$$M_2 = \underline{3}$$

$$L_2 \quad y = \underline{3} x + c \quad x = 1, y = 1$$

$$2$$

$$1 = \underline{3} + c$$

$$2$$

$$c = -\frac{1}{2}$$

$$L_2 \quad y = \underbrace{3}_2 x - \underbrace{1}_2$$

16. BP = shs. 
$$\frac{144}{6}x$$
 100

SP = shs.  $\frac{140}{6}x$   $\frac{144}{6}x$  100

100  $\frac{1}{6}$ 

Let pineapples sold at shs. 72 for every shs. 3 be  $x$ 

At shs. 60 for every 2 will be  $144 - x$ 
 $\frac{x}{3}$   $x$  72 +  $\frac{144 - x}{3}$  = 3360

 $\frac{24x + 30(144 - x) = 3360}{6}$ 
 $x = 60$ 

17. 
$$\frac{x+2-x-1}{3} = \frac{5}{2}$$

$$2(x+2) - 3(x-1) = 30$$

$$22x + 4 - 3x + 3 = 30$$

$$-x + 7 = 30$$

$$-x = 23$$

$$x = -23$$

### 24. Reflection and congruence

- 1. (a) Dist. traveled in 3hrs s. drawing Plane  $A 400 \times 3 = 1200 \text{km} \text{cm}$  Plane  $B 500 \times 3 7.5 \text{cm}$  Plane  $C 300 \times 3 = 900 \text{km} 4.5 \text{cm}$ 
  - (b) Dist.  $BA = 12.8 \ 0.1 \ x \ 200 = 2560 km \ 20 km$   $T = \underline{D} = 2560 \ hrs$  S = 500  $= 5.12 hrs \ of 5 hrs, 7.2 mns$   $\approx 5 hrs, 7 min \ (nearest \ min)$

(c) Bearing of B from 
$$C = 360^{\circ} - 20^{\circ} = 340^{\circ}$$
  
Dist.  $BC = (10.9 \pm 0.1 \text{ x } 200)\text{km}$   
 $= 2180\text{km} \pm 20\text{km}$ 

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#### 25. Rotation

 $V.S.F = 3^3 : 5^3 = 27 : 125$ Volume of larger tank =  $8.1 \times 125$ =  $37.5m^3$ 

#### 26. Similarities and enlargement

1.  $E.S.F = \frac{4 - x}{0 - x} = 3$  4 - x = -3x 2x = -4 x = -2  $6 - y = 3 \longrightarrow 6 - y = 6 - 3y$  2 - y -2y = 0 y = 0 Centre of enlargement = (-2, 0)

2. a) L.S.F = 1:500  
Height in 
$$cm = (500 \text{ x 5}) = 2500cm$$
  
 $\therefore$  Height in  $m = \frac{2500}{100} = 25m$ 

b) A.S.F = 1:250000  
= 1:25 (in 
$$m^2$$
)  
:: if  $25 = 36$   
=  $({}^{36}/_{25})m^2$  = 1.44 $m^2$ 

c) V.S.F = 1:500  
1:125
$$m^3$$
  
Corresponding volume  
=  $(^{125}/_{120})m^3$   
= 1.042  $m^3$  = 10420 $cm^3$ 

3. Let 
$$DE = x cm$$
  

$$\therefore AD = 3 + x$$

$$3 + x = 9$$

$$x = 4$$

$$12 + 4x = 9x$$

$$x = 2.4 \text{ cm}$$

$$DE = 2.4$$

4. 
$$L.S.F = \underline{12} = \underline{3}$$
  
 $8$   $2$   
 $A.S.F = \underline{9} = \underline{336}$   
 $4$   $x$   
 $x = 149^{1}/3cm^{2}$ 

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Area of QRTS = 
$$336 - 149^{1/3}$$
  
=  $186^{2/3}$ cm<sup>2</sup>

(a) 
$$\frac{4}{3} = \frac{64}{3}$$
  
 $x = 48cm$   
(b)  $\frac{3}{4} = \frac{810}{9}$   
 $\frac{27}{64} = \frac{810}{9}$   
 $\frac{27}{9} = 810 \times 64$ 

6.  $\triangle ABC$  is similar to  $\triangle ADE$ 

y = 1920grams

DE = 
$$\frac{7}{4}$$

DE =  $(\frac{7x8}{4})cm$ 

=  $14cm$ 
=  $e^{-7/23}$ 

7. Area scale factor = 12: 108

Linear scale factor =  $\sqrt{1}$ :  $\sqrt{9}$ 

$$= 1 : 3$$

*Volume scale factor* =  $1^3$  :  $3^3$ 

$$= 1:27$$

*Volume of the smaller cone* =  $810cm^3 \times 1$ 

$$=30cm^2$$

8. 
$$\frac{1}{2}h(a+b) = Area \ of \ trap.$$

$$\frac{1}{2}x^{3}(DC+4) = 15.6$$

$$DC + 4 = 15.6 \times 2$$

$$DC = 6.4$$

$$\frac{DC}{BE} = \frac{DA}{EA}$$

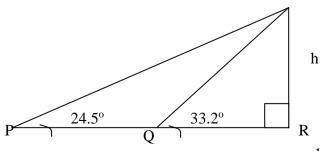
$$\frac{3+x}{x} = \frac{6.4}{4}$$

$$12 + 4x = 6.4 \text{ x } \sqrt{2.4x} = 12 \text{ } \sqrt{x}$$

$$x = 5cm$$

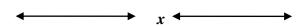
# 27. The Pythagoras theorem

1.



1.

2.





*From*  $\triangle$  *PTR*,  $tan\ 24.5^{\circ} = \frac{h}{x} \underline{\qquad} x \underline{\qquad} \frac{h}{tan\ 24.5^{\circ}}$ 

From 
$$\triangle QTR$$
,  $\tan 33.2^{\circ} = \frac{h}{x-5} \underline{\qquad} x = \frac{h}{\tan 33.2^{\circ}} + 5$   
 $\therefore \frac{h}{\tan 24.5^{\circ}} = \frac{h}{\tan 33.2^{\circ}} + 5 \underline{\qquad} \frac{\circ h}{\tan 24.5^{\circ}} - \frac{h}{\tan 33.2^{\circ}} = 5$   
 $h [\frac{1}{0.4557} - \frac{1}{0.6544}] = 5$   
 $h = (2.194 - 1.528) = 5$   
 $h = \frac{5}{0.666} = 7.508$   
 $\therefore height = 7.5m$ 

2. 
$$L.S.F = \frac{2}{3}$$

$$V.S.F. = \left(\frac{2}{3}\right) = \frac{8}{27}$$

$$Ratio = 8 : 27$$

# 28. The trigometric ratio 1

Tan 
$$30^{\circ} = \underline{x} \quad x$$
  
 $100 + y$   
 $x = (100 + y) \tan 30^{\circ}$   
 $(100 + y) \tan 30^{\circ} = y \tan 60^{\circ}$   
Tan  $60^{\circ} = \underline{x} = x = y \tan 60^{\circ}$   
 $(100 + y) 0.5774 = 1.1732y$   
 $57.74 = 1.155y$   
 $y = \underline{57.74}$   
 $1.155$   
 $y = 49.99 = 50m$   
 $\therefore x = 50 \tan 60$   
 $x = 86.6m$ 

$$\theta$$
= 44.43°, 135.57°

3. (a) (i) Area of triangle  $A^{1}B^{1}C^{1} = \frac{1}{2} \times 4 \times 4$ 

Sin  $\theta$ = 0.70

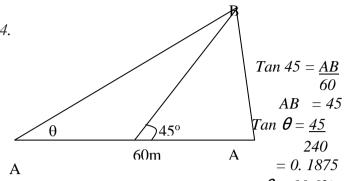
$$= 8 \text{ sq. units}$$
(b) (ii) Reflection in the line  $y = x$ 
(c) combine transformation =  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix}$ 

$$\begin{pmatrix} 0 & 2 \\ 2 & 0 \end{pmatrix}$$

$$De\begin{pmatrix} 0 & 2 \\ 2 & 0 \end{pmatrix} 0 - 2 \times 2 = -4$$

Inverse transformation =  $-\frac{1}{4}\begin{pmatrix} 0 & 2 \\ 2 & 0 \end{pmatrix} = \begin{pmatrix} 0 & -\frac{1}{2} \\ -\frac{1}{2} & 0 \end{pmatrix}$ 





 $\theta = 10.62^{\circ}$ 33 E 5. 5 C 36 A 20 21 В 40 42 25 E 40  $\mathbf{C}$ D 25

> Area A:  $\frac{1}{2}x 25 (33 + 21) = 675$ Area B:  $\frac{1}{2}x 40 (21 x 42) = 1260$

Area C:  $\frac{1}{2}$  x 30 x 42 = 630

Area D:  $\frac{1}{2}$  x 25 x 40 = 500

Area E:  $\frac{1}{2}$  x 5 (40 + 25) = 162.5

Area F:  $\frac{1}{2}$  X 60 (25 + 36) = 1830

Area G:  $\frac{1}{2}$  x 5 x 36 = 90  $\sqrt{\phantom{a}}$ 

 $= 5,147.5m^2$ 

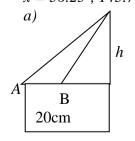
6. : Philip takes 10 days.

 $2Cos\ 2x = 0.600$  $Cos\ 2x = 0.3000$ 

 $2x = 72.5^{\circ}, 287.5^{\circ}$ 

 $x = 36.25^{\circ}, 143.75$ 

*7*.



 $a32 = \underline{h}$  20 + xTeacher.co.ke

Tan32 = h 20 + x  $h = (20 + x) tan32^\circ = 12.498 + 0.6249x$   $tan 40^\circ = {}^h/_x$   $h = x tan 40^\circ = 0.8391x$  0.8391x = 12.498 + 0.6249x 0.8391x - 0.6249x = 12.498 0.2142x = 12.498 x = 12.498 = 58.35m 0.2142  $\therefore$  The distance of A from the house = (20 + 58.35)m = 78.35

b) 
$$h = x \tan 40^\circ = 58.35 \times 0.8391 = 48.96m$$
  
.: The total height of the house  
 $= 1.82m + 48.96m = 50.78m$ 

11. 
$$tan 32^{\circ}c = \underline{h}$$

$$20 + x$$

$$h = (20 + x) tan 32^{\circ}$$

$$tan 40^{\circ} = \underline{h}$$

$$x$$

$$h = tan 40^{\circ}$$

$$\therefore x \tan 40^{\circ} = (20 + x) \tan 32^{\circ}$$

$$0.8391x = (20 + x) 0.6249$$

$$0.8391x = 12.498 + 0.6249x$$

$$0.8391x - 0.6249x = 12.498$$

$$x = 58.35m$$

$$20 + 58.35 = 78.35m$$

(b) The height of the house 
$$Tan \ 40^{\circ} = \underline{h} = h = 58.35 \ tan \ 40^{\circ} \ 58.35$$

$$h = 58.35 \ x \ 0.8391$$

$$h = 48.96 + 1.82$$

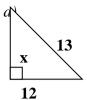
$$h = 50.78$$

12. 
$$\underline{24} = 2R \Rightarrow R = 16.15 \text{ cm}$$

$$Sin 48$$

$$Area = 3.14 \times 16.15^2$$
$$= 819.26 \text{ cm}^2$$

13.



$$Hyp = \sqrt{5^2 + 12^2}$$
$$= 13$$

$$cos x = {}^{12}/_{13}$$
(b) Sin2990-x)
$$= ({}^{12}/_{13})^2 = {}^{144}/_{169}$$

]14.

Tan 
$$\theta = \frac{8}{15}$$
 C  
 $\theta = \frac{17}{17}$ 
 $\theta = \frac{17}{15}$ 
 $\theta = \frac{15}{15}$ 
 $\theta = \frac{8}{15}$ 
 $\theta = \frac{8}{15}$ 
 $\theta = \frac{8}{15}$ 
 $\theta = \frac{8}{15}$ 
 $\theta = \frac{8}{17}$ 
 $\theta = \frac{15}{17}$ 
 $\theta = \frac{1$ 

29. Area of a triangle

1. a) 
$$BC^2 = 50^2 + 80^2 - 2 \times 50 \times 80 \cos 30$$
  
 $= 2500 + 6400 - 6928.20 = 1971.8$   
 $\therefore BC = \sqrt{1971.8}$   
 $= 44.40m$   
 $= 44m$   
b) Area of the plot  
 $= \frac{1}{2} \times 50 \times 80 \times \sin 30 = 1000m^2$   
 $= (1000) \text{ ha}$   
 $= 10000$   
 $= 0.01\text{ ha}$ 

30. Area of polygons

1. 
$$\frac{180(n-2)}{180(n-1-2)} = \frac{4}{3}$$

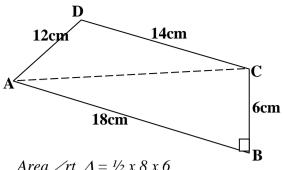
$$540n - 1080 = 720n - 2160$$

$$720n - 540n - 2160 - 1080$$

$$180n = 1080$$

$$n = 6$$
Area of hexagon = 6 (½ x 10 x sin 60)
$$= 6 x 43.30 = 259.81 \text{ cm}^2$$





Area 
$$\angle rt$$
  $\Delta = \frac{1}{2}x 8x 6$   
 $S = \frac{12 + 14 + 10}{2}$   
 $A = 18(18-12)(18-14)(18-10)$   
 $= 18x6x 4x 8$   
 $= 3456$   
 $= 58.79$   
Total area =  $24 + 58.79 = 82.79$ 

## 31. Area of part of a circle

1. (a) 
$$A = \frac{120}{360}x \pi x \frac{10^2 - \frac{1}{2}x}{100} x \frac{100}{100} x \frac{100}{100}$$
  
= 104. 72 - 43.30 = 61.42m<sup>2</sup>

(b) (ii) 
$$\underline{120} \times 2 \times 10 \times 20$$
  
 $\underline{360}$   
=  $418.9m^2$ 

(b) Total area = 
$$61.42 + 61.42 + 418.9$$
  
=  $541.74m^2$   
 $Cost = 541.74 \times 310 = 167,939$ 

2. a) 
$$Cos 54^{\circ} = \frac{x}{10}$$
  
 $X = 5.878$   
 $\therefore size = 2 \times 5.878 = 11.756$   
Area of  $\Delta = \frac{1}{2} \times 10^{2} \sin 72^{\circ} = 47.55$   
Total area of  $\Delta s = 47.55 \times 5 = 237.8 cm2$ 

b) Area of circle = 
$$\frac{22}{7} \times 10 \times 10 = 314.8$$

Shaded region = 
$$\frac{3}{5}$$
 (3.143 – 237.8)  
=  $45.9$ cm<sup>2</sup>

3. (a) 
$$7.8^2 = 6.6^2 + 5.9^2 - 2 \times 6.6 \times 5.9 \cos R$$
  

$$Cos R = \frac{6.6^2 + 5.9^2 - 7.8^2}{2 \times 6.6 \times 5.9}$$

$$= \frac{78.37 - 60.84}{77.88}$$

$$= 0.2251$$

$$\angle R = 77^\circ$$

$$\frac{7.8}{Sin 77} = 2r$$

$$r = \frac{7.8}{2 \sin 77}$$
$$= 4 cm$$

(b) 
$$\underline{5.9} = \underline{7.8}$$
  
 $Sin p Sin 77$   
 $Sin P = \underline{5.9 sin 77}$   
 $7.8$   
 $= 0.7370$   
 $\angle P = 47.5^{\circ}$   
 $\angle Q = 180 - (77 + 47.5) = 55.5^{\circ}$ 

(c) Area of shaded region  
= 
$$3.142 \times 4^2 - \frac{1}{2} \times 6.6 \times 5.9 \sin 77$$
  
=  $50.27 - 18.97 = 31.30$ 

4. 
$$(60/360 \times 22/7 \times 24 \times 24) - (60/360 \times 22/7 \times 12 \times 12)$$
$$301.71 - 75.43 = 226.26$$

## 32. Surface area of solids

B
$$x = 4$$
 $x + 6 = 6$ 
 $6x = 4x + 24$ 
 $x = 12 \text{ cm}$ 
 $L = \sqrt{12^2 + 4^2}$ 
 $= \sqrt{160}$ 
 $= 12.65 (2 d.p)$ 
 $L = \sqrt{18^2 + 6^2}$ 
 $\sqrt{360}$ 

= 18.97

 $= 3.142 (6 \times 18.97 - 4 \times 12.65)$ 

 $SA = \pi (RL - rL)$ 



(b) Cost of material for one lamp shape = <u>198.64</u> x 800 10000 = Sh15.90 Cost of 10 lamp shape = 2 x 10 x 15.90 = sh 318

2. Area of the remaining cross-section

- $=4.22 \times \pi$
- $= (17.64\pi)cm^2$

Area of the curved surface

- $= (8.4\pi x 150)$
- $= \frac{1260}{2}\pi \, cm^2$

Area of the flat surface

- $= (150 \times 8.4) cm^2$
- $=1260cm^{2}$

Total area =  $(1260 + 630 \ \pi + 17.64 \pi)$ 

- $= (1260 + 647.64\pi)cm^2$
- $= 3295 cm^2 / 3295.44 cm^2$

3. Surface area = 
$$2(0.6 \times 2.8)m^2 + 2(0.6 \times 3.2)m^2$$
  
=  $(3.36 + 3.84)m^2$   
=  $7.2m^2$ 

4. a) Area of hemispherical part

$$= \frac{1}{2} X 4 UR^{2}$$

$$= 2 X^{22}/_{7} x 35 X 35$$

$$= 7700 cm^{2}$$

b) Slant height for original cone

$$\underline{L} = \underline{35}$$

$$L - 60 \qquad 14$$

$$L = 100cm$$

c) Surface area of frustrum

$$= URL - url$$

$$= {}^{22}/7 X 35 x 100 - {}^{22}/7 x 14 X 40$$

$$= 11000 - 1760 = 9240 cm^{2}$$

d) Area of base

$$\frac{22}{7}$$
 X 14<sup>2</sup> = 616 cm<sup>2</sup>

e) Total surface

$$= 7700 + 9240 + 616 = 17556cm^2$$

5. 
$$a)TA = 2 X 6.8 X 3.5 + 2 X 4.2 X 3.5m^2$$
  
 $= 47.6 + 29.4 m^2 = 77m^2$   
 $b) 77 - (^{75}/_{100} X 2.5 X 2 + {}^{400}/_{100} X 1.25)m^2$   
 $77 - (3.75 + 5) m^2$   
 $77 - 68.25 m^2 = 8.75m^2$ 

c)i) Cost of paint A  $= 68.25 \times 0.8 \times 80 = Kshs.43681$ 

ii) Cost of paint B

68.25 X 35 0.5

= Kshs.4777.5

d) No of tins

 $= 54.6 \times 1000$ 400

= 136.5

= 137 tins

No. of tins

= <u>136.5</u>

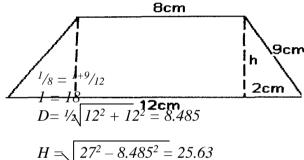
1.25

= 109.2= 110 tins

Top surface area =  $8x8 = 64cm^2$ 6. Bottom surface area =  $12x12=144cm^2$ Height of slanting faces  $H = 9^2 - 2^2 = 8.775cm$ Area of slanting face =  $\frac{1}{2}(12 + 8) \times 8.775 \times 4$  $= 351 cm^2$ 

For both Attempt to solve area for slant face

 $T.S.A = 64 + 144 + 351 = 559cm^2$ 



$$H = 27^2 - 8.485^2 = 25.63$$
  
 $h/25.63 = 8/12$ 

h=17.09cm

 $v = (\frac{1}{3} \times 12 \times 12 \times 25.63 - (\frac{1}{3} \times 8 \times 8 \times 17.09)$ 

 $= 865.7cm^2$ 

(c)  $Tan \theta^{25.63}/6 = 4.272$  $\theta = 76.82^{\circ}$ 



## 33. Volume of solids

1. a) Length of diagonal = 
$$\sqrt{10^2 + 8^2}$$
  
=  $\sqrt{164}$ 

*Vertical height* =  $\sqrt{16^2 - (\sqrt{164})^2}$ 

= 14.66cm

*b*) Height of the slant surfaces  $\sqrt{16^2 - 4^2} = \sqrt{240}$  $\sqrt{16^2 - 5^2} = \sqrt{231}$ Area of slant surfaces

 $(\frac{1}{2} \times 8 \times \sqrt{240} \times 2) = 124.0 \text{ cm}^2$  $(\frac{1}{2} \times 10 \times \sqrt{231} \times 2) = 152.0 \text{cm}^2$ Area of the rectangular base=  $8 \times 10 = 80 \text{cm}^2$  Teacher.co.ke

Total surface area =  $356cm^2$ 

- c) Volume =  $(\frac{1}{3} \times 80 \times 14.66) = 391.0 \text{cm}^3$
- 2. Volume of the cylinder  $= (^{22}/7 \times 6 \times 6 \times 12) cm^{3} = 1357.71 cm^{3}$ Volume of a sphere  $= (^{4}/_{3} \times ^{22}/_{7} \times 3 \times 3 \times 3) cm^{3} = 113.14 cm^{3}$   $\therefore \text{ No. of spheres formed}$   $= \frac{1357.71}{113.14 cm^{3}}$  = 12 spheres
- 3. Let the smaller length be x cm  $\therefore Dimensions \ are \ x, 2x, 3x$   $x \cdot 2x \cdot 3x = 1024$   $6x^3 = 1024$   $x^3 = \frac{1024}{6}$   $x = 3\sqrt{\frac{1024}{6}}$

301.71 - 75.43 = 226.26

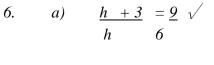
Dimensions are 5.547, 11.09, 16.64

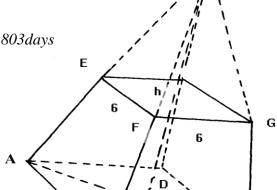
4. 
$$(60/360 \times 22/7 \times 24 \times 24) - (60/360 \times 22/7 \times 12 \times 12)$$

5. (a)(i) 
$$2\pi rh + 2r\pi^2 + \pi r^2$$
  
=  $2 \times 22/7 \times 1.4 \times 1.4) + 2 \times 22/7 \times 1.42) + (22/7 \times 1.42)m^2$   
=  $(12.32 + 12.32 + 6.16)m^2 = 30.8m^2$   
OR  $r(2h + 2r + r)$   
=  $22 \times 1.4 (2 \times 1.4 + 3(1.4) = 30.8m^2$ 

- (ii) shs.  $(75 \times 30.8) = Shs.2,310$
- (iii) Total vol.  $= {}^{22/7}x \ 1.42 \ x \ 1.4) + ({}^{1/2}x {}^{4/3}x {}^{22/7}x \ 1.42)m^3$   $= 8.624 \ 4.106 = 12.7306m^3$   $capacity = (12.7306 \ x \ 1000) liters = 12730.6 litres$
- (b) First  $2 days = 185 \times 2 = 370 litres$ Remaining amount = (12730.6 370) liters= 12360.6 litresDays to use = 12,360.6200
  = 61.803 daysIn all it takes = (61.803 + 2) days = 63.803 days

19





$$6h + 18 = 9h$$

$$h = 6 \text{ cm } \sqrt{$$

$$height = 6 + 3 = 9 \text{ cm}$$



b) 
$$Base = 9 \times 9 = 81 \text{ cm}^2$$
  
 $Top = 6 \times 6 = 36 \text{ cm}^2$   
 $Sides = 3.67 \times 15 \times \frac{1}{2} \times 4$   
 $= 110.15 \text{ cm}^2$   
 $Total = 227.15 \text{ cm}^2$ 

c) Vol. of bigger = 
$$\frac{1}{3}$$
 x 81 x 9  
= 243  
Vol of smaller =  $\frac{1}{3}$  x 36 x 6  
= 72  
Vol. of frustrum =  $\frac{171 \text{ cm}^2}{11.02}$   
 $\theta = 54.8^{\circ}$ 

7. Volume of a hemisphere
$$\frac{2}{\pi}r^3 = \frac{2}{2}x\frac{22}{2}x12x12x12$$
3 3 7
$$= \frac{176}{x}x144$$

$$= 3620.571429 = 3620.57$$
Volume of a cone
$$^2/_3\pi r^2 h$$

$$\frac{1}{x} \frac{22}{2}x6x6x6xh = 36.20.57$$
3 7
$$\frac{6x44h}{7} = 3620.57$$
7
$$264h = 3620.57x7$$

$$h = \frac{3620.57x7}{264}$$

$$= 95.9981 = 95.998$$

8. 
$$V = \left(\frac{22}{7}x \, 2x \, 2x \, 2x \, 1.5\right) + \left(\frac{22}{7}x \, 3x \, 3x \, 1.5\right) + \left(\frac{22}{7}x \, 4.4. \, x \, 1.5\right)$$

$$= \frac{132}{7} + \frac{297}{7} + \frac{528}{7}$$

$$V \text{ of hole} = \frac{22}{7}x \, 1x \, 14.5$$

$$= \frac{99}{7}$$

$$V = \frac{957}{7} - \frac{99}{7} = \frac{858}{7}$$

$$= 122.57 \text{ cm}^3$$

$$Mass = 2.8 x \, 122.57$$

$$= 343.196g$$

$$\approx 343.2g$$

Volume of hemisphere =  $\frac{1}{2}x \frac{4}{x} \frac{22}{x} \frac{7}{x} 7 x 7$ 9.

$$3 7_1$$
  
= 718.67 cm<sup>3</sup>

$$= 718.67 cm^3$$

Vol. of cylinder = 
$$\pi r^2 h = \frac{22}{7} x^{1/2} x 7 x 5 = 770 \text{ cm}^3$$

Vol of frustrum = 
$$\frac{1}{3}x \frac{22}{2}x 7x 7x h_1 - \frac{7}{7}$$
  
 $\frac{1}{3}x \frac{22}{7}x 3.5x 3.5x h_2$ 

Height of cone 
$$\Rightarrow h_1 = \frac{7}{h_2}$$
 but  $h_1 = h_2 + 6$ 

$$\frac{h_2 + 6}{h_2} = \frac{7}{3.5} \Rightarrow 7h_2 = 3.5h_2 + 21$$

$$3.5 h_2 = 21$$

$$h_2 = 6 cm$$

$$h_1 = 12 cm$$

.: Vol. of frustrym 
$$\neq \frac{1}{3}$$
/x  $\frac{22}{7}$  x  $\frac{4}{7}$ /x  $7$  x  $12$  -  $\frac{1}{7}$ 

$$= 616 - 77 = 539 \text{ cm}^3$$
Total volume = 718.67 cm<sup>3</sup> + 770cm<sup>3</sup> + 539 cm<sup>3</sup>

$$= 2027.67 \text{ cm}^3$$

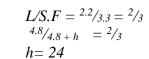
a) S.A of top = 
$$\pi r^2 \frac{22}{7} \times 3.5 \times 3.5 = 38.5 \text{ cm}^2$$

S.A of curved part of frustrum = 
$$\frac{22}{7}$$
 x 7 x 13.89 -

S.A of curved part of cylinder = 
$$2\pi r x h = 2/x \frac{22}{x} x 7 x 5$$
  
=  $2220 \text{ cm}^2$ 

S.A of hemisphere = 
$$\frac{1}{2}x \ 4 \pi r^2 = \frac{22}{7}x \ 7 x \ 7 = 308 \ cm^2$$
  
Total S.A =  $\frac{795.685 \ cm^2}{}$ 

10.



volume of smaller cone  $^{1}/_{3} x^{22}/_{7} x 2.2 x 2.4$ = 12.169

Volume of large cone  $^{1}/_{3} x^{22}/_{7} x 3.3 x 3.3 (4.8 + 2.2)$   $\therefore$  V of frustum  $82.14 - 12.17 = 69.97 \text{ cm}^{3}$ 

11. (a) Volume = 
$$\frac{2}{3}\pi r^3 + \frac{1}{2}\pi r^2 \times \frac{3}{2}r = 31.5\pi$$

$$4r^3 + 3r^3 = 31.5 \times 6$$

$$r = 3 \frac{31.5 \times 6}{7}$$

$$= 3cm$$

(b) slant height of 
$$con = \sqrt{4.5^2 + 3^2}$$
  
= 5.408cm  
Surface are =  $2\pi x 3^2 + \pi x 3 x 5.408 = 107.5 cm^2$ 

(c) Height = 
$$\frac{31.5}{4^2\pi}$$
  
=  $1.969cm$ 

(d) Density = 
$$\frac{144}{231.5\pi}$$
  
=  $1.46$ g/cm<sup>3</sup>

12. Volume of cube side 
$$x cm = (xcm)^3$$

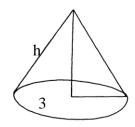
$$\therefore x^{3}cm^{3} = \underbrace{1280}_{20} cm^{3}$$

$$x = 3 \underbrace{1280}_{3}$$

$$= 3 \underbrace{64}$$

$$= 4 cm$$

13. 
$$\frac{9}{3} = \frac{14 + h}{h}$$



$$9h = 42 + 3h$$

$$6h = 42$$

$$h = 7$$

volume of the frustrum =  $(\frac{1}{3} x^{22}/_7 x 9 x 9 x 21)cm^3$ 

1.



$$(3x + 5)^{2} + (\sqrt{611})^{2} = (7x = 2)^{2}$$

$$(9x^{2} + 30x + 25) + 611 = 49x^{2} + 28x + 4$$

$$-40x^{2} + 2x + 632 = 0$$

$$20x^{2} - x = 316 = 0$$

$$x = \frac{1 \pm \sqrt{2581}}{40}$$

$$= \frac{160}{40} \quad OR \quad x = 4$$

$$Area = (\frac{1}{2}x\sqrt{611}x 17)$$

$$= 210.1cm^{2}$$

2. 
$$7x - 4 \le 9x + 2$$
  $9x + 2 < 3x + 14$   $6x < 12$   $x < 2$   $3 \le x$   $3 \le x < 2$   $4 \le 3x < 2$   $4 \le$ 

Integral values are -3, -2, -1, 0 and 1

### 35. Linear inequalities

1. 
$$\frac{12 \times 0.25 - 12.4 \div 0.4 \times 3}{\frac{1}{8} \text{ of } 2.56 + 8.68}$$

$$\frac{3 - 31 \times 3}{9}$$

$$0.32 + 8.68$$

$$\frac{-90}{9}$$

$$= -10$$

2. 
$$x - 9 \le -4 < 3x - 4$$
  
 $x - 9 \le -4$   
 $x \le 5$ 

$$3x-4 > -4$$

$$3x > 0$$

$$x = 0$$

$$0 > x \le 5 \sqrt{ }$$

$${1, 2, 3, 4, 5}$$

3. 
$$x > 3 - 2x$$
  
 $x \le 2x + 5$   
 $3 - 2x < x = -5$   
 $-2x < x = -3$ 

Teacher.co.ke

$$-3x < -3$$

$$x < 1$$

$$2x + 5 \ge 3x$$

$$-x \ge 5$$

$$x \le -5$$

 $-5 \leq x < 1$ 

$$3 - X \le 1 - \frac{1}{2}X$$

$$3 - 1 \le X - \frac{1}{2}X$$

$$2 \le \frac{1}{2}X$$

$$X \ge 4$$

5. 
$$4x - 3 \le 6x - 1$$
  
 $-2x \le 2$   
 $x \ge -1$   
 $6x - 1 < 3x + 8$   
 $3x < 9$   
 $x < 3$   
 $-1 \le x < 3$ 

6. 
$$2(2-x) < 4x - 9$$

$$4 - 2n < 4x - 9$$

$$4 + 9 < 4x + 2n = 13 6x$$

$$= \frac{13}{6} < n \qquad = \frac{2^{1}}{6} < n$$

$$and 4x - 9 < x + 11$$

$$4n - n < 11 + 9$$

$$3n < 20$$

$$x < \frac{20}{3} = \frac{2}{3}$$
Integral values 3, 4, 5, 6

7. 
$$L_3: y \ge 1$$
  
 $L_1: y + x \ge -1$   
 $L_2: y - x$   
8.  $a)$   $x^2 + 2xy + y^2 = x^2 + xy + xy + y^2$   
 $= x(x + y) + y(x + y)$   
 $= (x + y)(x + y)$   
 $\therefore (x + y)^2 = 8x \cdot 8 = 64$ 

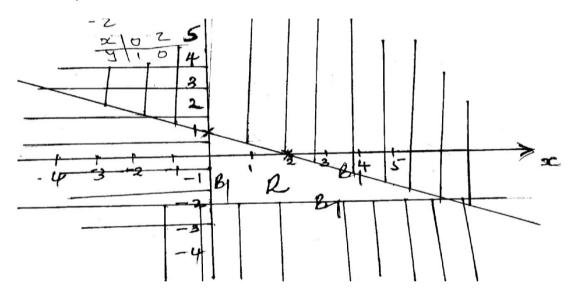


b) 
$$x^{2} + 2xy + y^{2} = 64$$
$$(x^{2} + y^{2}) + 2xy = 64$$
$$34 + 2xy = 64$$
$$2xy = 30$$

Equation of L1 (3.5, 4) (0, 2) y-2 = 2  $x-0 \quad 3.5-0$  3.5y - 7 = 2x  $\therefore y = \sqrt[4]{7x} = 2x$ Inequality of  $y \le \sqrt[4]{7x} + 2$  $Or 7y \ 4x + 14$ 

Equation of L2 (0, 3) (4, 2) y-2 = 3-2 x-4 0-4 -4(y-2) = x-4 -4y + 8 = x-4 -4y = x-12inequality  $y \ge -\frac{1}{4}x + 3$  $4y \ge -x + 12$  Equation of L3  $\underline{y-2} = \underline{2}$  x-4 - 0.5 -0.5(y-2) = 2(x-4) -5y + 1 = 2x - 8 -5y = 2x - 9 y = -4x + 18in equality  $y \le 4x + 18$ 

10. Lines to be drawn 
$$x = 0$$
,  $y = 2$   
 $2y + x = 2$   $x = 0$   $x = 0$   
 $y = 2$ 



11. 
$$3(1+x) < 5x - 11$$
  
 $3+3x) < 5x - 11$   
 $-2x < -14$   
 $x > 7$   
 $5x - 11 < 45$   
 $5x < 56$   
 $x < 11.2$   
Integral values are 8, 9, 10, 11

12. 
$$y \leqslant x$$
 $x \leqslant 8$ 
 $y \geqslant 0$ 

## 36. Angle properties of circles

1. Area of 
$$\triangle AXY = \frac{1}{2} x 4^2 x \sin 97.2^0$$
  
= 7.94 cm<sup>2</sup>  
Area of sector  $AXY = \frac{97.2}{360} x \pi x 4^2$ 



$$= 13.57 \text{ cm}^2$$

Area of shaded part = 
$$13.57 - 7.94 = 5.63 \text{ cm}^2$$

Area of 
$$\triangle$$
 BXY =  $\frac{1}{2}$  x 6<sup>2</sup> sin 30

$$= 9 cm^2$$

Area of sector BXY = 
$$\frac{30}{360}$$
 x  $\pi$  x  $6^2$ 

$$= 9.42 \text{ cm}^2$$

Area of shaded part

$$= (9.42 - 9) cm^2 = 0.42 cm^2$$

Area of shaded region =  $(5.63 + 42) \text{ cm}^2 = 6.05 \text{ cm}^2$ 

2. (i) 
$$\angle AOB = 2 \angle ACB$$
  
 $= 100^{\circ}$   
 $\angle OAB = \underline{180 - 100}$  Base angles of Isosceles  $\triangle$ 

$$=40^{0}$$

(ii) 
$$\angle ADC = 180^{\circ} - 70^{\circ}$$
  
=  $110^{\circ}$ 

3. 
$$\frac{2}{5} \div \frac{1}{2} 0f^{4}/9 - \frac{1}{10}$$

$$= \frac{2}{5} \div \frac{1}{2} X^{4}/9 - \frac{11}{10}$$

$$= \frac{2}{5} x^{9}/2 - \frac{11}{10}$$

$$= \frac{9}{5} - \frac{11}{10} = \frac{18 \cdot 11}{10} = \frac{7}{10}$$

$$^{1}/_{8} - ^{1}/_{6} X^{3}/_{8} = ^{1}/_{8} - ^{1}/_{16}$$
  
=  $^{2-1}/_{16} = ^{1}/_{16}$ 

$$\frac{\frac{2}{5} \pm \frac{1}{2} 0f^{4}/9 - 1^{1}/10}{\frac{1}{8} - \frac{1}{6} 0f^{3}/8} = \frac{\frac{7}{10}}{\frac{1}{16}}$$

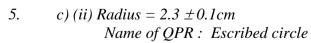
$$= \frac{7}{10} X^{16}/1$$

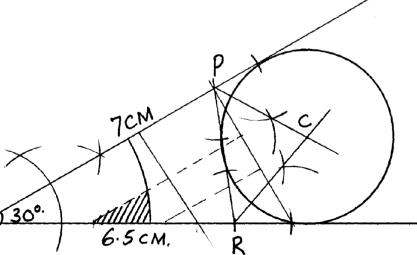
$$= \frac{56}{5} = 11^{1}/5$$

4. a) 
$$DAC = DCA = \frac{1}{2}(180 - 100)$$
 (base sios =  $40^{\circ}$ 

(b) 
$$BAC = DCA \ alt \ , \angle s \ AB/AD$$
)  
=  $40^{\circ}$ 

(b) 
$$DAB = DAC + BAC = 40 + 40 = 80^{\circ}$$
  
 $BCD = 180^{\circ} - 80^{\circ}$   
 $= 100^{\circ}$ 







- (i)  $\angle ACB = 10^{\circ} (\angle s \text{ subtended by chord } AB)$
- (ii)  $\angle AOD = 160^{\circ} (\angle \text{ at centre line at circumference})$
- (iii)  $\angle CAB = 40^{\circ}$  ( $\angle s$  subtended by chord AB)
- (iv)  $\angle ABC = 130^{\circ}$  ( Opposite  $\angle s$  of cyclic quadrilateral)
- (v)  $\angle AXB = 60^{\circ}$  (sum angle of triangle
- 7. i)  $\underline{80} \times \underline{22} \times 9 \times 9$   $360 \quad 7$ = 63.6429 cm<sup>2</sup>
  - ii)  $\frac{1}{2}$  ab Sin C =  $\frac{1}{2}$  x 9 x 9 Sin 80<sup>0</sup> = 39.8847 cm<sup>2</sup>
  - iii)  $\frac{180}{360}$  x  $\frac{22}{3}$  x 9 x 9 = 127.2857 cm<sup>2</sup>

Segment: 63.6429 - 39.8847=  $23.7582 \times 2 = 47.5164 \text{ cm}^2$  $\therefore 127.2857 - 47.5164$ =  $79.7693\text{cm}^2 = 79.77 \text{ cm}^2$ 

- 8. (a)  $\angle RST = 180^{\circ} 46^{\circ}$  Opposite angel in cyclic quadrilateral =  $134^{\circ}$ 
  - (b)  $\angle SUT = 180^{\circ} 46^{\circ} 27^{\circ}$  (Sum of angles in a traingle QRU) =  $180^{\circ} - 173^{\circ} = 7^{\circ}$
  - (c)  $\angle ROT = 2 \times 46^{\circ}$  (angle substended by chord RT at the centre =  $92^{\circ}$
  - (d)  $\angle PST = 180^{\circ} 37^{\circ} 48^{\circ} 53^{\circ}$ Sum of angles in a triangle PST
  - (e) Reflex  $\angle SOP = (2x \ 37^{\circ}) + 2x \ 42^{\circ}) = 158^{\circ}$ Angle subtended chord at centres is twice angle at circle

9.  $\angle POQ = 80^{\circ}$ Radius = 1.7Sin 40 = 2.645cm Area of the triangle =  $\frac{1}{2}x \ 2.645^{2} \sin 80 = 3.445$ cm<sup>2</sup> Area of the sector =  $(80 \times \pi \times 2.645^{2})$  360 = 4.884cm<sup>2</sup> Area of the shaded segment = (4.884 - 3.445) = 1.439cm<sup>2</sup>

10. a)  $\angle BDC = 90^{\circ} -33^{\circ}$ ,  $3^{rd}$  angle of

1.

= 
$$57^{\circ} \triangle BCD$$
,  $\angle BCD = 90$ .

$$\angle ADC = \angle ADB + \angle BDC$$
  
=  $48^{\circ} + 57^{\circ} = 105^{\circ}$ 

#### b) Consider $\triangle$ BCE

∡ AEB is an exterior opposite angle

$$\therefore \angle AEB = 33^{\circ} + 48^{\circ} = 81^{\circ} \sqrt{}$$

#### 37. Vectors

$$Sin \overline{60} = \sqrt{3}/2 \qquad 1$$

$$Sin \overline{45} = \frac{1}{\sqrt{2}} - \frac{\sqrt{3}}{\sqrt{2}} \frac{1}{\sqrt{2}} - \underline{1}$$

$$= \underline{1} - \frac{\sqrt{3}}{2\sqrt{2}} \cdot \frac{1}{\sqrt{2}}$$

$$= \underline{\sqrt{6}} - \underline{\sqrt{2}}$$

$$= \underline{\sqrt{6}} - 2\sqrt{2}$$

$$= \underline{\sqrt{6}} - 2\sqrt{2}$$

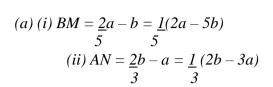
2. 
$$OP = OA + \frac{1}{4}AB$$
  
 $\stackrel{\sim}{=} QA + \frac{1}{4}(QB - QA)$   
 $= QA + \frac{1}{4}QB - \frac{1}{4}QA$   
 $= \frac{3}{4}QA + \frac{1}{4}QB$ 

$$= \frac{3}{4} QA + \frac{1}{4} QB$$

$$= \frac{3}{4} \begin{bmatrix} 12 \\ 8 \end{bmatrix} + \frac{1}{4} \begin{bmatrix} 16 \\ 4 \end{bmatrix} = \begin{bmatrix} 3 \\ 6 \end{bmatrix} + \begin{bmatrix} 4 \\ 1 \end{bmatrix} = \begin{bmatrix} 7 \\ 7 \end{bmatrix}$$

3. 
$$m + 4 + n = \begin{bmatrix} -3 \\ 2 \end{bmatrix} = \begin{bmatrix} 5 \\ 8 \end{bmatrix}$$
  
 $4m - 3n = 5 \dots (i) \times 2$   
 $3m + 2n = 8 \dots (ii) \times 2$   
 $8m - 6n = 10$   
 $9m + 6n = 24$   
 $17m = 34$ 

$$m= 2$$
  
 $4 \times 2 - 3n = 5$   
 $-3n = -3$   
 $n = 1$   
∴  $m = 2, n = 1$ 



(b) 
$$BX = \underline{t}(2a - 5b)$$

$$5$$

$$AX = \underline{h}(2b - 3a)$$

$$OX_1 = OB + BX = b + t(\underline{2}a - 5b)$$

$$5$$

$$= (-t)b + \underline{2} + a$$

$$5$$

$$OX = OA + AX = a + h(2b - 3a)$$

$$= (1-h)a + \underline{2}hb$$

$$3$$

(c) 
$$OX_1 = OX_2$$
  
 $\frac{2}{5} + a + (\frac{1}{4} - t)b = (1 - h)a + 2hb$   
 $\frac{2}{5}$   
 $\frac{2}{3}t = 1 - h ....(i)$   
 $\frac{2}{5}t = 1 - h ....(i)$   
 $\frac{2}{$ 

5. 
$$a) i) MA = \frac{1}{2} a$$

$$ii) AB = a$$

$$iii) AC = a + c$$

$$iv) AX = \frac{2}{7} AC = \frac{2}{7} (-a + c)$$

b) 
$$MA = \frac{1}{2}a$$
  
 $AX = \frac{2}{7}c - \frac{2}{7}a$   
 $MX = \frac{1}{2}a + \frac{2}{7} - \frac{2}{7}a$   
 $= \frac{3}{14}a + \frac{2}{7}c$ 

Co-ordinates of 
$$P = (\underline{1+3}, \underline{6+0}, \underline{8+4})$$



$$/OP/ = \sqrt{2^2 + 3^2 + 6^2}$$
  
=  $\sqrt{4 + 9 + 36}$   
=  $\sqrt{49}$  = 7 units

- c) Co-ordinates of O (0,0,0) Co-ordinates of A (1, 6, 8) Mid points of AO =  $(\underline{1+0}, \underline{6+0}, \underline{8+0})$   $\underline{2}$   $\underline{2}$   $\underline{2}$ = (0.5, 3, 4)
- 6. a)  $AB = DC \Rightarrow 1 x = 2 \Rightarrow x = -1$   $6 y = 4 \Rightarrow y = 2$   $\therefore D = (-1, 2)$

b) (i) 
$$\overrightarrow{RQ} = Q \left( R = q - \frac{3}{2} q - \frac{1}{2} p \right)$$
  
 $\left( -\frac{1}{2} q \right) - p \left( = \frac{1}{2} p \right) - q \quad \sqrt{2}$ 

(ii) 
$$\overrightarrow{PR} = \frac{3}{2} \cancel{q} \quad \cancel{-1/2} p - P \sqrt{\frac{3}{2} \cancel{q} - p}$$

$$= \frac{3}{2} \cancel{q} \quad \cancel{q} - p$$

$$= \frac{3}{2} \cancel{q} \quad \cancel{q} - \cancel{p}$$

$$\Rightarrow k = -3$$

Hence P, Q, R, Q Collinear.

(iii) 
$$\overrightarrow{PQ} = q - p$$
,  $Q\overrightarrow{R} = \frac{1}{2}(q - P)$   
 $PQ : QR = 2 : 1$ 

7. (a) 
$$PQ = PO + OQ = -p + q$$
  
 $Or = OP + PR = P + 2/3 PQ$   
 $= P + 2/3 (-p+q)$   
 $= \frac{1}{3}p + \frac{2}{3}q$ 

$$QT = QO + OT = -q + \frac{1}{2} OR \text{ since } OT = TR$$
  
=  $-q + \frac{1}{2} (\frac{1}{3}p - \frac{2}{3}q)$   
=  $\frac{1}{6}p - \frac{2}{3}q OR \frac{1}{6} (p-4q)$ 

(b) 
$$TS = TO + OS = -\frac{1}{2} OR + \frac{1}{4} OP$$
  
=  $-\frac{1}{2} (\frac{1}{3}p + \frac{2}{3}q) + \frac{1}{4}p = \frac{-1}{6}p - \frac{1}{3}q + \frac{1}{4}p$   
=  $\frac{1}{12}p - \frac{1}{3}q \text{ or } \frac{1}{12}(p-4q)$ 

*QT*:  $TS = {}^{1}/6(p-4q)$ :  ${}^{1}/12(p-4q) = {}^{1}/6$ :  ${}^{1}/12 = 2$ : 1 ::  $QT = 2TS \ OT//TS \ but \ T \ is a common point hence \ Q, \ T, \ S \ are \ collinear$ 



```
(c) Vector OT can be expressed in 2 ways

1^{st} OT = \frac{1}{2} OR given

= \frac{1}{2} (\frac{1}{3} P + \frac{2}{3} q) = \frac{1}{6} q + \frac{1}{3} q \dots (i)

2^{nd} using OPT

OT = OP + PT = P + \frac{5}{6} PM

But PM = PO + OM = -P + KOQ = -P + Kq

OT = P + \frac{5}{6} (-P + kq)

= P - \frac{5}{6} kq

= \frac{1}{6} p + \frac{n^{5}}{5} kq \dots (ii)

Aqn (i) and (ii) represent the same vector OT

\frac{1}{6} p + \frac{1}{3} q = \frac{1}{6} p + \frac{5}{6} kq \dots (iii)

Comparing coefficients of q in eqn (iii) have \frac{5}{6} k = \frac{1}{3}

15k = 6
```

8. 
$$3a = 3(-3) = (-9)$$

$$2 = 6$$

$$\frac{1}{2}b = \frac{1}{2}(4) = (2)$$

$$-6 = -3$$

$$\frac{1}{100}c = \frac{1}{10}(5) = (0.5)$$

$$-10 = -1$$

$$P = (-9) - (2) + 0.5$$

$$6 = -3 = -1$$

$$= (-10.5)$$

$$8$$

$$\frac{1}{1000} = \frac{1}{1000} = \frac{1}{1000}$$

$$\frac{1}{1000} = \frac{1}{1000} = \frac{1}{1000}$$

$$\frac{1}{1000} = \frac{1}{1000} = \frac{1}{1000}$$

$$\frac{1}{1000} = \frac{1}{1000} = \frac{$$

$$(i)BM = BO + OM$$
$$= \frac{2}{5}a - b$$

$$(ii) AN = AO + ON$$
$$= \underbrace{2}_{3} b - a$$

(b) 
$$OX = OB + BX$$
  
 $= b + k (2 a - b)$   
 $\sim = 2 ka + b(1 - k)$   
 $\sim 5$   
 $OX = OA + AX$   
 $= a + h (2b - a)$   
 $\sim 3$   
 $= a (1 - h) + 2 hb$   
 $= a (10h) 2hb$ 

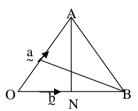
(c) 
$$^{2}/_{5} a = a (1-h) also b(1-k) = 2hb$$
  
 $2k = 1-h$   $1-k = 2h$   
 $k = \frac{5}{2} - \frac{5}{2}h$ 

$$\begin{array}{ccc}
\overline{2} & \overline{2} \\
\vdots & 1 - \underline{5} + \underline{5}h = \underline{2}h \\
\underline{5}h - \underline{2}h & \underline{5} - 1 \\
\underline{2} & 3 & 2
\end{array}$$

$$\begin{array}{cccc}
\underline{5}h - \underline{2}h & \underline{5} - 1 \\
\underline{2} & 3 & 2
\end{array}$$

$$\begin{array}{cccc}
\underline{15}h & \underline{3} & \underline{6} & \underline{9} \\
\underline{211} & \underline{11} & \underline{6} & \underline{5} & \underline{9} \\
\underline{22} & \underline{11} & \underline{5} & \underline{9} \\
\underline{22} & \underline{22} & \underline{11}
\end{array}$$

$$\begin{array}{ccccc}
\underline{5} - \underline{45} & \underline{9} \\
\underline{222} & \underline{5}
\end{array}$$



10. (i) 
$$AN = AO + ON$$
$$= -a + \frac{4}{5}b$$

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$$(ii)$$
  $BM = BO + OM$   
=  $-b + \frac{2}{5}a$ 

$$(iii) AB = AQ + OB$$

$$= -a + b$$

$$\sim AX = sAN$$

$$\sim BX = tBM$$

$$OX = OB + BX$$
$$= b + tBM$$

$$=b+t\left(-b+\frac{2}{5a}\right)$$

$$= b - tb + \frac{2}{5}ta$$

$$= b (1-t) + \frac{2}{5}ta$$

$$OX = OA \pm AX$$

$$= a + sAN$$

$$= a + s(-a + 4/5b)$$

$$= \underbrace{a - Sa + \frac{4}{5} sb}_{a(1-s) + \frac{4}{5} sb}$$

$$b(1-t) + \frac{2}{5}sta = a (1-s) \frac{4}{5}sb$$
  
 $b(1-t) = \frac{4}{5}sb$ 

$$1-t = \frac{4}{5}s----(i)$$

$$a(1-s) = \frac{2}{5}ta$$

$$1-s = \frac{2}{5}ta^2$$

$$s=1-\frac{2}{5}t-----(ii)$$

$$1-t = \frac{4}{5}(1-\frac{2}{5}t)$$

$$1 - t = \frac{4}{5} - \frac{8}{25}t$$

$$-\frac{17}{25} = -\frac{1}{5}$$

$$t = \frac{5}{17}$$

$$s = \frac{15}{17}$$

11. <u>115800</u> x <u>97.5</u> 76.84 100

= 1469.35 
$$\sqrt{\phantom{0}}$$

$$= 1469.35 - 270$$

= 1199.35 
$$\sqrt{}$$

= 1199 dollars

*12*.

$$RM = \begin{bmatrix} -2\\6\\7 \end{bmatrix} - \begin{bmatrix} 5\\-2\\0 \end{bmatrix} = \begin{bmatrix} -3\\8\\-1 \end{bmatrix}$$

$$|RM| = \sqrt{(+3)^2 + 82(-1)^2}$$
  
74 = 8.602 units

13. (a) (i)  $OB \equiv a \pm b$ 

(ii) 
$$BC = BA + AO + OC$$
  
=  $ab + -a + 2b$ 

$$= b - a$$

(b) CX = CQ + OA + AB + BX= = 2b + a + b + hBC

$$= -2b + a + b + a$$

$$= a - b + h(b - a)$$

$$=a-b+hb-ha$$

~

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~ ~

$$= (1 - h)a + (h - 1)b$$

(c) 
$$CX = CO + OA + AX$$
  
 $= 2b + a + KAT$   
 $but AT = AO + OT$   
 $= -a + 3b$   
 $CX = 2b + a + K(3b - a)$   
 $= a - Ka + 3Kb + 2b$   
 $= (1 - K) a + 3 (K + 2) b$ 

(d) 
$$I - h = 1 - k$$
 ......(i)  
 $h - 1 = 3k + 2$ .....(ii)

from (i) 
$$h = k$$
  
sub in (ii)  $h-1 = 3h + 2$   
 $h = {}^{-3}/_2$   
 $K = {}^{-3}/_2$ 

14. 
$$a + b = (2-3)i + (1+4)j + (-2-1)k$$
  
=  $-i + 5j - 3k$ 

$$/a + b / (-1)^{2} + (5)^{2} + (-3)^{2}$$

$$= \sqrt{35}$$

$$= 5.916$$

15. i) 
$$BD = BA + AD$$
  
 $= -b + \frac{3}{5}c$   
 $AE = AB + BE$   
 $= b + \frac{1}{2}BC = b + \frac{1}{2}(c - b)$   
 $= \frac{1}{2}b + \frac{1}{2}c$ 

ii) 
$$BF = t (\sqrt[3]{5}c - b)$$
  
 $AF = n (\sqrt[4]{2}b + \sqrt[4]{2}c) = \sqrt[n]{2}(b + c)$   
 $AF = AB + BF$   
 $= b + t(\sqrt[3]{5}c - b) = b + \sqrt[3]{5}tc + tb$   
 $= (1 - t) b + \sqrt[3]{5}tc$   
 $(1 - t)b + \sqrt[3]{5}tc = \sqrt[n]{2}b + \sqrt[n]{2}c$   
 $1 - t = \sqrt[n]{2}; 2 - 2t = n \dots (i)$   
 $\sqrt[3]{5}t = \sqrt[n]{2}; 6t - 5n = 0 \dots (ii)$ 

Sub from équation (ii)  

$$6t - 5(2 - 2t) = 0$$
  
 $6t - 10 + 10t = 0$   
 $16t = 10$   
 $t = {}^{10}/_{16} = {}^{5}/_{8}$   
 $n = {}^{3}/_{4}$ 

iii) 
$$BF = \frac{5}{8}BD$$
  
 $F$  divides  $BD$  in the ratio  $5:3$   
 $AF = \frac{3}{4}AE$   
 $F$  divides  $AE$  in the ratio  $3:1$ 



$$16. \qquad BA = \begin{bmatrix} -8 \\ -2 \end{bmatrix}$$

$$\frac{1}{2}BC = \frac{1}{2} \begin{bmatrix} -3 \\ -4 \end{bmatrix} = \begin{bmatrix} 1 & \frac{1}{2} \\ -2 \end{bmatrix}$$

$$OP = \begin{pmatrix} -8 \\ -2 \end{pmatrix} \begin{pmatrix} -1 \\ -2 \end{pmatrix} \frac{1}{2} \begin{pmatrix} -2 \\ -4 \end{pmatrix} \frac{1}{2}$$

Co-ordinates of  $P(-9\frac{1}{2}, -4)$ 

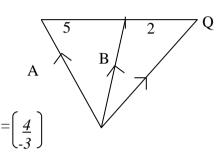
17. 
$$OB = \frac{5}{2}OQ + \frac{2}{2}OA$$

$$OQ = \frac{7}{2}OB - \frac{2}{2}OA$$

$$5$$

$$OQ = \frac{7}{5} \begin{pmatrix} 2 \\ -1 \end{pmatrix} - \frac{2}{5} \begin{pmatrix} -3 \\ 4 \end{pmatrix}$$

$$= \begin{pmatrix} 14/5 \\ -7/5 \end{pmatrix} - \begin{pmatrix} -6/5 \\ 8/5 \end{pmatrix} = \begin{pmatrix} 20/5 \\ -15/5 \end{pmatrix}$$



$$Q = (4, -3)$$

## 38. Representation of data

1.

Length	Frequency
$11.5 \le x \le 13.5$	6
$13.5 \le x \le 15.5$	9
$15.5 \le x \le 17.5$	6
$17.5 \le x \le 23.5$	3

2. Food: 
$${}^{40}/_{100} \times 360 = 144$$
 °

*Transport:*  $^{10}/_{100} \times 360 = 36^{\circ}$ 

*Education:*  $\frac{20}{100} \times 360 = 72^{\circ}$ 

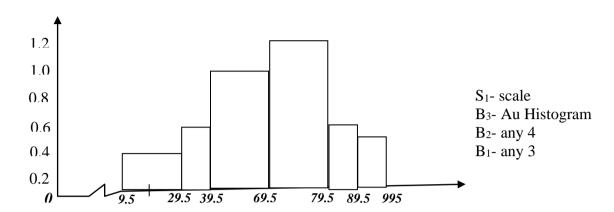
*Clothing:*  $^{20}/_{100} \times 360 = 72^{\circ}$ 

*Rent:*  $^{10}/_{100} \times 360 = 36^{\circ}$ 

3	C. Class	Tally	Frequency	Upper Limit
	10 – 29	JH1 111	8	29.5 B <sub>2</sub> for
	30 – 39		6	39.5 all tally
	40 – 69	1141111 1111 1111 11		69.5 B <sub>2</sub> all
			209	



<u> Modal class 40 – 6</u>9 B1



4. See the graph paper.

For correct class boundaries

For correct class intervals.

All frequency densities

Correct scale

All the bars drawn.

Top mid pts. Of bars indicated.

For the mid pts. Joint to make a polygon.

For correctly identifying the modal mark point.

For reading correctly the modal mark  $\equiv 53.5 \pm 0.1$ 

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Marks	Frequency
5-9	20
10-19	50
20-30	40
40-49	30

#### (b) Modal class is $\overline{10-19}$

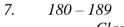
(c)(i)

Class	X	f	fx	Cf
5-9	7	20	140	20
10-19	14.5	50	725	70
20-39	29.5	40	1180	110
40-49	44.5	30	1335	140
		$\Sigma F =$	$\Sigma Fx = 3380$	
		140		

$$x = \underline{\Sigma f x} = \underline{3380} = 24.14$$
 $\Sigma f = 140$ 
(ii) Median mark is at  $70 + 71 = 70.5^{th}$  position
Median =  $119.5 + (\underline{0.5}) \times 20$ 
 $= 19.5 + 0.25$ 

= 19.75

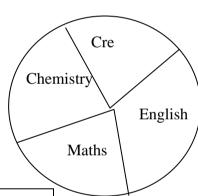
6. Total No. of sessions  
= 
$$8 + 7 + 4 + 3 = 22$$
  
Angle for:  
English =  $\frac{8}{22} \times 360 = 130.9^{\circ}$   
Maths =  $\frac{7}{22} \times 360 = 114.5^{\circ}$   
Chemistry =  $\frac{4}{22} \times 360 = 65.5^{\circ}$   
 $CRE = \frac{3}{22} \times 360 = 49.01^{\circ}$ 



Class limits

class	limits	f	cf
149.5	159.5	2	2
159.5	169.5	9	11
169.5	179.5	12	23
179.5	189.5	16	39
189.5	199.5	7	46
199.5	209.5	4	50

Median = 
$${}^{50}/_{2}$$
 = 25  
 $179.5 + \underline{25 - 23} \times 10$   
 $16$   
=  $179.5 + \underline{20} = 180.75$   
 $16$   
 $179.5 + \underline{26 - 23} \times 10$   
 $16$   
 $179.5 + \underline{30} = 181.38$   
 $16$   
 $\underline{180.75 + 181.38}$   
 $2$ 



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*a) i)* 145 – 153

ii) Median class

 $(^{40+1}/_2)^{th}$  value :: median class = 145-153

This is the 20.5<sup>th</sup> value

The value also in the 145 - 153 class

b)

Class	X	f	fx
118- 126	122	3	366
127- 135	131	4	524
136 – 144	140 B1	10 B2	1400
145 – 153	149	12	1788
154 - 162	158	5	790
163 – 171	167	4	668
172 - 180	176	2	352
		<i>Ef</i> = 40	Efx = 5888

B2 for all values of fx correct and B1 for 4 values of fx and above orrect

Mean = Efx = 
$$5888$$
 =  $147.2mm$   
Ef 40  
Median  $20^{th}$  =  $144.5 + (^{11}/_{12}x 9) = 152.75$   
 $21^{st}$  =  $144.5 + (^{12}/_{12}x 9) = 153.5$   
Median =  $\underline{152.75 + 153.5}$  =  $153.125$ 

(Alternatively one could work out the 20.5 value directly using median formula)

### 39. Measures of central tendency

1. 
$$4+6+10+14+x+24+14+6=100$$
  
 $78+x=100$ 

- (*i*) x = 22
- (ii)  $Modal\ class = 55$  -59

Marks	x	f	fx	cf
30-34	32	4	128	4
35-39	37	6	222	10
40-44	42	10	420	20
45-49	47	14	659	34
50-54	52	22	1144	56
55-59	57	24	1368	80
60-64	62	14	868	94
65-69	67	6	462	100
E	$\mathbf{B}_{I}$	$\Sigma f = 100$	$\Sigma fx = 5210$	$B_{I}$
		$B_1$	-	

$$\Sigma fx = 5210$$
(i)  $Mean = 5210$ 
 $100$ 
 $= 52.10$ 

(ii) Median = 
$$49.5 + \frac{50-34}{22} \times 5$$

= 53.14

 $Log_{10} 5^2 - log_{10} 2^3 + log 2^5$ 

$$Log_{10}\left(\frac{25 \times 32}{8}\right)$$

 $\sqrt{Application}$  of logarithmic laws.

 $\sqrt{Application}$ 

*C.A.O* 

 $Log_{10} 100 = \log_{10}^{2} \log_{10}^{10}$  $= 2 \log_{10}^{10}$ 

But  $log_{10}^{10} = 1$ 

*∴* = 2

3. *Modal class* 150-154

Height	Frequency	c.f
140- 144	3	3
145 – 149	15	18
150 – 154	19	37
155 – 159	11	48
160 -164	2	50

Height Frequency c.f  
= 
$$149.5 + (25-18) \times 5$$
  
=  $149.5 + 7 \times 5$   
=  $149.5 + 7 \times 5$ 

= 15.34

= 149.5 + 1.842

4.

Н	20-24	25-29	30-34	35-39	40-44	45-49
$\boldsymbol{F}$	3	19	25	20	18	15
CF	3	22	47	67	85	100

$$Md = 34.5 + (50 - 47) \times 4$$

$$= 34.5 + \frac{12}{20} = 35.1$$

5. a) 
$$2x^{2} + 6x - 2x = 0$$
$$32 - 24 - 2x = 0$$
$$-2x = -8$$
$$x = 4$$

b) 
$$2x^2 + 6x - 8 = 0$$
  
 $x^2 + 3x - 4 = 0$   
 $x^2 + 4x - x - 4 = 0$   
 $x(x - 4) - (x + 4) = 0$   
 $(x - 1)(x + 4) = 0$   
 $\therefore$  the other root is 1

6. 
$$\Sigma xf = 61 \times 10 + 65.5 \times 20 + 71 \times 40 + 77 \times 15$$
$$= 610 + 1310 + 2840 + 1155$$
$$= 5915$$
$$\underline{\Sigma} xf = 5915$$



Marks	30-39	40-49	50-59	60-69	70-79	80-89	90-99
No. of candidates	2	3	10	12	8	3	2
C.F	2	5	15	27	35	38	40

- a) Number who sat = 40
- b) The modal class = 60 69

	١
0	
u	,

Marks	x	f	X - 64.5 = d	fd
30-39	34.5	2	-30	-60
40-49	44.5	3	-20	-60
50-59	54.5	10	-10	-100
60-69	64.5	12	0	0
70-79	74.5	8	10	80
80-89	84.5	3	20	60
90-99	94.5	2	30	60
		$\pounds f = 40$		$\pounds fd = -20$

$$Mean = 64.5 + \frac{-20}{40}$$

$$= 64.0$$

 $= \frac{1}{2} (128.16666667)$ 

d) The median mark

$$= \frac{1}{2} (20^{th} \text{ and } 21^{st}) \text{ marks}$$

$$= \frac{1}{2} (59.5 + \frac{5}{2} x 10 + 59.5 + \frac{6}{2} x 10)$$

$$= \frac{1}{2} (59.5 + 4.16666 + 59.5 + 5)$$

- a) Mode = 4
- b) Median = 3

c) 
$$Mean = \underbrace{1 \ x2 + 2 \ x \ 2 + 3 \ x \ 1 + 4 \ x \ 3 + 6 \ x \ 1}_{9}$$
  
= 3

9. *a) i)* 
$$Modal\ class = 60 - 69$$

# ii) class where medium lies median class 50- 59

median class 50- 59			
Class	Centre X	Fd	D=x-A
0 - 9	4.5	-50	-50
10 - 19	14.5	-80	-40
20 - 29	24.5	-120	-30
30 – 39	34.5	-140	-20
40 - 49	44.5	-100	-10
50 – 59	54.5	0	0
60 - 69	64.5	200	10
70 – 79	74.5	120	20
80 – 89	84.5	90	30
90 – 99	94.5	40	40

= 64.083

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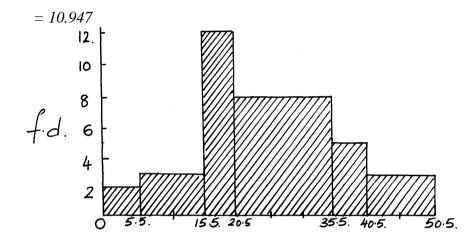
$$Mean = 54.5 - 40$$

$$70$$
= 53.93

10.

Cumulative frequency 3,11, 30, 44, 50 Median = L1t  $(\frac{n}{2} - cfa)$ Fn =  $8 + (25 - 11) \times 4$ 

11.



#### 40. Linear motion

1. Distance covered by Kinyua in 12/3hrs

$$= 5 \times 90 = 150 \text{km}$$

Distance traveled by Nyaboke during the rest =  $(\frac{1}{3} \times 120) = 40$ km

$$\underline{x} = \underline{390 - x} \Rightarrow 120x = 90(390 - x)$$

$$= 167.1km$$

$$Time = \frac{167.1}{90} = 1.86$$

$$8.33 + 1.86 = 10.19$$
; they met at = 10.11a.m

$$580 - (150 + 167.1) = 262.9$$
km from M

Before the rally driver started, Nyaboke had traveled for 1 1/2 hrs

$$(\sqrt[3]{2} \times 120) = 180 \text{km}$$

$$\underline{x} = \underline{x + 180}$$

$$180x - 120x = 21600$$

$$x = 360km$$

*Distance from K* = 580 - (180 + 360)

$$x = 40km$$

$$Time = \underline{540} = 3hrs$$

$$(9.30 + 3hrs) = 12.30p.m$$

2. Distance covered by the car after 15 min =  $(\frac{1}{4} \times 80)$ km = 20km

Distance covered together = 130km

*Relative speed* = (80 + 40) = 120 km/h

Time taken to meet 120 = 1hr 5 min

= (130) hrs

Time they met = 10:15 a.m +

. 
$$a) \frac{1}{2} X 50h + \frac{1}{2} X 100 h + 150h = 2700$$

$$225h = 2700$$

$$H = \frac{2700}{225} = 12 \text{m/s}$$

$$Maximum\ speed = \frac{12\ x\ 60\ x\ 60}{1000}$$

= 43.2 km/h

b) Acceleration =  $\frac{12}{50}$  m/s  $= \frac{6}{25} \, m/s$ 

c)  $\frac{1}{2}$  X 50 x 6 150 m

d) Time for half of journey

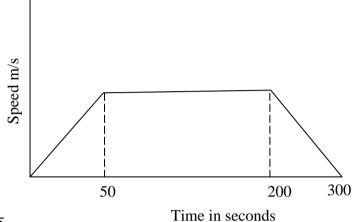
$$\frac{1}{2}X 12 (50 + t + t) = \frac{1}{2}X 2700$$

$$6(50 + 2t) = \frac{1}{2}X 2700$$

$$50 + 2t = 225$$

$$T = 225 - 50 = 87.5$$

Total time = 50 + 87.5 = 137.5 sec



4. Time taken at 10km

$$= \frac{45}{10} = 4.5 \ hrs$$

Time taken at 15km/hr

$$^{45}/_{15} = 3hrs$$

*Total time taken* = (4.5 + 3) = 7.5

$$(4.5 + 3) = 7.5 \, hrs$$

Average speed

$$= 90/7.5$$

= 12km/hr

5.  $D = 5 \times 80 + 50$ 

4

1000

= 100.05km

Speed = 120 - 80 = 40 km/h

$$T = D = \frac{100.05}{S}$$

$$S = 40$$

$$= 2.50125 hours$$

(b) 
$$D = S xT = 120 + \underline{100.05} + \underline{199}$$
  
 $4000 - 800$   
 $= \underline{120 \times 11000}$   
 $40000$ 



(c) Total time = 
$$\frac{330}{80}$$
  
=  $\frac{4^{1}}{8}hrs$   
Time lapse =  $\frac{41}{5} + \frac{100.05}{40000} + \frac{199}{800}$   
=  $\frac{41}{8} - 4$   
 $\frac{1}{8} = \frac{1}{8}hrs$ 

6. a) Distance traveled by bus before the matatu started off the journey is

Distance = speed x time  
= 
$$60 \times 2 \frac{1}{2}$$
  
=  $150 \text{km}$ 

Relative speed = 100-60 = 40km/hr

The matatu would cover the bus head start of 150km in 150/40 hrs = 3.75hrs = 3hrs 45 min  $\therefore$  The matatu will overtake the bus after 3hrs 45 minutes This will be 1:15 + 3:45 = 5.00pm

b) Time taken by the matatu to complete the remaining  $350km = 350/100 = 3 \frac{1}{2} hrs$  = 3hours 30 minutes

Time taken by the bus to complete the remaining 350 =  $\frac{350}{60} = \frac{5^5}{6}$  hrs = 5 hours 50 minutes Matatu waits for 5hr 50min – 3hr 30 min = 2 hrs 20 min

7. 
$$Total\ distance = 100 + 140 + 150 = 490$$
  
 $Total\ speed = 88 + 164 = 252\ km/hr$   
 $252\ km/hr\ into\ m/h = 252\ x\ 1000 = 70m/h$   
 $3600$ 

*Time taken* =  $^{490}/_{70}$  = 7 *sec* 

8. Distance = 
$$(5 + 15)m = 20m$$
 =  $0.02km$   
 $S \Rightarrow Bus = 40 \text{ km/h}$   
Trailer =  $xkm/h$   
Relative speed =  $(40 - x) \text{ km/h}$   
 $T = 4.8 \text{ sec.} = 4.8h$ 

3600

$$S = \frac{D}{T}$$

$$(40 - x) = \frac{0.02}{48}$$

$$3600$$

$$\approx \frac{0.02 \times 3600}{48}$$

$$= 15 \text{ km/h}$$

$$40 - x = 15$$

$$x = 25 \text{ km/h}$$

9. 
$$L.C.M = 2^4 \times 3^2 \times 5^3 = 1800$$



10. Total distance = 60 cmTotal time taken =  $3^{-1}/5 \text{ hrs}$ Let speed in still water be x km/hSpeed upstream = (x - 5) km/hSpeed downstream = (x + 5) km/h

$$\frac{30}{x-5} + \frac{30}{x+5} = \frac{16}{5}$$

$$30x - 150 + 30x + 150 = \frac{16}{5}(x^2 - 25)$$

$$5$$

$$300x = 16x^2 - 400$$

$$x = -\frac{5}{4} \text{ or } 20$$

.: Speed in still water is 20 km/hr

- 11. When David left, Ojwang had covered  $15 \times 3/2 = 22.5 \text{ km}$ .

  a) (i) Remaining dist. = 40 22.5 = 17.5 kmRelative speed = 15 + 25 = 40 km/hTime taken before meeting = 17.5 = 0.4375 hrs40

  Ojwang covered  $15 \times 0.437 = 5.5625 \text{ km}$ Distance from Ojwang's house  $= 22.5 + 6.5625 \text{ } \checkmark$  = 29.0625 km
  - (ii) 0.4375 = 26 min 15 sec  $\therefore \text{ They met at } 10.30 + 26.15$ = 10.56.15 am.
  - (iii)  $40 29.0625 \sqrt{\phantom{0}} = \underline{10.9375 \text{ km}} \sqrt{\phantom{0}}$
  - b) Time take =  $\underline{10.9375} \lor = 0.9115 \text{ hrs}$  12 = 54 min, 41 sec.They arrived at 10.56. 15 + 54.41 + 10 min= 12.00.  $56 \text{ pm. } \checkmark$
- *12*. In 10minutes Kamau has travelled (a)  $10 \times 24 = 6km$ 60 Distance left = 42 - 6 = 36km Relating speed = 24 + 50.4k/hr= 74.4 km/hr*Time taken to meet* = 42= 0.565 hrs74.4 = 34minutes Time for meeting is 6.10 34 6.44a.m  $34 \times 50.4 = 28.56 \text{km from R or } 13.44 \text{ from S}$ 60



(b) Kamau arrival time

$$\frac{42km}{24km/hr} = 1.75hrs$$

$$1hr.45 minutes$$

(c) Mrs Ronoh speed = 
$$\frac{D}{T}$$
  
= 50.4km/hr  
Twice = 50.4 x 2 = 100.8  
7.00a.m, Mr. Kamau covered = 1x24= 24km  
Retain speed = 100.8- 24 = 76.8km/hr  
So 24 = 8.75  
76.8  
He was overtaken at 7.00

s overtaken at 
$$7.00$$
  
 $+ 18.75$   
 $7.18am$   
At distance of  $D = S x t$   
 $= 100.8 \times 189.75$   
 $60$ 

31.5km from S or 10.5km from R

13. i) A gains on B at the rate of (72 − 56) Km/hr or 16km/h
: in 1 hr A gains on B 16km
In 545 A gains on B
16 X 1000 X 54 m = 240

The sum of the lengths of the two trains is 240m but the length of the first train is 100m The length of the second train is 140m

ii) Relative speed = (72 + 56) km/h = 128km/hr

Distance between A and B decrease at the rate of 128km/hr

The distance decreases by 240m

$$\frac{60 \times 60 \times 240}{128 \times 1000} s = \frac{27}{4} seconds 
= 63/4 s$$

14. (a) 
$$Time = \underline{D}$$

$$S$$

$$= \underline{5}$$

$$x hrs$$

(ii) 
$$Time = \frac{7}{x + 24} hrs$$

$$(b) \frac{5}{x} - \frac{36}{60} = \frac{7}{x + 24}$$

$$\frac{7}{x + 24} = \frac{25 - 3x}{5x}$$

$$35x = 25x - 3x^{2} + 600 - 72x$$

$$3x^{2} + 82x - 600 = 0$$

$$(3x + 100)(x-6) = 0$$

$$x = -100 \text{ or } 6$$

 $His\ speed = 6km/hr$ 

(c) Time = 
$$\stackrel{\frown}{S} x T$$
  
=  $\stackrel{\frown}{5} x 60$   
= 50mins

15. a) Relative speed = 
$$80 - 60$$
  
=  $20 \text{ km/h}$   
Time =  $\frac{40}{20} \text{ hrs}$   
=  $20$ 

(b) 
$$1.50 \text{ p.m.} = 13.50 \text{ hrs.}$$
  
 $Time = 13.50 + 2 = 15.50 \text{ hrs.}$ 

16. (a) Nairobi 400km Kisumu 
$$Speed = 120km/h$$

$$Distance = 400km$$

$$Time\ taken = 400 = 10 = 3hrs\ 20min$$

$$120$$

$$8.30 + 3hrs\ 20min = 11:50a.m$$

(b) at 8.30a.m distance covered by bus = 
$$\frac{1}{2}x \ 80 = 40$$
km

Dist. Left =  $360$ km speed =  $200$ km/h

Time taken =  $\frac{360}{200}$  =  $1$ hr  $48$ mins

 $\frac{200}{100}$ 

They met at  $8:30+1$ hr  $48$ mins

=  $10:18$ a.m

(c) 
$$8 - 10.18a$$
.m is  $2hrs\ 18mins\ distance = 2\ x\ 80 +  $\underline{18}\ x\ 80$$ 

$$= 160 + 24km = 184 \text{ from Nairobi}$$
(d) car arrived in Nairobi after 3hrs 20mins
Bus traveled a time of 3hrs 20mins + 30mins
3hrs 50mins
Dist. =  $3 \times 80 + 50 \times 80 = 240 + 66^{2}/3$ 

Distance from Kisumu =  $93^{1/3}$  km

17. Total distance = 
$$25m$$
Relative speed=  $54km/hr$ 
To  $m/s = \left[\frac{54 \times 1000}{60 \times 60}\right] = 15/ms$ 

Time they met =  $\left(\frac{25}{15}\right)$ 
=  $1^2/3$  sec

## 41. Quadratic expressions and equation 2



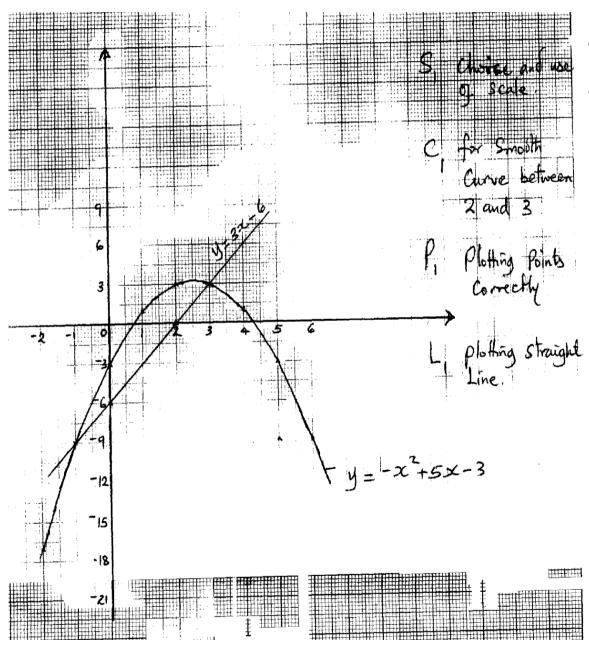
§ 1.	
(a)	

х	-2	-1	0	1	2	3	4	5	6
У	-17	-9	-3	1	3	3	1	-3	-9

(b) 
$$y = 5x - x^2 - 3$$
  
 $\frac{0 = 5x - x^2 - 3}{y = 0}$   
 $x = \frac{0.75 \text{ or } 4.3 \pm 0.1}{(c) \ y = 5x - x^2 - 3}$   
 $\frac{0 = 2x - x^2 + 3}{y = 3x - 6}$   
 $\frac{x \ 0 \ -1 \ 2}{y \ -6 \ -9 \ 0}$ 

For all  $\sqrt{\text{values of y B1}}$  for at least 5  $\sqrt{\text{values}}$ .

$$x = -1 \text{ or } 3 \pm 0.1$$



2.  $x-2.5-\sqrt{3}$   $x-2.5+\sqrt{3}=0$ 

$$x^{2} - 2.5x + x\sqrt{3} - 2.5x + 6.25 - 2.5\sqrt{3}$$
  
 $x\sqrt{3} + 2.5\sqrt{3} = 0$ 

$$x\sqrt{3} + 2.5 \ \sqrt{3} = 0$$
$$x^2 - 5x + 6.25 - 3 = 0$$

$$x^2 - 5x + 3.25 = 0$$

$$4x^2 - 20x + 13 - 0$$

$$4x^2 - 20x + 13 = 0$$

$$17.35 \times 13.85 = 240.3$$

$$17.35 X 13.75 = 237.2$$
  
 $\therefore 17.3 X 13.8 = 238.7$ 

$$240.3 - 238.7 = 1.5$$

$$238.7 - 237.2 = 1.6$$

$$= 1.6 + 1.5 = 3.1$$

$$\frac{5+1.5}{2} - \frac{5.5}{2}$$

= 1.55

Product

Last product Max err =

$$error = 1.55 \times 100 = 0.6\%$$

$$Relative err =$$

4.

х	-6	-5	-4	-3	-2	-1	0	1	2	3	4
у		04	-2		-8	-8		-2	4	12	

(c) (i) 
$$x^2 + 3x - 6 = 0$$

$$x = -4.5 \text{ or } 1.5 \pm 0.2$$

$$(ii) y = x^2 + 3x - 6$$

$$x^2 + 3x - 2$$

$$y = -4$$

$$x = 5 \text{ or } 4 \pm 0.2$$

5.

х	-4	-3	-2	-1	0	1	2	3
ν	21	10	3	0	1	6	15	28

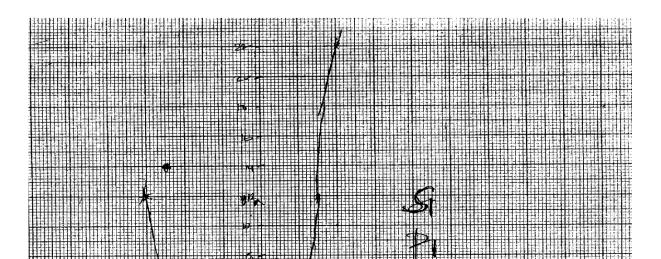
$$(c) 2x^2 + 3x + 1 = 0$$

$$2x + 4x - 3 = 0$$

$$-x + 2 = y$$

$$x = 0.6 \text{ or } x = -2.6 \pm 0.1$$

(*d*) 
$$x = 0.30 - x = -1.8 \pm 0.1$$





*ii)* 
$$\left(\frac{480,000}{x-4}\right) / = \frac{1}{x-4}$$

$$b) \qquad \frac{480,000}{x-4} = \frac{480,000}{x} + 20,000$$

Multiply all hr' by L.C.M.  $480,000x = 480,000(x-4) + 20,000(x^2-4x)$ Dividing by 10,000

$$48x = 48x - 192 + 2x^{2} - 4x$$

$$48x - 48x + 4x - 2x^{2} + 192 = 0$$

$$4x - 2x^{2} + 192 = 0$$

$$x = -b + \sqrt{(b^2 - 4ac)}$$

$$= -4 + \sqrt{1552}$$

$$= -4 + 39.3954$$

$$= -4 + 39.3954 \text{ or } x = -4 - 39.3954$$

$$-4 \text{ But } x \text{ cannot } be -ve \text{ hence}$$

$$x = -43.3954 = 10.8489$$

c) Original: new cont.

= 11

d) Size of land bought = 6 hectares  $\underline{6} = 0.857143$ 

ge 27.

	1	П	П		1	1
$\boldsymbol{\mathcal{X}}$	-3	-2	-1	0	1	2
у	13	4	-1	-2	1	8

(iii)  $y = 2x^2 + x - 2$  $0 = 2x^2 + 2x - 3$ 

	<i>y</i>	$\lambda + \lambda$	L			
X	-3	-2	-1	0	1	2
y	5	3	2	1	0	-1

$$y = 2x^{2} + x - 2$$

$$0 = 2x^{2} + x - 5$$

$$y = 3$$

8. (a) Dist. traveled in 3hrs s. drawing Plane  $A - 400 \times 3 = 1200 \text{km} - \text{cm}$ Plane  $B - 500 \times 3 - 7.5 \text{cm}$ Plane  $C - 300 \times 3 = 900 \text{km} - 4.5 \text{cm}$ 

(b) Dist.  $BA = 12.8 \ 0.1 \ x \ 200 = 2560 km \ 20 km$   $T = \frac{D}{S} = \frac{2560}{500} hrs$   $= 5.12 hrs \ of 5 hrs, 7.2 mns$   $\approx 5 hrs, 7 min \ (nearest min)$ 

(c) Bearing of B from  $C = 360^{\circ} - 20^{\circ} = 340^{\circ}$ Dist.  $BC = (10.9 \pm 0.1 \times 200) km$  $= 2180 km \pm 20 km$ 

9. *a*)

х	-2	-1.5	-1	-0.5	0	0.5	1	
$x^2$	4	2.25	1	0.25	0	0.25	1	
<i>4x</i>	-8	-6	4	-2	0	2	4	

 4
 4
 4
 4
 4
 4
 4
 4
 4

 y
 0
 0.25
 9
 2.25
 4
 6.25
 9

$$A = \frac{1}{2}h \left\{ (y_1 + y_7) + 2(y_2 \dots y_6) \right\}$$

$$= \frac{1}{2}x \frac{1}{2} \left\{ (0+9) + 2(0.25+9+2.25+4+0.2) \right\}$$

$$= \frac{1}{4} \left\{ 9+4.25 \right\} \sqrt{$$

$$= 13.25 \text{ sq. units } \sqrt{}$$

b) 
$$\int_{2}^{0} (x^2 + 4x + 4) dx + \int_{0}^{1} (x^2 + 4x + u) dx$$

$$\left(\underline{x^3} + 2x^2 + 4x\right) + \left(\underline{x^3} + 2x^2 + ux\right) \sqrt{224}$$

 $=\frac{9}{Error} \sqrt{}$   $Error = 13.\overline{25} - 9 = 4.125$ 

$$\% = 4.125 \quad \sqrt{x \, 100}$$

a)

Х	-2	-1.5	-1	-0.5	0	0.5	1	
$x^2$	4	2.25	1	0.25	0	0.25	1	
4x	-8	-6	4	-2	0	2	4	

$$A = \frac{1}{2}h \left\{ (y_1 + y_7) + 2(y_2 \dots y_6) \right\}$$

$$= \frac{1}{2}x \frac{1}{2} \left\{ (0+9) + 2(0.25+9+2.25+4+0.2) \right\}$$

$$= \frac{1}{4} \left\{ 9+4.2 \right\}$$

$$= \frac{1}{4} \left\{ 9 + 4.2 \right\}$$
  
= 13.25 sq. units  $\sqrt{\phantom{0}}$ 

b) 
$$\int_{2}^{0} (x^2 + 4x + 4) dx + \int_{0}^{1} (x^2 + 4x + u) dx$$

$$\left(\frac{x^{3}}{3} + 2x^{2} + 4x\right) + \left(\frac{x^{3}}{3} + 2x^{2} + ux\right) \checkmark$$

$$= (-\frac{8}{3} + 8 - 8) + (\frac{1}{3} + 2 + 4) \checkmark$$

$$= \frac{9}{13.25 - 9} \checkmark$$

$$Error = 13.25 - 9 = 4.125$$

$$Error = 13.\overline{25} - 9 = 4.125$$

$$\% = 4.125 \sqrt{x 100}$$

 $y = 2x^2 - 4x - 5$ 

2	$x^2 - 4$	x-5							y	=2x	+3					
	X	-3	-2	0	1	2	3	4	5			x	-4	-2	0	2
	$2x^2$	18	2	0	2	8	18	32	50			у	-5	-1	3	7
	<i>4x</i>	-12	-8	-4	0	4	8	12	16	20						
	5	5	5	5	5	5	5	5	5	5						

25

y (a) x = 1

(b)  $-0.9 \times 2.8$ 

$$x = -1 \text{ and } x = 4$$

12.

*11*.

X	-	-1	0	1.5	2	2.5	3.5

-5

	1.5						
Y	-4	0	5	5	3	0	-9



(0.75, 6.125)

Y = -2

*Range of values -1.3,* < x < 2.75

Integral values; -1, 0, 1, 2

*13. a)* 

<u>u</u> )							
X	-4	-3	-2	-1	0	1	2
$2x^2$	32	18	8	2	0	2	8
4x-3	-19	-15	-11	-7	-3	1	5
у	13	3	-3	-5	-3	3	13

(b)Roots for 
$$x = -2.6 \pm 0.1$$
  
  $x = 0.6 \pm 0.1$ 

$$y = 2x^2 + 4x - 3$$

$$\frac{0=2x^2+x-5}{y=3x+2}$$

Roots read from the 2 pts of intersection of the line and curve.

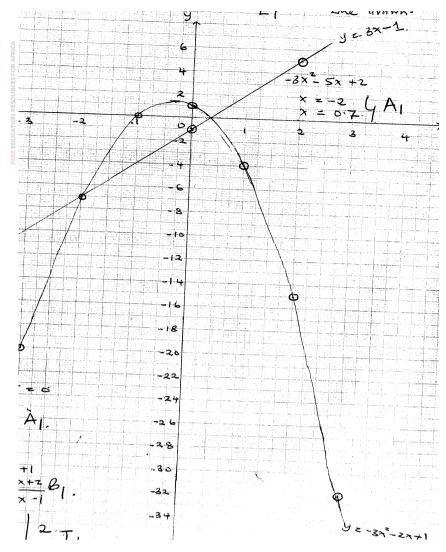
$$X = -1.9 \pm 0.1$$

$$X = 1.4 + \overline{0.1}$$

14.

х	-3	-2	-1	0	1	2	3
$-3x^2$	-27	-12	-3	0	-3*	-12	-27*
		*					
-2x	6	4	2	0	-2	-4	-6
	*		*		*	*	
1	1	1	1	1	1	1	1
у	-20	-7	0	1	-4	-15	-32
		*	*		*		*





$$\begin{vmatrix}
1 - 2x - 3x^2 &= 0 \\
x &= -1 \\
or x &= 0.7
\end{vmatrix}$$

$$\begin{vmatrix}
y &= -3x^2 - 2x + 1 \\
0 &= -3x^2 - 5x + 2 \\
y &= o + 3x - 1
\end{vmatrix}$$

$$\begin{vmatrix}
x & 0 & 2 \\
y & -1 & 5
\end{vmatrix}$$

$$T_1$$

15. 
$$x^{2} + ax - b = 0$$
$$(x-1)(x+5) = x^{2} + ax - b$$
$$x^{2} + 4x - 5 = x^{2} + ax - b$$
$$a = 4, b = 5$$

16. Let 
$$a = 1.5 + \sqrt{2}$$
  
 $b = 1.5 - \sqrt{2}$   
 $\therefore (x - a)(x - b) = 0$   
 $x^2 - xb - ax + ab = 0$   
 $x^2 - x(1.5 - \sqrt{2}) - x(1.5 + \sqrt{2}) + ab = 0$   
 $x^2 - 1.5x + x\sqrt{2} - x(1.5x - \sqrt{2}) = 0$ 

2.

$$x^{2}-3x + ab$$

$$x^{2}-3x + (1.5 + \sqrt{2})(1.5 - \sqrt{2}) = 0$$

$$x^{2}-3x + 2.25 - 2 = 0$$

$$x^{2}-3x + \frac{1}{4} = 0$$

$$4x^2 - 12x + 1 = 0$$

a) i) 
$$a^2 + b^2 = 89$$
  $a + b = 13$   
 $a^2 + 2ab + b^2 = (a + b)^2 = 13^2 = 169$ 

*ii)* 
$$2ab = 169 - 89$$
  
= 80

*iii*) 
$$a^2 - 2ab + b^2 = a^2 + b^2 - 2ab$$
  
=  $89 - 80 = 9$ 

*iv)* 
$$(a-b)2 = 9$$
  $a-b = \pm 3$ 

$$b) a + b = 13$$

$$\underline{a - b = 3}$$

$$2a = 16$$

## 42. Approximation and errors

1.  $Maximum\ perimeter = 2(12.05 + 8.05) = 40.2cm$   $Actual\ perimeter = 2(12.0 + 18.0) = 40.0cm$  Error = 40.2cm - 40.0cm = 0.2cm $\%error = (0.2\ x100)$ 

$$A = \frac{1}{2}$$
  $x 12 x 8 = 48$ 

i) Absolute error =  $[\frac{1}{2}x12.5 \times 8.5 - \frac{1}{2}x \times 11.5 \times 7.5]$ 

3. A = L x W $A = x (14-x) = 14x - x^2$ 

$$\frac{dA}{dx} = 14 - 2x = 0$$
$$14 = 2x, x = 7$$

= 10.4%

Maximum area = 
$$7(14 - 7)$$
  
=  $7x 7 = 49cm^2$ 

Shortest possible length of 2<sup>nd</sup> piece



5. Absolute error  $10 \pm 0.05$  and  $15 \pm 0.05$ 

 $Max \ area = 10..5 \ x \ 15.05$ 

 $Min\ area = 9.95\ x\ 14.95 = 148.7525$ 

$$a.e = \frac{150.2525 - 15 + 150 - 148.7525}{2}$$

$$= 1.25$$
% error =  $\frac{1.25}{150} \times 100$ 

$$= 0.8333\%$$

6. 
$$17.35 \times 13.85 = 240.3$$
  
 $17.35 \times 13.75 = 237.2$   
 $\therefore 17.3 \times 13.8 = 238.7$   
 $Max \ err$   $240.3 - 238.7 = 1.5$   
 $Min \ err$   $238.7 - 237.2 = 1.6$   
 $Max \ err$   $= \frac{1.6 + 1.5}{2} = \frac{3.1}{2} = 1.55$   
 $Last \ product$   $240$   
 $Max \ err$   $= 1.55$   
 $Relative \ err$   $= \frac{1.55}{28.1\%}$   
 $error = \frac{1.55}{238.7} \times 100 = 0.6\%$   $28.1$   
 $Relative \ err$   $= \frac{1.55}{238.7}$ 

8.

<u> </u>													
X	$0^{\circ}$	<i>3</i> °	60	90	120°	150°	180°	21	24	270°	300°	330°	360°
			0	0				$0^{\circ}$	$0^{\circ}$				
Cos x	1	0.87	0.	0	-0.5	0.87	-1.0	-	0.5	0	0.5	0.87	1
			5					0.					
								87					
$2\cos(x+30)$	1.73	1	0	-	-1.73	-2.0	-1.73	-	0	1	1.73	2.00	1.73
				1.				1.					
				0				0					

b) i) Amplitude of 
$$y = \cos x$$
 is 1 unit  
And  $Y = 2\cos(x + 30)$  2 units

ii) period of 
$$y = 2 \cos(x + 30^\circ)$$
  
330°

c) 
$$Cos x = 2 cos (x + 30^{\circ})$$

$$x = 40^{\circ} \pm 1$$
$$x = 219^{\circ} \pm 1$$



$$y + x = 12 + 6$$

$$y - x = 18$$

$$= 18$$

$$= 9$$

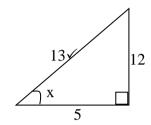
Correct substitution

Simplification

CAO

## 43. Trigometry 2

1. 
$$5 \sin x + \cos x$$
  
 $= 5 \left[ \frac{12}{13} \right] - \frac{5}{13}$   
 $= \frac{60}{13} - \frac{5}{13} = \frac{55}{13}$   
 $= \frac{12}{15}$ 



2. 
$$\frac{2 \cos 3\theta}{1} = \frac{1}{2}$$

$$\cos 3\theta = 0.5$$

$$3\theta = \cos^{-1}0.5$$

$$\frac{3}{3}\theta = \frac{60^{\circ}}{3}, \frac{300^{\circ}}{3}, \frac{420^{\circ}}{3}, \frac{66^{\circ}}{3}, \frac{78^{\circ}}{3}, \frac{102^{\circ}}{3}$$

$$\therefore \theta = 20^{\circ}, 100^{\circ}, 140^{\circ}, 220^{\circ}, 260^{\circ}, 340^{\circ}$$

 $\sqrt{Identification}$  of exact number of quadrants to satisfy the equation.  $\sqrt{Values}$  of at least 4 soln. of  $\theta$ 

3.. 
$$\frac{1/2}{\sqrt{3}/2} \frac{X^{\sqrt{3}/2}}{X^{1/\sqrt{2}}}$$

$$\frac{\sqrt[4]{4}}{\sqrt[4]{2} - \sqrt[1]{2}} X \frac{\sqrt[4]{2} + \sqrt[1]{2}}{\sqrt[4]{2} + \sqrt[1]{2}}$$

$$\frac{\frac{3/8 + \sqrt{3}/4\sqrt{2}}{3/4 - 1/2}}{\frac{3/8 + \sqrt{3}/4\sqrt{2}}{1/4}} = \frac{\frac{3/8 + \sqrt{3}/4\sqrt{2}}{1/4}}{\frac{1}{4}}$$

4. a) 
$$b^2 = a^2 + c^2 - 2ac \cos B$$
  
 $b^2 = 7^2 + 5^2 - 2.5... 7 \cos 100$   
 $= 74 - 70(-0.173648)$   
 $= 74 + 12.15537$   
 $b^2 = 86.15537$   
 $b = 9.28199$   
 $AC = 9.3 \text{ km}$ 

$$AC = 9.3 \text{ km}$$
b)  $9.3 = 5$ 
 $\sin 100 = \sin \theta$ 

$$Sin \ \theta = \frac{5 \ sin \ 100}{9.3} = 0.529466$$
  
 $\theta = 31.9694$ 

$$\theta \simeq 32^{0}$$
  
 $32 - 20 = 12^{0}$   
 $Bearing = 360^{0} - 12^{0}$  = 348<sup>0</sup>

Teacher.co.ke

c)  $020^{0}$ 

$$Sin \overline{60} = \sqrt{3}/2 \qquad 1$$

$$Sin \overline{45} = \frac{1}{\sqrt{2}} - \frac{\sqrt{3}}{\sqrt{2}} \cdot \frac{1}{\sqrt{2}} - \underline{1}$$

$$= \underline{1}$$

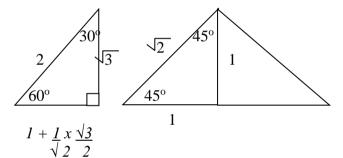
$$= \frac{1}{\sqrt{3}} - \frac{1}{\sqrt{2}}$$

$$= \frac{\sqrt{6}}{5} - \frac{\sqrt{2}}{2}$$

$$= \underline{\sqrt{6}} - 2\sqrt{2}$$

$$= 4$$

6.



$$1 + \sqrt{3} \times 2 \frac{\sqrt{2}}{2\sqrt{2}}$$

$$2\sqrt{2} \times 2 \frac{\sqrt{2}}{2\sqrt{2}}$$

$$\frac{1}{1} + \frac{2\sqrt{6}}{4}$$

$$\frac{4+2\sqrt{6}}{4}$$

7. 
$$\frac{\sqrt{5}(2\sqrt{2} + \sqrt{5}) + \sqrt{2}(2\sqrt{2} - \sqrt{5})}{(2\sqrt{2})^2 - (\sqrt{5})^2}$$

$$\frac{2\sqrt{10+5+4-\sqrt{10}}}{8-5}$$

$$\frac{9+\sqrt{10}}{3}$$

$$3+\frac{1}{3}\sqrt{10}$$

8. a) 
$$b^2 = a^2 + c^2 - 2ac \cos B$$
  
 $b^2 = 7^2 + 5^2 - 2.5... 7 \cos 100$   
 $= 74 - 70(-0.173648)$   
 $= 74 + 12.15537$   
 $b^2 = 86.15537$ 

$$b = 9.28199$$
  
 $AC = 9.3 \text{ km}$ 



b) 
$$\frac{9.3}{\sin 100} = \frac{5}{\sin \theta}$$

$$Sin \ \theta = \frac{5 \ sin \ 100}{9.3} = 0.529466$$
 $\theta = 31.9694$ 
 $\theta \simeq 32^{0}$ 
 $32 - 20 = 12^{0}$ 
 $Bearing = 360^{0} - 12^{0}$ 
 $= 348^{0}$ 

c)  $020^{0}$ 

### 44. Surds

1.. 
$$\frac{3}{\sqrt{7}-2} + \frac{1}{\sqrt{7}} = \frac{3}{7} + \frac{7}{2} + \frac{\sqrt{7}}{7}$$

$$\frac{3}{\sqrt{7}-2} + \frac{1}{\sqrt{7}} = \frac{3\sqrt{7}+7-2}{\sqrt{7}}$$

$$\frac{3}{\sqrt{7}-2} + \frac{7}{\sqrt{7}} = \frac{3\sqrt{7}+7-2}{\sqrt{7}} = \frac{3\sqrt{7}+7-2}{\sqrt{7}} = \frac{3\sqrt{7}+7-2}{\sqrt{7}} = \frac{3\sqrt{7}+7-2}{\sqrt{7}} = \frac{49-28}{21}$$

$$= \frac{(4\sqrt{7}-2)7+27}{21}$$
2.

 $\frac{2 + \sqrt{5}}{2 - \sqrt{5}} - \frac{3 + \sqrt{5}}{2 + \sqrt{5}} = a + b\sqrt{5}$   $\frac{4 + 45 + \sqrt{5} - (6 - 3\sqrt{5} + 2\sqrt{5} - 5)}{4 - 5}$   $\frac{8 + 5\sqrt{5}}{2 - 1}$ 

$$a = -8 \quad b = -5$$

4. 
$$(\sqrt{2-1})^2 = 2\sqrt{2} + 1\sqrt{3} = 2$$
$$(\sqrt{2-1})^3 = 2 - 1(\sqrt{3-2} + 2)$$

$$= 5 2 - 7$$

$$\frac{2 - \sqrt{2}}{5\sqrt{2-7}} x \frac{5\sqrt{2+7}}{5} = 2\sqrt{2+7} - 2\sqrt{2+2}$$

$$= 17\sqrt{2-6} = -6+1\sqrt{2}$$

$$(2-3)(3+2)$$

$$3(2)2-2)2$$

$$3x2-3+2-2$$

$$9x2-4x3$$

$$6-3+2-6$$

$$18-12=6$$

6. i) 
$$Or = 16^2 - 5^2$$

$$= 256 - 25$$

$$= 15.198 \text{ cm}$$
ii)  $tan \theta = 5.066 = 1.2665$ 

$$\therefore \theta 51.71^0$$

7. 
$$\log_{10} 5 - \log_{10} 10^2 + \log_{10} (2y + 10) = \log_{10} (y - 4)$$

$$Log 10 \{5 (2y + 10)\} = log 10 (y-4)$$

$$10^{2}$$

$$10y + 50 = 100 y - 400$$

$$90 y = 450$$

$$y = 5$$

8. 
$$\frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}} \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} - \sqrt{2}}$$

$$= 3 - \sqrt{6} - \sqrt{6} + 2$$

$$3 - \sqrt{6} + \sqrt{6} - 2$$

$$= 5 - 2\sqrt{6}$$

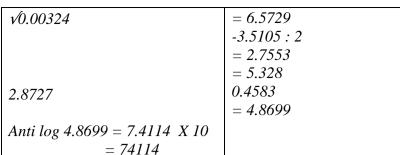
$$= 5 - 2\sqrt{6}$$

$$= 5 - 2\sqrt{6}$$

## 45. Further logarithms

1. No Log 3.2865 X 2

√0.00324	= 6.5729
	-3.5105 : 2
	= 2.7553
	= 5.328
2.8727	0.4583
	= 4.8699
Anti $log 4.8699 = 7.4114 \times 10$	
= 74114	



*a) monthly taxable pay;* 

15% of monthly salary = 
$$^{15}/_{100} \times 20000$$

= kshs.3000

 $Monthly\ pay = Kshs.(20000 + 3000 - 700)$ 

= Kshs. 22300

In Kenya pounds =  $\frac{22300}{20}$ 

= KE 1115

b) Total tax payable (Gross tax)

$$1 - 342$$
\_\_\_\_\_\_  $342x2 = Kshs.684$ 

$$1027 - 1368$$
  $89x5 = Kshs.445$ 

 $Total\ tax = Kshs.3523$ 

- c) Net tax
  - = Gross tax relief
- = Kshs.(3523 600) = Kshs.2923
- d) Net pay;

$$= Kshs.20000 - (2923 + 2100 + 200 + 2/100 \times 20000)$$
  
=  $Kshs. (20000 - 5623)$  =  $Kshs.14377$ 

*Number of periods* = 8

 $400,000 (1-0.08)^8 = 205288$ 

6 month depreciation rate = 8%

3.

4.

5. N. 
$$\log_{3^6} \frac{2^5 \times 2^7}{3^6} = \log_{3^6} \frac{2^{12}}{3^6}$$
$$= \log_{3^6} \left(\frac{2^2}{3}\right)^6 = \left(\frac{4}{3}\right)^6$$

$$\begin{bmatrix}
D; \log \frac{2^5 \times 2^l}{3^3} & \frac{2^6}{3^3} & \frac{2^6}{3^3} & \frac{2^2}{3^3} &$$

$$Log\left(\frac{4}{3}\right)^3$$

$$= 6 \log 4$$

$$3 \log 4$$

$$3 \log 4$$

$$6/3 = 2$$

$$Log (x+5) = log(4)$$

$$(x+2)$$

$$x + 5 = 4$$

$$x + 2$$

$$(x+5) (x+2) = 4$$

$$x^{2} + 2x + 5X + 10 = 4$$

$$x^{2} + 7x + 6 = 0$$

$$x^{2} + 6x + x + 6 = 0$$

$$x(x+6) + 1(x+6) = 0$$

$$(x+1) (x+6) = 0$$

$$x = -1 \quad x = -6$$

7. 
$$a = 100$$
  
 $r = \underline{200} = 2$   
 $100$   
 $\underline{a(r^n - 1)} > Sn$   
 $r - 1$   
 $\underline{100(2^n - 1)} > 3,100$   
 $2 - 1$   
 $2^n - 1 > 31$   
 $2^n > 32$   
 $2^n > 2^5$   
 $n > 5$   
 $n = 6$   
8. a)  $2 \underbrace{\begin{array}{c} 3 & 5 & 7 \\ 2 & 32 & 52 & 72 \\ 3 & 23 & 53 & 73 \\ \hline 5 & 25 & 35 & 75 \\ 7 & 27 & 37 & 57 \\ \end{array}}_{7}$ 

b)  $P(E) = \underline{4}$ 

9. 
$$\begin{aligned}
&= \frac{1}{4} \\
&= \frac{1}{4} \\
&= \frac{1}{4} \\
x^2 + y^2 - 6x = 3 - 4y \\
x^2 - 6x + \left(\frac{-6}{2}\right)^2 + y^2 + 4y + \left(\frac{4}{2}\right)^2 = 3 + \left(\frac{-6}{2}\right)^2 + \left(\frac{4}{2}\right)^2 \\
&= \frac{(x - 3)^2 (y + 2)^2}{(x - 3)^2 (y + 2)^2} = 3 + 9 = 4 \\
&= \frac{(x - 3)^2 (y + 2)^2}{(x - 3)^2 (y + 2)^2} = 16
\end{aligned}$$

$$C(3, -2)$$

Gradient 
$$\Delta y = 7 - -2 = 3$$

$$10. \quad A = P(1 + \frac{r}{100})^{n}$$

$$= 10000 (1 + \frac{4}{100})^{6}$$

$$= 10000(1.04)^{6}$$

$$= 12653.19 \quad (12,653)$$



12. 
$$Log_{10} 5^2 - log_{10} 2^3 + log 2^5$$

$$Log_{10} \left( \underbrace{25 \times 32}_{8} \right)$$

$$1$$

$$Log_{10} 100 = log_{10}^{10}$$

$$= 2 log_{10}^{10}$$

$$But log_{10}^{10} = 1$$

$$\therefore = 2$$

 $\sqrt{Application}$  of logarithmic laws.  $\sqrt{Application}$ 

13.  $Log \ \frac{3x+8}{2^3} = log (x-4)$ 

$$3x + 8 = 8(x - 4)$$

$$3x + 8 = 8(x - 4)$$

$$3x + 8 = 8x - 32$$

$$-5x = -40$$

$$x = 8$$

Division of logs.

Dropping logs and simplification.

C.A.O

C.A.O

## 46. Commercial Arithmetic 2

1. After 
$$1^{st}$$
 year =  $\frac{95}{100}$  x 4200000)  
=  $Shs.357,000$   
After  $2^{nd}$  year =  $(\frac{87}{2}x 357000)$   
 $100$   
=  $sh310590$   
After  $3^{rd}$  year =  $(\frac{88}{2}x 310590)$   
 $100$   
=  $shs.273319.20$   
After  $4^{th}$  year =  $(\frac{91}{2}x 273319.20)$   
 $100$   
=  $shs.248720.50$   
After  $5^{th}$  year =  $(\frac{248720.50}{2}x 93)$   
 $100$   
The next 6years

 $A = 231310 (1-0.05)^6 = 170034.10$ 

= shs.231310

 $(n \ 140000 = 170034.10 \ (1-0.04)^n$   $(1-0.04)^n = 140000 = 0.8234$ Teacher.co.ke

```
Then 140000 = 170034.10 (1-0.04)^n

(0.96)^n = \underline{140000} = 0.8234

170034.10

n = \underline{log \ 0.8234}

log \ 0.96

= \underline{0.0844} = 4.76yrs

0.01773
```

Total no. of years = 5 + 6 + 4.76yrs

= *15.76years* 

D

В

Е

Gross 
$$tax = 4830 + 1120 + 600 = sh 6550 \ per month$$
Annual gross  $tax = 6550 \ X \ 12 = 78,600$ 

$$100 \quad 100 \quad 100$$

$$15 \ X \ 120,000 = sh.18,000$$

$$100 \quad 25 \ X \ 120,000 = sh. 30,000$$

$$100 \quad Re. \ tax = 78600 - (12000 + 18000 + 30000)$$

$$= 78600 - 60,000 = 18,6000$$

$$\frac{35}{100} \quad X \ x = 18,600$$

$$0.35x = 18,600$$

$$x = sh 53142.86$$

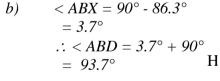
$$Taxable income \ p.a = 36,000 + 53142.86$$

$$= sh.412142.86$$

$$Monthly \ salary = \frac{413142.86}{12000} + 12,000$$

$$12 \quad = 34428.57 + 1200 = Sh 35628.57$$

3. a)  $Sin 86.3^{\circ} = {^{XB}/_{AB}}$   $Sin 86.3^{\circ} = {^{XB}/_{30}}$   $XB = 30sin86.3^{\circ}$ XB = CD = 29.93746855



c)  $< DBF \ obtuse = 360^{\circ} - 187.4^{\circ}$ = 172.6°

Arc DEF =  $^{\theta}/_{360} \pi D$  or  $^{\theta}/_{360} x2 \pi r$ But  $\cos 86.3^{\circ} = {}^{AX}/_{AB}$ 

Cos  $86.3^{\circ} = \frac{AX}{30}$ 

 $AX = 1.935969248 \ cm$ 

$$DB = 16 - 1.935969248 = 14.06403075 cm$$
  

$$\therefore Arc DEF = \frac{172.6^{\circ}/360^{\circ}}{360^{\circ}} x^{22}/7 x 14.06403075$$

$$= \frac{106807.8751}{2520}$$

$$= 42.38407742 cm$$

Arc CGH

16cm

86.3°

G

30cm

$$< reflex CAG = 360^{\circ} - (2x 86.3^{\circ})$$
  
= 187.4°



: Arc CGH = 
$${}^{187.4^{\circ}}/{}_{360^{\circ}}$$
 x2 x  ${}^{22}/{}_{7}$  x 16  
=  $\frac{131,929.6}{2520}$   
= 52.35301587 cm

Total length of belt to go round the belt

$$= CD + DEF + GF + CHG$$
  
= 29.93746855 + 42.38407742 + 29.93746855 + 52.35301587  
= 154.6120304 cm

$$4. \qquad \angle ABD = 31^0$$

$$\angle CBD = 37^{\circ}$$

5. 
$$A = 15,000(1 + \frac{8}{100})^7$$
  
=  $Ksh.25,707$ 

$$Amount = 18 \times 2000$$

$$A = P \left( \frac{1}{100} + r \right)$$

$$6,000 = 24000 \left( \frac{1}{100} + r \right)^{18}$$

$$\frac{36000}{24000} = \begin{pmatrix} 1 + \frac{r}{100} \end{pmatrix}$$

$$\frac{3}{2} = \left(\frac{1}{00} + r\right)$$

$$1 + r = 100$$

$$1 + r = 1023$$

$$1 + \underline{r} = 1.023$$

$$\frac{r}{100} = 0.023$$

let sales in 3rd bracket be y

$$^{10}/_{100} \times 5000) + (^{15}/_{100} \times 3000) + (^{20}/_{100} \times y) = 1668$$

$$500 + 450 + 0.2y = 1668$$

$$0.2y = 1668 - 950 = 718$$

$$y = \frac{718}{0.2} = 35\%$$

 $Total\ sales = (8000 + 3590)$ 

$$= shs.11590$$

8. Find the principal which in 12 years at 5% p.a compound interest amounts to sh.450,00

$$A = P (I + \underline{R})^{n}$$

$$100$$

$$I = A - P$$

$$A = (100 + \underline{R})^n$$

$$100$$

$$I = P (100 + \underline{R})^n - P$$

$$100$$

$$= P (100 + R/100)n - 1$$

$$450000 = P = 450000 = 565397$$



a)  $Taxable\ income = (25000 + 12000 + 3000) = 40000$ 

b) Income tax

 $10164 \text{ x}^{2}/_{20} = \text{Shs.} 1016.40$ 

 $10164 \ x^{3}/_{20} = Shs.1524.60$ 

 $10164 \text{ x}^{4/20} = \text{Shs.} 2032.80$ 

Remaining:

 $9508 \ x^{5}/_{20} = Shs.2377$ 

Total tax payable p.m

= 6950.8 - 1162 = Shs.5788.80

- c) Annual tax payable =  $5788.80 \times 12 = Shs.69465.60$
- 10. (a) taxable income = Kshs. 25000 + Kshs.10480 = Kshs. 35480

b) tax charged:

 $1^{st} 4350 = 4350 \times \frac{2}{20} = 683.25$ 

 $2^{nd} 4555 = 4555 x^{3}/_{20} - 683.25$ 

 $3^{rd} 4555 = 4555 \times \frac{4}{20} - 911$ 

 $4^{th} 4555 = 4555 \times \frac{5}{20} - 1138.75$ 

*Rem.*  $17465 = 17645 \times 6/20 - 5239$ 

 $Total\ tax - 8407.5$ 

800.00 7607.50

(c)  $40/100 \times 35480 - 14.192 = 49672$ 

New income = 35480 + 14192 = 49672

Remainder = 49672 - 18015 = 31657

 $Tax\ charged = 31657\ x\ 6/20 = 12665.1$ 

 $Total\ tax = 12665.1$ 

% increase in income  $ax = 4257.6 \times 100$ 

7607.5 = 55.97%

11.  $A = P(HR/100)^n$ 

 $500000 = P(1 + \underline{20})^5$ 

100

 $500,000 = (^{120}/_{100})^5$ 

500,000 = P

 $(1.2)^5$ 

P = Shs.200,938.786  $\approx shs. 200,939$ 

12. Principal = 26,000 - 6,000 = 20,000

*Total H.P instalments* =  $1045.3 \times 24 = 25087.20$ 

$$25087.20 = 20,000 \left( \frac{1}{100} + r \right)^2$$

$$1.254 = \begin{pmatrix} 1 + \underline{r} \\ 100 \end{pmatrix} 2$$

$$1.120 = 1 + r$$

$$\underline{r} = 0.12 \text{ or } 12\%$$

= K 28071 p.a

```
13. No. of periods = 12

r = 4\% per period

A = 1.0412 \times 15000

= 24015.5
```

14. a) i)  $taxable\ income = 19200 + 12000 + 1300 + 2300 = 34800$ 

b) Net tax

$$8400 \ x^{2}/_{20} = 840$$

$$9600 \ x^{3}/_{20} = 1440$$

$$12000 \ x^{4}/_{20} = 2400$$

$$4800 \ x \ 5/_{20} = \underline{1200}$$

$$5800$$

Net tax = 5800 - 1240= 4560

c) Net salary = 34800 - (4560 + 5530) = 24710

15. (a) 9000 + 350 + 800 + 1200 = 11350

(b) 9000 + 3000 = 12000

(c)  $Total\ taxes = 12000\ x\ 12$ = shs.144000p.a

Taxes

 $450 \times 2 = shs.9000$ 

 $3000 \times 3 = shs.9000$ 

 $3000 \times 4 = shs.12000$ 

 $3000 \times 5 = shs.15000$ 

 $3000 \times 6 = \underline{shs.18000}$ 

Shs.63,000

144000 - 63000 = shs.81000

7y = 81000y = 11571

 $Taxable\ income = 4500 + 3000\ x\ 4 + 11571$ 

 $Gross\ salary = shs.\ 561420p.a$ 

(d)  $Total \ allowances = 12000 \ x \ 12$ 

= 144,000

 $Basic\ salary = 561420$ 

14400

Shs.417,420

Monthly basic pay = shs. 34785

16. (a) Net tax 5512 Add relief 1162

Tax payable 6674

 $Tax \ on \ 9680 \ earned$  $9680 \ X^{10/}_{100} = 968$ 

Tax on 9120 earned

 $9120 x^{15}/_{100} = Shs. 1368$ 

Tax on next  $9120 \times \frac{20}{100} = Shs. 1824$ 

Tax on next 9120  $x^{25}/_{100} = 2280$ 



Total 
$$968 + 1368 + 1824 + 2280 = 6440$$
  
 $6674 - 6440 = 234$   
Let x be charged at  $30\%$   
 $^{30}/_{100} X x = 234$   
 $X = \underline{234 \times 100} = Shs.780$   
 $30$ 

Total chargeable Income 780 + (9120 x 3) + 9680 = 37820 Salary 37820 - 15220 = Shs.2260 per month.

- b) Net salary (37820 1270 6674) = Shs.298<u>76</u>
- 17. a)  $1^{st}$  year after dep. Of 20%  $800\ 000\ x\ 80$  100  $= Khs.\ 640,000...$

2<sup>nd</sup> year after dep. of 5% = 640000 x <u>95</u> 100 = 608,000 .....

The next 3 yrs

$$\begin{array}{ll}
\mathbf{n} \\
A = P \left( 1 - \underline{R} \\ 100 \right) &= 608,000 \left( 1 - \underline{10} \right)^{3} \\
= 698\,000\,(0.9) \\
= Sh.\,\,443,232 \\
800,000 - 443,232 &= Sh.\,\,356,768 \\
\end{array}$$

(b)  $S.I = 3000 x^{15}/_{100} x 2$ =  $Sh 900 \dots$ 

$$A = 3000 \left( 1 + \frac{15}{100} \right)$$

$$= 3000 \left( 1.15 \right)^{2}$$

$$= sh \ 3067.50$$

18. (i) Taxable Income  $\left(\frac{115}{100}x 24800\right) + 12000 - 1220$  = 28520 + 12000 - 1220 = Ksh.39,300 = K£ 1965 p.m.

 $\begin{array}{rcl}
- & \times & 1705 & p.m. \\
(ii) & Tax & due & 325 & x & 2 & = sh & 650 \\
650 & x & 3 & = sh & 1950 \\
325 & x & 5 & = sh & 1725 \\
325 & x & 6 & = sh & 1950 \\
340 & x & 7.50 & = sh & 2250
\end{array}$ 

# Total tax = $\underline{sh. 8825 P.m}$ ...... without relief



(ii) Net income = 
$$sh (24800 + 1200 - 12596)$$
 =  $sh 24,204 P.m$ ....

b) 
$$124\% = 37200$$
  
 $100\% =$   
 $C.P = \underline{100} \times 37200$   
 $124$   
 $= 30000$ 

c) 
$$A = 30000 (1 + {}^{18}/{}_{100})^2$$
  
=  $30000 (1.18)^2 = 41772$   
Total interest =  $41772 - 30000 = 11772$ 

20. (a) (i) 
$$(10, 500 + 6,500) \times \underline{12} = K \pounds 10,20 \ p.a$$

$$= Shs. \ 4156.70$$
(b) Net monthly pay
$$17000 - 320 + 2 x 17000$$

$$= 17000 - 660$$

$$= Kshs \ 16 \ 340.00$$

## 47. Circles –chords and tangents

1. a) i) 
$$ii)  $< BAO = 50^{\circ}$   
Acute angle  $AOB = 80^{\circ}$   
 $\therefore obtuse \ angle = 360 - 80 = 280^{\circ}$$$

b) Area of the sector =  $({}^{80}/_{360}x {}^{22}/_{7}x 7 x 7) = 34.22cm^2$ Area of the  $\Delta = {}^{1}/_{2}x 7 x 7 x sin80 = 24.13cm^2$ Area of the shaded segment =  $34.22 - \frac{24.13}{10.09cm^2}$ 



$$< COB = 2 \times 50 = 100^{\circ}$$
  
 $< OCA = < OAC = 180 - 100 = 40$   
 $\therefore < BAC = 180 - (50 + 70)$   
 $= 60$ 

3. 
$$PB. PA (PT)^{2}$$

$$PB = PT$$

$$PA$$

$$4 = 12$$

$$12 \quad 4 + 2r$$

$$\frac{4(4+2r)}{4} = \frac{12^2}{4}$$

$$4+2r=36$$

$$2r=32$$

$$r=16 cm$$

4. (a) 
$$\angle BOE = 2 \angle BCE = 2 \times 20^{0} = 40^{0}$$
  
(b)  $\angle BOE = 40^{0}$   
 $\angle BEC = \frac{1}{2} (360^{0} - 60^{0}) = 150^{0}$ 

Angels subtended at the centre is twice at the Circumference.

c) 
$$\angle CEF = 90^{0} - 80^{0} = 10^{0}$$

$$d) \angle BCO = \angle CBO = 60^{0}$$

Base angles isosceles triangle.

$$\angle OXC = 180^{0} - (60^{0} + 20^{0})$$
  
=  $100^{0}$ 

e) 
$$\angle BCE = 20^{0}$$
  
 $\angle CXE = 180^{0} - 100^{0} = 80^{0}$   
 $\angle CEX = 80^{0}$   
 $\angle OEF = 180^{0} - (80^{0} + 50^{0} + 10^{0})$   
 $= 40^{0}$ 

5. (a) 
$$PQ = \sqrt{8^2 - 2^2}$$
  
= 60  
= 7.746cm

(b) 
$$\angle PAS = 2\cos^{-1}$$
  
=  $151^{\circ}$   
::  $Reflex \angle PAS = 209^{\circ} OR \ 360^{\circ} - 151^{\circ} = 209^{\circ}$ 

(c) Length PYS = 
$$\frac{209}{360}$$
 x 2 x 6 = 21.89cm  
360  
Length QXR =  $\frac{151}{200}$  x 2 x 4 = 10.54cm



(d) Length of belt = 
$$7.74 \times 2 + 21.89 + 10.54$$
  
=  $47.92cm$ 

a) i) In 1 hr; Tap A fills  $\frac{1}{3}$ B -  $\frac{1}{4}$ Capacity filled in 1 hr =  $\frac{1}{3} + \frac{1}{4}$ =  $\frac{7}{12}$   $\frac{7}{12} = 1$  hr

1 = 1 x 1 x  $\frac{12}{7}$ =  $1\frac{5}{7}$  hrs.

ii) 
$$\frac{1}{3} + \frac{1}{4} - \frac{1}{6} = \frac{5}{12} \implies in \ one \ hr$$
  
 $\frac{5}{12} = 1hr$   
 $1 = 1 \times 1 \times \frac{12}{5}$   
 $= 2 \frac{2}{5} hrs$ 

7. 
$$\angle ABD = 31^{\circ}$$

$$\angle CBD = 37^{\circ}$$

8. 
$$x(x+9) = 4x9$$
$$x^{2} + 9x - 36 = 0$$
$$(x^{2} - 3x) + (12x - 36 = 0)$$
$$x(x-3) + 12(x-3) = 0$$
$$(x+12)(x-3) = 0$$
$$x - 3 = 0$$
$$x = 3 \text{ only}$$

9. 
$$PO. OQ = BO.OA$$
  
 $8 x 6 = 4.5 x y$   
 $y = 8x 6$   
 $4.5$   
 $= 10.67$ 

10.  $< DGB = < ABG = 40^{\circ} (alt.seg <, s)$   $a) < DGE = < DBE = 25^{\circ} (< s \text{ in same segment})$  b) < EFG  $< GEB = 40^{\circ}, = < BDG \text{ and } < BED = 45^{\circ} = < BGD$   $\therefore In \Delta GED, < GDE = 180 - (25 + 40 + 45) = 70^{\circ}$   $\therefore < GFE = 180 - 70 = 110^{\circ} (Sup \text{ angles})$   $d) Angle CBD \text{ in } \Delta BGE, Angle GBE = 180 - (110) = 70^{\circ}$   $\therefore Angle CBD = 180 - (40 + 70 + 25) = 45^{\circ}$   $Or Angle CBD = Angle BGD = 45^{\circ} (Angles \text{ in Alt segment})$   $e) Angle BCD \text{ in } \Delta BCD, Angle BDC = 70^{\circ} Angles \text{ in a straight line}$   $\therefore Angle BCD = 180 - (70 + 45) Angles \text{ of a triangle} = 65^{\circ}$ 

11. 
$$(a)Sin\theta = \frac{4.5}{8} = 0.5025$$
  
 $\theta = Sin^{-1} 0.5625$   
 $= 34.23^{\circ}$ 

$$\angle Apb = 68.46^{\circ}$$
 $Sin \alpha = \underline{4-5} = 0.75$ 
 $6$ 
 $\alpha = Sin-10.75$ 
 $= \angle 48.59^{\circ}$ 
 $\angle Aqb = 97.18^{\circ}$ 

(b) Area Of Segment PAB =  $\frac{68.46}{360}$  X  $\frac{22}{7}$  X 8 X 8  $-\frac{1}{2}$  X 8 Sin 68.46  $\frac{360}{360}$  7 = 38.25 - 29.77 = 8.48cm<sup>2</sup>

Area Of Segment AQB =  $\frac{97.18}{360}$  X  $\frac{22}{7}$  X 36 Sin 97.18  $\frac{360}{360}$  7 = 30.65 - 17.86 = 12.68cm<sup>2</sup>

Area of quadrilateral APBQ =  $\frac{1}{2}$  64 sin 68.46 +  $\frac{1}{2}$  x 36sin 92.18 = 29.77 + 17.86 = 47.63 Shaded area = 47.63 - (8.48 + 12.68) = 26.47cm<sup>2</sup>

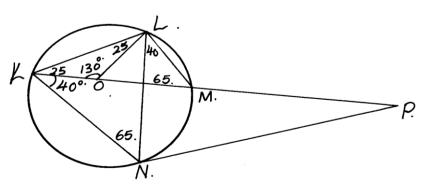
12.  $CBD = 90 - 42 = 48^{\circ}$ Angle of triangle add to  $180^{\circ}$   $DOB = 180^{\circ} - 42 = 138^{\circ}$ Opposite angles of cyclic quadrilateral add to  $180^{\circ}$ 

$$DAB = \underline{138}^o = 69^o$$

Angle at circumference is half the nagle substended at centre by same chord

CDA ABD = 90 - 48 = 420 ADB = 180 - (69 + 42)  $180 - 111 = 69^{\circ}$   $CDA = 90 + 69^{\circ}$   $Show \ \Delta ADB \ is \ asoccesters$   $\angle DAB = 69^{\circ}$   $\angle ADB = 69^{\circ}$   $\angle ADB = 69^{\circ}$   $\angle ABD = 42^{\circ}$ So two angles are equal hence it is asoccesters

*13*.

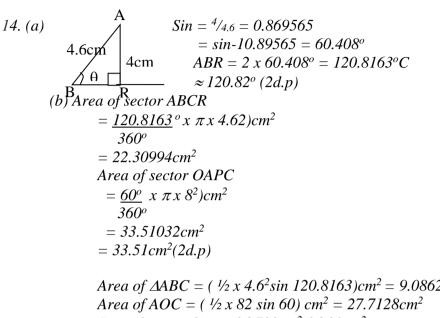


a)  $MLN = 40^{\circ}$  angles subtended by same chord in the same segment are equal.

b) 
$$OLN = 90 - 65 = 25^{\circ}$$



- c) LNP =  $65^{\circ}$  exterior  $\Delta$  is equal to opposite interior angle or angle by two a chord and a tangent is equal to angle subtended by the same chord in the alternate segment.
- d) MPN =  $180 170 = 10^{\circ}$  angle sum of a  $\Delta$  is  $180^{\circ}$
- e)  $LMO = 65^{\circ}$  angles subtended by same chord.



Area of 
$$\triangle ABC = (\frac{1}{2}x + 4.6^2 \sin 120.8163)cm^2 = 9.08625cm^2$$
  
Area of  $AOC = (\frac{1}{2}x + 82 \sin 60) cm^2 = 27.7128cm^2$   
Sum of area of  $\triangle s = 36.799cm^2 + 36.80cm^2$   
.: Area of shaded part = area of sectors - area of  $\triangle s$   
=  $(22.31 + 33.51 - 36.80)cm^2 = 19.02cm^2(2dp)$ 

- 15. (a)  $\angle TDC = ABT$  (exterior opp. angle of a cyclic quadrilateral) =  $100^{\circ}$ 
  - (b) BAT = ATB (base s of isosceles ATB) =  $180 - 100 = 40^{\circ}$
  - (c)  $\angle TCD = \angle X TD$  (angles in alternate segments) =  $60^{\circ}$

Or 
$$\angle BTC + 40^{\circ} = 100^{\circ} (exterior \ angle \ of \ a \ \Delta)$$
  
 $\angle BTC = 100^{\circ} - 40^{\circ} = 60^{\circ}$ 

(d) 
$$DTC = 180^{\circ}$$
-  $(58^{\circ} + 100^{\circ})$  (angles in  $\Delta TDC = 12^{\circ}$ 

16. a) 
$$GBD = 90^{\circ}$$
  
 $ABG = 180 - (90 + 36)$   
 $= 180 - 126 = 54^{\circ}$   
 $GEB = ABG = 54^{\circ}$ 

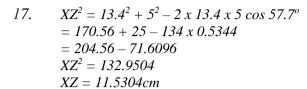
b) 
$$BED = CBD = 36^{\circ}$$

c) 
$$DGE = FEG = 20^{\circ}$$
  
 $OEB = 90 - (36 + 20)$   
 $= 90 - 56 = 34^{\circ}$ 

$$OBE = OEB = 34^{\circ}$$

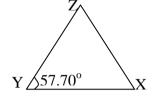
*d*) 
$$BGE = 36 + 20 = 56^{\circ}$$

e) 
$$GFE = 180 - EDG$$
  
=  $180 - 70 = 110^{\circ}$ 



(ii) 
$$2R = 11.5304$$
  
 $Sin 57.7^{\circ}$   
 $2R = 11.5304$   
 $0.8453$   
 $2R = 13.60866$ 

R = 6.08043cm



18. 
$$52 = 62 + 62 - 2 \times 6 \times 6 \cos A$$
  
 $72 \cos A = 72 - 25 = 46$   
 $Cos A = \frac{46}{72} = 0.6389$   
 $A = Cos-1 \ 0.6389 = 50.29^{\circ}$   
Area of the minor sector APQ  
 $= \frac{50.29}{360} \times 3.142 \times 6^{2}$   
 $= 15.801 \text{cm}^{2}$   
Area of the triangle APQ  $= \frac{1}{2} \times 6 \times 6$   
Area of the minor segment  $= (15)$ 

Area of the triangle APQ =  $\frac{1}{2} \times 6 \times 6 \sin 50.29 = 13.847 \text{cm}^2$ Area of the minor segment =  $(15.801 - 13.847) \text{cm}^2 = 1.954 \text{cm}^2$ Area of triangle PBQ  $\sqrt{6.5 (6.5 - 4) (6.5 - 4) (6.5 - 5)}$   $\sqrt{6.5} \times 2.5 \times 2.5 \times 1.5 = 7.806 \text{cm}^2$ Area of shaded region =  $(7.806 - 1.954) \text{cm}^2 = 5.852 \text{cm}^2$ 

19. a) 
$$\angle PQR = 180^{\circ} - 75^{\circ}$$
  
= 105°. NPQR is cyclic quadrilateral.

(b) 
$$\angle NRP = 90^{\circ} -75^{\circ}$$
  
= 15°, Third angle of  $\triangle NRP$ .

$$\angle PRS = 180^{\circ}$$
 -65°, Angles on a = 115°, straight line.

$$\therefore \angle QSR = 180^{\circ} - (115^{\circ} - 35^{\circ})$$

$$= 30^{\circ}, 3^{rd} \text{ angle of triangle PRS.}$$

(c) Reflex 
$$\angle POR = 2 \angle PQR$$
  
=  $2 \times 105^{\circ} = 210^{\circ}$ 

### (d) $\angle MQR = \angle MNR = 40^{\circ}$

#### Subtended by same chord MR

20.

- (a)  $\angle TDC = 100^{\circ}$  (Cyclic quadrilateral)
- (b)  $\angle TCB = 40^{\circ}$  (Cyclic quadrilateral)
- (c)  $\angle TCD = 58^{\circ}$  (Cyclic quadrilateral)
- (d)  $\angle BTC = 60^{\circ}$  (Sum angle of a  $\triangle$  add upto  $180^{\circ}$ )
- (e)  $\angle DTC = 22^{\circ}$  (angle sum of a straight line add upto  $180^{\circ}$ )

21. 
$$4 \times 10 = 5(5 + x)$$
  
 $40 = 25 + 5x$   
 $3 = x$ 

22. 
$$T_{11} = a + 10d$$
  
 $T_2 = a + d$   
 $a + 10d = 4a + 4d$  ......(i)  
 $3a - 6d = 0$   
 $57 = \frac{7}{2} \{ 2a + 6d \} = 175$  ...(ii)  
 $2a + 6d = 50$   
 $3a - 6d = 0$   
 $5a = 50$   
 $a = 10$   $d = 5$ 

23. 
$$CBE = 40^{\circ}$$
 (alt.segiment theoren)  
 $\angle BCE = 120^{\circ}$  (Suppl. To  $BCD = 60^{\circ}$ alt. seg.)  
 $\therefore (40 + 120 + E) = 180^{\circ}$  (Angle sum of  $\Delta$ )  
 $\angle BEC = 20^{\circ}$ 

24. Taxable income p.a = 36,000+53142.86=sh.412142.86Monthly salary = 413142.86 + 12,00012

$$= 34428.57 + 1200 = Sh\ 35628.57$$

25. a) (i) 
$$\angle PTQ = 180^{\circ} - 56^{\circ} = 124^{\circ}$$
  
 $124 + 38 = 162^{\circ}$   
 $180^{\circ} - 162^{\circ} = 18^{\circ}$   
 $90^{\circ} + 18^{\circ} = 108^{\circ}$   
 $180^{\circ} - 108^{\circ} = 72^{\circ}$   
 $180^{\circ} - (72^{\circ} + 56^{\circ}) = 52^{\circ}$   
 $\angle PRS = 52^{\circ}$ 

 $(ii) \angle RSQ = \angle RPQ = 18^{\circ}$ 

$$(ii) \ge KSQ = \ge KPQ$$

b) 
$$A \propto B$$
.  $\frac{1}{C^3}$ 

$$A = \underbrace{K.B}_{C^3}$$

$$12 = \underbrace{3K}_{2^3}$$

$$K = \underbrace{42 \times 8}_{S} = 32$$

$$\vdots \quad A = \underbrace{32B}$$

√Value of the constant.

√Substitution √Formulation

Values of constants. √Substitution

$$\frac{10 \times (1.5)^3}{32} = B$$

B = 1.055



c)  $y = K + Mx^2$  where K and M are constants 7 = K + 100 M  $100 \times 0.005 + K = 7$  5.5 = K + 400M -0.5 + K = 71.5 = 300M K = 7.5

$$M=0.005$$

$$y = 7.5 - 0.005 \times 18^{2}$$

$$y = 7.5 - 1.62$$

$$y = 5.88$$
a)  $PN^{2} = 5^{2} - 4^{2}$ 

$$PN = 3cm$$

$$QN^{2} = 6^{2} - 4^{2}$$

$$QN = 4.47cm$$
∴  $PQ = 3 + 4.47 = 7.47$ 

b)i) < APB  

$$Sin \frac{1}{2} \theta^{4}/5 = 0.8$$
  
 $\frac{1}{2} sin \theta = 53.13$   
 $< APB$ 

ii) 
$$Sin \frac{1}{2} \propto = \frac{4}{6} = 0.6667$$
  
 $\frac{1}{2} \propto = 41.81$   
 $\propto 83.62$   
 $\therefore < AQB = 83.62^{\circ}$ 

c) Area of the shaded region – Area of the segments = 
$$\frac{106.3}{360} \times \frac{22}{7} \times 5^2 - \frac{1}{2} \times 5 \times 5 \sin 106.3$$
  
=  $\cancel{p}3.19 - \cancel{1}1.998 = 1\cancel{p}.192$   
 $\frac{83.6}{360} \times \frac{22}{7} \times 6 \times 6 - \frac{1}{2} \times 6 \times 6 \sin 83.6 = 8.38$   
 $\frac{360}{7} \times 7$   
Total 11.192 + 8.38 = 19.52

27. Using cosine rule
$$7.8^{2} = 6.6^{2} + 5.9^{2} - 2 \times 6.6 \times 5.9 \cos R$$

$$Cos C = 6.6^{2} + 5.9^{2} - 7.8^{2}$$

$$2 \times 6.6 \times 5.9$$

$$= 43.59 + 34.81 - 60.84$$

$$77.88$$

$$= 17.53 - 0.2251$$

$$77.88$$

$$\angle C = 77^{\circ}$$

$$\frac{7.8}{5in 77} = 2 \times \sin 77$$

$$= 4cm$$

$$Area of circle = 3.142 \times 4^{2} = 50.27$$

$$A \ge a of \qquad PQR = \frac{1}{2}(6.6)(5.9) \sin 77$$

$$= 18.97$$

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a) 
$$\angle PAQ = 2 \ PAB = 42^{\circ} \ x \ 2 = 84^{\circ}$$
  
 $\angle PBQ = 2 \ \angle ABQ = 30^{\circ} \ x \ 2 = 60^{\circ}$ 

 $AB = 42^{\circ} \times 2 = 84^{\circ}$   $BQ = 30^{\circ} \times 2 = 60^{\circ}$   $\sqrt{}$   $APQ = 84 \times 22 \times 6 \times 6 = 264 \text{ cm}^2$ 

(b) (i) Area of sector APQ = 
$$\frac{84}{360}$$
 x  $\frac{22}{7}$  x 6 x 6 = 26.4 cm<sup>2</sup>  
Area of sector PBQ  $\frac{60}{360}$  x  $\frac{22}{7}$  x 8 x = 33.5 cm<sup>2</sup>

√ diff. areas

√**a**ngle √angle

(ii) Area of 
$$\triangle APQ = \frac{1}{2}x 6x 65$$
:-  $84^{o} = 18x 0.9945$ 

 $84^{\circ} = 18 \times 0.9945$   $\sqrt{\text{diff. areas}}$ = 17.9 cm<sup>2</sup> Exp. for total

Area of 
$$\triangle$$
 PBQ =  $\frac{1}{2}x \ 8 \ x \ 85$ : =  $60^{\circ} = 32 \ x \ 0.8660$   
=  $27.7 \ cm^2$ 

√answer.

= area of sector APQ - area of triangle APQ

 $= 26.4 - 17.9 = 8.5 \text{ cm}^2$ 

2<sup>nd</sup> circle, shaded area

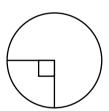
= area of sector PBQ – area of  $\triangle PBQ$ 

$$= 33.5 - 27.7 = 5.8 \text{ cm}^2$$

Total shaded area = 8.5 + 5.8

 $= 14.3 \text{ cm}^2$ 

### 29. $\underline{90}$ x 3.142 x 2 x 6.5 $\underline{360}$ $\underline{10.2115 cm}$ = 10.21 cm



## 48. Matrices

1. 
$$\begin{pmatrix} 3 & 2 \\ 4 & -1 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} 12 \\ 5 \end{pmatrix}$$

$$\begin{pmatrix}
\frac{1}{11} & \frac{2}{11} \\
\frac{4}{11} & \frac{-3}{11}
\end{pmatrix}
\begin{pmatrix}
3 & 2 \\
4 & -1 \\
6
\end{pmatrix}
=
\begin{pmatrix}
\frac{1}{11} & \frac{2}{11} \\
\frac{4}{11} & \frac{-3}{11}
\end{pmatrix}
\begin{pmatrix}
12 \\
5
\end{pmatrix}$$

Premultiplication by the inverse.

Simplification.

C.A.O

$$\frac{4}{11} \quad \frac{-3}{11}$$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$a = 2$$
 $b = 3$ 



$$a = 2 \sqrt{and b} = 3 \sqrt{and b}$$

2. 
$$(x-3) - (2x) = 0$$
  
 $x-3-2x = 0$   
 $-2x + x - 3 = 0$   
 $-x - 3 = 0$   
 $x = 3$ 

$$3a + 2c = 9$$

$$2a + 2c = 2$$

$$a = 7$$

$$c = -6$$

$$3b + 2d = -3$$

$$2b + 2d = 1$$

$$b = -4$$

$$d = 4.5$$

$$A = \begin{pmatrix} 7 & -4 \\ -6 & 4.5 \end{pmatrix}$$

5. 
$$20x(-3-8)$$
  
 $100 \text{ area of } 1^{st} \text{ image.}$   
 $100 x(4-3)$   
 $700 \text{ area of } 2^{nd} \text{ image}$   
6.  $Det. 9+2=11$ 

$$A^{1} = \frac{1}{11} \begin{pmatrix} 3 & -2 \\ 1 & 3 \end{pmatrix}$$
$$\begin{pmatrix} 3 & 2 \\ 3 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 10 \\ 4 \end{pmatrix}$$
$$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{11} \begin{pmatrix} 3 & -2 \\ 1 & 3 \end{pmatrix} \begin{pmatrix} 10 \\ 4 \end{pmatrix}$$
$$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 22 \\ 1 \end{pmatrix}$$

$$\left( \begin{array}{c} x \\ y \end{array} \right) = \left( \begin{array}{c} 2 \\ 2 \end{array} \right)$$

$$PQ = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 2 & -3 \\ -1 & 2 \end{pmatrix} \quad \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ -3 \end{bmatrix}$$

$$\begin{pmatrix} 2 & 3 \\ 1 & 2 \end{pmatrix} \quad \begin{pmatrix} 2 & -3 \\ -1 & 2 \end{pmatrix} \quad \begin{bmatrix} x \\ y \end{bmatrix} = \begin{pmatrix} 2 & 3 \\ 1 & q \end{pmatrix} \begin{pmatrix} 5 \\ -3 \end{pmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$x = 1 \quad y = -2$$

$$\frac{1}{2}x - \frac{1}{4}y = -2$$

8. 
$$\frac{1/2}{2}x - \frac{1}{4}y = 2$$
  
 $\frac{2}{5} + \frac{1}{6} = 6$   
 $2x - y = 8$ 

$$12x + 5y = 180$$

$$10x - 5y = 40 \qquad + \qquad$$

$$22x = 220$$

$$x = 10$$

$$\frac{1}{4}y = \frac{1}{2}(10)^{-2}$$

$$\frac{1}{4}y = 5-2 = 3$$

$$Y = 12$$

9. 
$$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\begin{pmatrix} -1 & -2 & -6 \\ 1 & 4 & 9 \end{pmatrix}$$

$$= \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} X^{1} & Y^{1} & Z^{1} \\ -1 & -2 & -6 \\ 1 & 4 & 9 \end{pmatrix}$$

Final image  $X^{11}$   $Y^{11}Z^{11}$ 

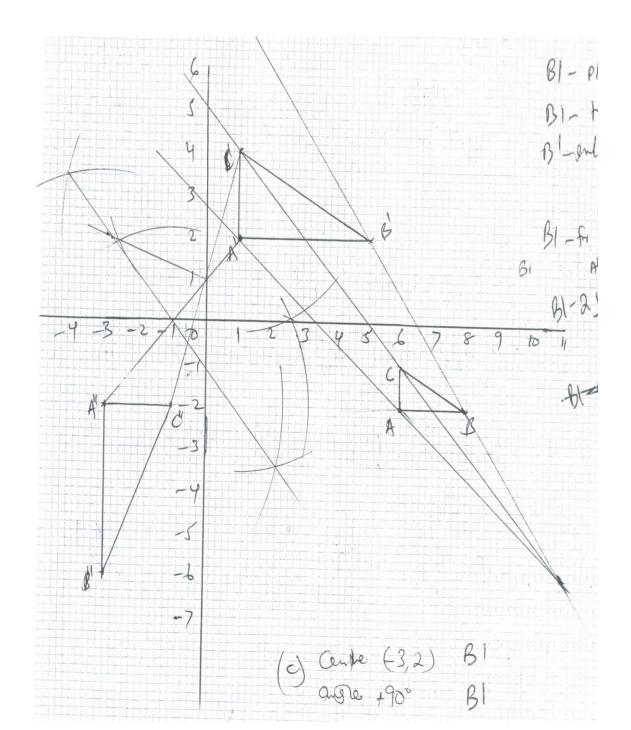
$$X^{11}(1, -1) Y^{11}(4, -2), Z^{11}(9, -6)$$



10.

(c) Centre (-3,2)

$$\begin{array}{ccc} & & & Angle + 90^{o} \\ & & A & B & C \\ a) & \begin{pmatrix} 2 & 4 \\ 0 & 2 \end{pmatrix} & \begin{pmatrix} 5 & 6 & 4 \\ 1 & -1 & -\frac{1}{2} \end{pmatrix} & = \begin{pmatrix} 6 & 8 & 6 \\ 2 & 2 & -1 \end{pmatrix} \end{array}$$





11. Det 2 - -3 = 5  
Area of 
$$A^{I}B^{I}C^{I} = 5 \times 15$$
  
= 75 cm<sup>2</sup>

12. 
$$A.S.F = \underline{110} = 11$$

$$10$$

$$5X(X) - 6 = 11$$

$$5X^{2} + 6 = 11$$

$$5x^{2} = 5$$

$$X^{2} = 1$$

$$X = \pm 1$$

13. Area of the image = Area of the object x Det.

Det. 
$$(\Delta) = 15 - 18 = -3$$
  
 $54 \text{ cm}^2 = A \text{ x } -3$   
 $\frac{54}{3} \text{ cm}^2 = A$ 

Area of  $\triangle ABC = 18 \text{ cm}^2$ 

14. Det. 
$$9 + 2 = 11$$

$$A^{I} = \frac{1}{11} \begin{pmatrix} 3 & -2 \\ 1 & 3 \end{pmatrix}$$

$$\begin{pmatrix} 3 & 2 \\ 3 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 10 \\ 4 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{11} \begin{pmatrix} 3 & -2 \\ 1 & 3 \end{pmatrix} \begin{pmatrix} 10 \\ 4 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{11} \begin{pmatrix} 22 \\ 22 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$$

$$P(2, 2)$$

#### 49. Formulae and variation

1. 
$$P = kr^2$$
;  $R = MT^2$   
 $18 = 9k$ ;  $3 = 25m$   
 $K = 2$ ;  $M = \frac{3}{25}$   
 $P = 2R^2$ ;  $R = \frac{3}{25}$ ;  $T^2$   
 $P = 2 \frac{3}{25}$ ;  $T^2 = \frac{18}{625}$ ;  $T^4$ 

$$P = 18 \times 10000 = 288$$



$v^2 =$	r	
	r+c	
$v^{2}(r_{+})$	<u>c)</u> = v	(r+c)
$r \rightarrow$	<b>€</b>	
$v^{2}r +$	vc = r	
$r-v^2r$	= vc	
r(1-v)	$v^2) = vc$	
<i>r</i> =	<u>vc</u>	
1	2	

$$v^{2} (\underline{r+c}) = v \qquad (r+c)$$

$$r \neq c$$

$$v^{2}r + vc = r$$

$$r - v^{2}r = vc$$

$$r (1 - v^{2}) = vc$$

$$r = \underline{vc}$$

$$1 - v^{2}$$

$$3. \qquad X \alpha Y^{3} \Rightarrow x = KY^{3}$$

3. 
$$X \alpha \underbrace{\frac{Y^3}{Z}} \Rightarrow x = KY^3$$

$$6 = \underbrace{\frac{K(3)^3}{\sqrt{25}}}$$

$$6 = \underbrace{\frac{27K}{5}}$$

$$K = \underbrace{\frac{10}{9}}$$

$$X = \underbrace{\frac{10}{9}} \underbrace{\frac{Y^3}{\sqrt{Z}}}$$

$$X = \underbrace{\frac{10}{9}} \underbrace{\frac{(7)^3}{9}}$$

$$= \underbrace{\frac{10 \times 34^3}{27}}$$

$$= 127.04$$

(a) 
$$Y^{3} = \underbrace{9}_{10} x Z$$

$$Y = \underbrace{3}_{10} \underbrace{9}_{10} x 4 x 8$$

$$Y = 3\sqrt{\frac{144}{5}} = 3.07$$

$$(b) X_{1} = \underline{KY^{3}} \\ \sqrt{Z}$$

$$X_{2} = \underline{K(1.2y)^{3}}$$

$$\sqrt{0.64Z}$$

$$\frac{1.728KY^{3}}{\sqrt{0.8}Z} - \frac{KY^{3}}{\sqrt{Z}}$$
M<sub>1</sub>

$$\frac{\left(\frac{2.16KY^{3}}{\sqrt{Z}} - \frac{KY^{3}}{\sqrt{Z}}\right)}{\frac{KY^{3}}{\sqrt{Z}}} x 100\% \qquad M_{1}$$

$$= 116\% \qquad A_{1}$$

4. 
$$K(b-a) = ab$$

$$Kb - ka = ab$$

$$Kb - ab = ka$$

$$B(k-a) = ka$$

Removing the sg. Root.

Factorization.

C.A.O

$$B = ka$$

$$K-a$$

$$x-2.5 - \sqrt{3}$$

$$x-2.5 + \sqrt{3} = 0$$



$$x^{2} - 2.5x + x\sqrt{3} - 2.5x + 6.25 - 2.5\sqrt{3}$$

$$x\sqrt{3} + 2.5\sqrt{3} = 0$$

$$x^{2} - 5x + 6.25 - 3 = 0$$

$$x^{2} - 5x + 3.25 = 0$$

$$4x^{2} - 20x + 13 = 0$$

6. 
$$Z = \frac{Kx^2}{y}$$

$$Z = \frac{(1.2x)^2 K}{\sqrt{0.64y}}$$

$$= \frac{1.44Kx^2}{0.85y}$$

$$= 1.8 \frac{Kx^2}{y}$$
% increase = 80%

7. 
$$ar^{3} = 48$$

$$ar^{6} = 384$$

$$\therefore \underline{ar^{6}} = \frac{384}{48}$$

$$r^{3} = 8$$

$$r = 2$$

$$ar^{3} = 48$$

$$8a = 48$$

$$a = 6$$

$$Sn = \underline{a(r^{n} - 1)}$$

$$r - 1$$

$$6(2^{6} - 1)$$

$$2 - 1$$

$$= 6(64 - 1)$$

$$= 6 \times 63$$

$$= 378$$

8. 
$$P = \frac{KQ^{2}}{R}$$

$$2 = \frac{16K}{6}$$

$$K = \frac{3}{4}$$

$$P = \frac{3}{4} \frac{Q^{2}}{R} = \frac{3}{4} \times \frac{64}{4} = 12$$

9. 
$$B \& M^2 = \frac{1}{N}$$
  
 $B = Km^2 + \frac{Q}{N}$   
 $(96 = 4K + 2Q)^3$   
 $(46 = 3K + 0.5Q)^4$   
 $104 = 4Q$   
 $Q = 26$   
 $K = 11$   
 $Expression B = 11m^2 + \frac{26}{N}$ 



10. 
$$3x = y - 1 \qquad .... i$$

$$2x + 2 = 1 \qquad y - 5 \qquad 2$$

$$4x + 4 = y - 5$$

$$4x + 9 = y \qquad ... ii$$

$$3x = y - 1$$

$$4x = y - 9$$

$$-x = 9 \qquad x = -9$$

$$-27 = y - 1$$

$$y = -26$$

11. 
$$P = \underbrace{\frac{x-1}{x+2}} \Rightarrow P^{3} = \underbrace{x-1}_{x+2}$$

$$P^{3}x - 2P^{3} = x - 1$$

$$P^{3}x - x = -1 - 2p^{3}$$

$$x(P^{3} - 1) = -1 - 2P^{3}$$

$$x = \underbrace{\left(-1 - 2P^{3} \atop P^{3} - 1\right)}_{x = 1 - p^{3}} - 1$$

$$x = \underbrace{1 + 2p^{3}}_{1 - p^{3}}$$

12. 
$$a^{4} = \frac{1+d^{2}+b}{b^{2}-3}$$
$$3d^{2} = 3a^{4}b^{2} - b^{2} - 3$$
$$d = \sqrt{\frac{3a^{4}b^{2} - b^{2} - 3}{3}}$$

13. (a) 
$$Z = \frac{KX^2}{y^2}$$

$$Z = \frac{100k}{16} = 15$$

$$K = \frac{12}{5}$$

$$Z = \frac{12x^2}{5^{y^2}}$$

(b) 
$$Z = 21.90$$

14. 
$$R = kn + t\sqrt{n}$$

$$9k + 3t = 42$$

$$25k + 5t = 100$$

$$45k + 15t = 210$$

$$75k + 15t = 300$$

$$-30k = -90$$

$$k = 3$$

$$t = 5$$

*17*.



$$R = 3 (16) + S (4) = 68$$
15. 
$$a^{2} = \frac{b^{2} d^{2}}{b^{2} + d}$$

$$a^{2} b^{2} + a^{2} d = b^{2} d^{2}$$

$$b^{2} d^{2} - a^{2} b^{2} = a^{2} d^{2}$$

$$b^{2} (d^{2} - a^{2}) = a^{2} d^{2}$$

$$b^{2} = \frac{a^{2} d^{2}}{d^{2} - a^{2}}$$

$$b = \mp \boxed{\frac{a^{2} d^{2}}{a^{2} - a^{2}}}$$

16. 
$$P = KQ + m\sqrt{Q}$$

$$22 = K(4) + m(2) \dots (1)$$

$$42 = K(g) + n(3) \dots (2)$$

$$22 = 4K + 2m$$

$$42 = 9K + 3m$$

$$3(22) = 3(4K) + 3(2m)$$

$$2(42) = 2(9K) + 2(3)$$

$$66 = 12k + 6m$$

$$84 = 18K + 6m$$

$$18 = 6k = k = 3$$

$$22 = 4(3) + 2m$$

$$22 - 12 = 2m$$

$$20 = 2m$$

$$M = 10$$

$$= 3(25) + 10(5)$$

$$= 75 + 50$$

$$= 125$$

$$b^{2} = k - ac$$

$$b^{2} - k = -ac$$

$$\frac{b^{2} - k}{-9} = c$$

$$C = \frac{b^{2} - k}{-9} \quad or \ c = \frac{k - b^{2}}{9}$$

$$C = \frac{1 - 2^{2}}{4}$$

$$= {}^{-3}/_{4} = -0.75$$

$$18. \quad V = 30, \ r = 2$$

$$K = Ur^{2}$$

$$= 30 \ x \ 22 = 120$$

$$When \ r = 4$$

$$V = {}^{120}/_{42} = 7.5 \text{m/s}$$

 $b = \sqrt{k - ac}$ 

19. 
$$P = \underbrace{\frac{XY}{Z+X}}_{Z+X}$$

$$P^{3} = \underbrace{XY}_{Z+X}$$

$$Xy = P^3Z + P^3X$$
  
 $Xy - P^3X = P^3$  z  
 $X(y-P^3) = P^3$  z

$$\therefore X = \frac{P^3 z}{Y - P^3}$$
20.  $X\alpha y + \frac{1}{z^2}, x = Ky + M$   
 $X = 6, y = 3, z = 2 - 6 = 3k + M$   
 $X = 8, y = 5, z = 1 - 8 = 5k + M$   
 $X = 8 + M = 12k + M$   
 $-16 = -7k + 16k = 160$   
 $-7k + 16$ 

21. 
$$T_{11} = a + 10d$$
  
 $T_2 = a + d$   
 $a + 10d = 4a + 4d$  ......(i)  
 $3a - 6d = 0$   
 $57 = \frac{7}{2} \{ 2a + 6d \} = 175$  ...(ii)  
 $2a + 6d = 50$   
 $3a - 6d = 0$   
 $5a = 50$   
 $a = 10$   
 $d = 5$ 

22. (i) 
$$R = m + nI$$
  
 $55 = M + 20n.....(i)$   
 $58 = m + 28n.....(ii)$   
 $-3 = -8n$   
 $n = \frac{3}{8} = 0.375$   
 $55 = m + \frac{60}{8}$   
 $m = 55 - 7.5 \implies m = 47.5$   
 $R = 47.5 + 60 X^{3}/8$   
 $R = 70 \text{ ohms}$ 

23. 
$$\left(1 - \frac{1}{2}\right)^{5} = \left[1 - 2x\right]^{5}$$

$$= 1^{5} (-2x)^{o} + 5.1^{4} (-2x)^{1} + 10.1^{3} (-2x)^{2} + 101^{2} (-2x)^{3}$$

$$= 1 - 10x + 40x^{2} - 80x^{3}$$

$$(1 - 2x)^{5} = (0.98)^{5} = (1 - 0.02)^{5}$$

$$\therefore 2x = 0.02$$

$$x = 0.01$$
Thus  $(0.98)^{5} = 1 - 10(0.01) + 40(0.01)^{2} - 80(0.01)^{3}$ 

$$= 1 - 0.1 + 0.004 - 0.00008 = 0.9039$$

# 50. Sequence and series

$$P\begin{pmatrix} 1 + \underline{R} \\ 100 \end{pmatrix}$$

$$= 40,000 \begin{pmatrix} 1 + \underline{2} \\ 3100 \end{pmatrix}$$

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2. (a)  $\frac{9^{x}}{3^{2x+1}} = \frac{81}{9}$   $9^{2x} = 3^{4}(3^{2x+1})$   $3^{4x} = 3^{4+2x+1}$   $3^{4x} = 3^{2x+5}$  4x = 2x+5 2x = 5 x = 2.5

(b) Common ratio = 
$$\frac{81}{92.5}$$
  
=  $\frac{1}{3}$   
(c)  $a = 3^{(2 \times 2.5 + 1)}$   
=  $3^{6}$   
=  $729$   
 $S_{10} = 729 \left[ 1 + \frac{1}{3} \right]^{10}$   
 $\frac{1}{1 - \frac{2}{3}}$   
=  $1093.5 \times 0.99998 = 1093.5$ 

For both the 5<sup>th</sup> and 7<sup>th</sup> term

(d) 
$$5^{th} term = 729 x (^{1}/_{3})^{4}$$
  
= 9  
 $7^{th} term = 729 x (^{1}/_{3})^{6}$   
= 1  
 $a = 9 \quad d = 1 - 9 = -8$   
 $S_{20} = \left(\frac{20}{2} \quad 2 \times 9 + (20 - 1)\right)(-8)$   
=  $10 (18 - 152) = -1340$ 

$$S_n = \frac{n}{2} \left\{ 2a + (n-1) \right\} d$$

$$338 = \underbrace{n}_{2} \ 2(-12) + (n-1)_{2}$$

$$676 = \begin{cases} n - 24 + 2n - 2 \end{cases}$$

$$\frac{2n^2 - 26n}{2} - \frac{676}{2} = \frac{0}{2}$$



$$n^{2} - 13n - 338 = 0$$
  
 $(n - 26)(n + 13) = 0$   
 $n = 26 \text{ or } n = -13 \text{ reject}$   
 $\therefore n = 26 \text{ terms}$ 

 $-12 \pm -10 + -8 + \dots$ a = -12 d = z

$$S_n = \frac{n}{2} \left\{ 2a + (n-1)d \right\}$$

$$338 = \frac{n}{9} 2(-12) + (n-1)2$$

$$676 = \left\{ n - 24 + 2n \right\} - 2$$

$$\frac{2n^{2} - 26n}{2} - \frac{676}{2} = \frac{0}{2}$$

$$n^{2} - 13n - 338 = 0$$

$$(n - 26)(n + 13) = 0$$

$$n = 26 \text{ or } n = -13 \text{ reject}$$

 $\therefore n = 26 \text{ terms}$ 

4. 
$$32 = 2 + (n-l)d.....(i)$$

$$357 = \left\{ \frac{n}{2} 2.2 + (n-l)d \right\}.....(ii)$$

$$N + (n-l)d = 714$$

$$2 + (n-l)d = 32$$

$$N(4 + nd - d) = 714$$

$$\frac{-d + nd}{4n + n^2d - d} = \frac{30}{744}$$

$$nd - d = 30$$

$$d(n-l) = 30$$

5. 
$$a)$$
  $OC = OB + BC = a + b$ 

b) 
$$OM = OA + AM = a + \frac{1}{2}b$$
  
Given  $OX = rOM$   
 $= r(a + \frac{1}{2}b)$   
From  $\triangle OBX$   
 $OX = OB + BX$   
 $= OB + BC + CX$   
 $= b + a + sa$   
 $= (1+s) a + b$   
 $\therefore r(a + \frac{1}{2}b) = (1+s) a + b$   
Comparing coefficients of a and b  
 $r = 1 + S$   
and  $\frac{1}{2}r = 1 \Rightarrow r = 2$ 

Substitute for  $r = 2 \Rightarrow 2 = 1 + s \Rightarrow s = 1$ 



c) Now 
$$BX = BC + Cx$$
  
=  $a + a = 2a$ 

$$\therefore BC:BX = 1:2$$
(a)  $-91 = 29 + (n-1)x - 6$ 

$$-120 = -6n + 6$$

$$6n = 126$$

$$n = 21$$

(b) 
$$S_{21} = \frac{21}{2} [(2 \times 2a) + (20 \times -6)]$$
  
=  $\frac{21 \times -62}{2}$   
=  $-651$ 

7. 
$$d = p-5....(i)$$
  
 $d = q-p.....(ii)$   
 $0 = 2p-q-5$   
 $0 = 7-2q+p$   
 $-p+2q=7$   
 $2p-q=5$ 

$$-2p + 4q = 14$$

$$2p - q = 5$$

$$3q = 19$$

$$q = {}^{19}/2$$

$$p = 2q - 7$$

$$p = {}^{17}/8$$

$$S = n [2a + (n-1)d]$$

$$2$$

$$= {}^{12}/2 (10 + 11 \times 2^{1/3})$$

$$= 6 (10 + {}^{22}/3) = 104$$

$$S_n = a(r^n - 1) = S(1.5 - 6)$$

$$r - 1 \quad 1.5 - 1$$

$$= 5 \times (1.5 - 1) = 103.90$$

$$0.65 = 10.4$$

8. 
$$a + a + d = 10....(i)$$

$$\frac{10}{2} \begin{cases} 2a + 9d \\ \end{cases} = 210....(ii)$$

$$2a + d = 10$$

$$\underline{2a + 9d = 42}$$

$$8d = 32$$

$$d = 4$$

$$T1 = 3 + 6(4)$$

$$= 3 + 24$$

$$= 27$$

9. 
$$S_6 = \frac{15 (1-0.56)}{1-0.5}$$
  
= 29.5314metres

10. 
$$Sn = \underline{n} \left\{ 2a + (n-1)L \right\}$$

$$S51 = \underbrace{51}_{2} (2x - 22) + (51 - 1)3$$
$$= 2703$$



$$11. \quad 100 + 200 + 400 + 800 + 1600 + 3200 + 6400 + 12800 + 25600 + 51200$$

$$\frac{200}{100} = \frac{400}{200} = \frac{800}{400}$$

$$= 51200 \quad 99600 \quad 108200 \quad 110,600$$

$$\frac{25600}{76800} \quad \frac{6400}{105,000} \quad \frac{1600}{109,800} \quad \frac{700}{111,300}$$

$$\frac{12800}{99,600} \quad \frac{3,200}{108,200} \quad \frac{800}{110,600}$$

$$= 111300$$

12.. a) Let n be the initial members

Each to contribute 720000

New membership n + 20

Contributions: 720000

$$n + 20$$

$$\frac{720000}{20000} - \frac{720000}{2000} = 3000$$

$$n + 20$$

$$720000(n+20) - 720000n = 3000n(n+20)$$

$$4800 = n(n + 20)$$

$$n^2 + 20 - 4800 = 0$$

$$n^2 + 80n - 60n - 4800 = 0$$

$$n(n + 80) - 60(n + 80) = 0$$

$$(n-60)(n+80)=0$$

$$n = 60$$

 $Original\ members = 60$ 

b) Contributions required before recruitment  $= \frac{720000}{60}$  = 120000After requirement = 720000

13. 
$$n^{th}$$
 term is  $ar^{n-1}$   
 $a = 8, r = \frac{1}{2}$ 

$$n^{th} term = \frac{1}{512}$$

$$8(1/2)^{n-1} = 1/512$$

$$8(1/2)^{n-1} = 2^{-9}$$

$$(\frac{1}{2})^{n-1} = 2^{-9} \div 2^3$$

$$(\frac{1}{2})^{n-1} = 2^{-12} = (\frac{1}{2})^{12}$$

$$n^{-1} = 12$$

$$n = 13$$

14. 
$$3^{rd} a + 2d$$
  
 $9^{th} a + 8d$ 

$$25^{th} a + 24d$$

(i) 
$$\underline{a+2d} = \underline{a+8d}$$
$$a+8d \ a=24d$$



$$(a + 2d) (a + 2d) = (a + 8d) (a + 8d)$$
 $a^2 + 26da + 48d^2 = a^2 + 16da + 64d^2$ 
 $\frac{10da}{10d} = \frac{16d^2}{10d}$ 
 $a = 1.6d....(i)$ 
 $(a + 6b) + 2(a + 5d) = 78$ 
 $3a + 16d = 78....(ii)$ 
But  $a = 1.6d$ 
 $\therefore (3x1.6d) + 16d = 78$ 
 $4.8d + 16d = 18$ 
 $4.8d$ 

(ii) 
$$S_n = \frac{n}{2} (2a + (n-1)d)$$

$$S_a = \frac{9}{2} ((2x6) + (9-1)3.75)$$

$$= \frac{9}{2} (12 + 30)$$

$$\frac{9}{2} x 42 = 189$$

15. 
$$T_{4} = a + 3d$$

$$T_{7} = a + bd$$

$$(a + 6d) - (a + 3d) = 12$$

$$3d = 12$$

$$d = 4$$

$$But \ a = 9$$

$$S5 = \frac{5}{2} 2(9) + 4(4)$$

$$= \frac{5}{2} 18 + 16$$

$$= \frac{5}{2} x 34$$

$$= 85$$

1. Vectors 2

1. a) (i) 
$$AN = OA + ON$$

$$= -a + \frac{2}{2}b$$

$$= \frac{2}{7}b - a$$

$$= \frac{7}{13}AN$$

$$\frac{7}{13}\left(-a + \frac{2}{7}b\right)$$

$$\frac{2}{13}b - \frac{7}{3}a$$

$$\frac{2}{13}a - \frac{7}{13}a$$

(iii)  $AM = \underline{1} AB$ 

$$= \underbrace{\frac{1}{4}}_{A} (\overrightarrow{AO} + OB)$$

$$= \underbrace{\frac{1}{4}}_{A} (\cancel{b} - \cancel{a})$$

$$= \underbrace{\frac{1}{4}}_{A} (\cancel{a} + \cancel{b})$$

$$= \underbrace{\frac{1}{4}}_{A} (\cancel{a} + \cancel{b})$$

$$= \underbrace{\frac{1}{4}}_{A} (\cancel{a} + \cancel{b})$$

$$\frac{OT}{OM} = \frac{2}{13} (3a + b)$$

$$\frac{1}{4} (3a + b)$$

$$\overrightarrow{OT} = \underbrace{8}_{13} OM$$

$$Or \overrightarrow{OM} = \underline{13} \overrightarrow{OT}$$

Since 
$$\overrightarrow{OT} = \underbrace{8}_{13} \overrightarrow{OM}$$
  
Then  $OT : TM = \underbrace{8}_{13} : \underbrace{5}_{13}$   
 $= 8 : 5$ 

2.

 $\sqrt{Construction of \ 260^{\circ} \ and \ 290^{\circ}}$ 

Bisect \( \subseteq btw \) 90° and 60° to obtain \( \subseteq 75° \)

 $\sqrt{\text{Construction of the given sides}}$ 

Construction of △ XYZ

$$-25 - 5y = -72$$
  
 $X = -8.4$   $y = 9.4$ 

-5y = -47

$$OX = \underbrace{2}_{3}(3i \pm 2j - 4k) + \underbrace{1}_{3}(6i \pm 11j + 2k)$$

$$= 2i + 4j - \underline{8k} + 2i \pm \underline{11j} + \underline{2}$$

$$3 \quad 3$$

$$= 4i + 5j - 2k$$

$$= 10x1 = \sqrt{16 + 25 + 4}$$

$$= 6.71 units$$

4. a) 
$$2^{5} - 5(2^{4}) (\frac{1}{5}) + 10 (2^{3}) (\frac{1}{5}x)^{2} - 10(2^{2}) (\frac{1}{5}x)^{3} + 5(2) (\frac{1}{5}x)^{4} - (\frac{1}{5}x)^{5}$$
$$32 - 16x + \frac{16}{5}x^{2} - \frac{8}{25}x^{3} + \frac{2}{125}x^{4} - \frac{1}{3125}x^{5}$$
$$-\frac{1}{5}x = -0.04$$
$$x = 0.2$$

b) 
$$32 - 16(0.2) + {}^{16}/_{5}(0.2)^{2-8}/_{25}(0.2)^{3} + \dots$$
  
=  $32 - 3.2 + 0.128 - 0.00256$   
=  $28.92544$   
=  $29.925$ 

5. 
$$AS = AO + OS$$

$$= -a + 2 (3 c)$$

$$= 2 c - a \dots BC = BA + AC$$

$$= a - b + AC$$

$$= a - b + AC$$

$$But AC = AO + OC = -a + 3 c$$

$$= 3 c - a \dots AB + 2 OC = 2 3 c = 2 c$$

$$3 3 3$$

$$BA = 2 c \dots BC = -12c + 3c - a = c - a.$$

b) (i) 
$$AT = \eta AS = \eta (2c-a)$$
  
=  $2\eta c - \eta a$   
 $AT = AB + BT = 2c + K(c-a)$   
=  $2c + Kc - Ka$   
=  $(2 + k)c - Ka$ 

(ii) 
$$2 + K = 2\eta$$
 (i)  $K = \eta$  (ii) 
$$2 + \eta = 2\eta$$
$$2 = 2\eta - \eta$$
$$2 = \eta, K = 2$$

$$(c) BT : BC$$

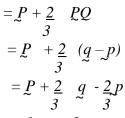
$$BT = 2 BC$$

6. 
$$(a) (i) \stackrel{PQ}{PQ} = \stackrel{PO}{PO} + OQ$$

$$= \stackrel{P}{P} + \stackrel{q}{q} \text{ or } \stackrel{q}{q} - \stackrel{p}{p}$$

$$(ii) O\stackrel{R}{R} = O\stackrel{P}{P} + \stackrel{R}{P}\stackrel{R}{R}$$

For  $\sqrt{PQ}$  or P and qFor  $\sqrt{exp}$ . Of ORFor  $\sqrt{SQ}$  in p & qFor  $\sqrt{SQ}$  in P & QFor  $\sqrt{OT}$  or p & q Multiply this by 12



$$=\frac{1}{3}p + \frac{2}{3}q$$

$$=\frac{1}{3}p + \frac{2}{3}q$$

(iii) 
$$SQ = SQ + QQ$$
  

$$= -\frac{3}{4} QP + QQ$$
  

$$= -\frac{3}{4} p + q \text{ or } q - \frac{3}{4} p$$

(b) Express OT in two different ways:

Given 
$$OT = n \ OR$$

$$= n \left( \frac{\tilde{I}P}{3} + \frac{2}{3} \ \mathcal{Q} \right)$$

$$= \frac{n}{3} p + \frac{2n}{3} \mathcal{Q}$$

From  $\triangle OST$ ,

$$OT = OS + ST$$

$$= \underbrace{3}_{4}OP + M SQ$$

$$= \underbrace{3}_{4}P + M \left(-\frac{3}{4}P + q\right)$$

$$= \left(\frac{3}{4} - \frac{3m}{4}\right)p + mq$$

$$\therefore \underline{n}_{3}P + \underline{2n}_{3}q = \left(\frac{3}{4} - \frac{3m}{4}\right)p + mq$$

$$= \underbrace{3}_{4}P + \underline{3}P + mq$$

Compare the coefficients of p and q

$$\frac{n}{3} = \frac{3}{4} - \frac{3}{4} m$$

$$4n = 9 - 9m$$

$$4n + 9m = 9 \dots eq (1)$$

$$\frac{2n}{3} = m$$

$$m = \frac{2n}{3} \dots eq. (2)$$

Substitutes form in equation (1)

$$4n + 9\left(\frac{2n}{3}\right) = 9$$

$$4n + 6n = 9$$

$$10n = 9$$

$$n = \frac{9}{10}$$

Substitute for n in equation (2)

$$m = \frac{2}{3} \times \frac{9}{10} = \frac{3}{5}$$

### 52. Binominial expansion



a) 
$$1^5 + 5(-3x)^1 + 10(-3x)^2 + 10(-3x)^3 + 5(-3x)^4 + (3x)^5$$
  
 $1 - 15x + 90x^2 - 270x^3 + 405x^4 - 243x^5$   
 $1 - 15x + 90x^2 - 270x^3 + 405x^4 - 243x^5$   
b)  $3x = 1 - 0.997$   
 $x = 0.001$   
 $= 1 - 15(0.001) + 90(0.001)^2 - 270(0.001)^3 + 405(0.001)^4$   
 $= 1 - 0.015 + 0.00009 - 0.00000027 + \dots$   
 $= 1 + 0.00009 - 0.015 - 0.00000027$   
 $= 1.00009 - 0.01500027 = 0.98508973$   
 $= -0.9851(4 d.p)$ 

2. (i) 
$$5 + \frac{x}{2} = 15625 + \frac{3125}{3}X + \frac{9375}{4}X^2 + \frac{625}{2}X^3 + \dots$$
  
(ii)  $X = 1$   
 $\left(\frac{11}{2}\right)^6 = 15625 + \frac{3125}{3} + \frac{9375}{4} + \frac{625}{2}$   
 $= 15625 + 1041.667 + 2343.75 + 312.5$ 

3. 
$$(\overline{3} + 2x)^{6} = (\overline{3})^{6} + \overline{6} (\overline{3})^{5} + 2x + 15 (3)^{4} (2x)^{2} + 20 (\overline{3})^{3} (2x)^{3}$$

$$= 27 + 108 x (\overline{3} + 270x^{2} + 480 x^{3}) (\overline{3})^{3}$$

$$\overline{3} + 2x = 3 (\overline{3})$$

$$\overline{2x + 2} = 3$$

$$x = \sqrt{3}$$

$$27 + 108 (\overline{3}) (\overline{3} + 270 (\overline{3})^{2} + 480 (\overline{3}) (3)^{3}$$

$$= 27 + 324 + 810 + 4320 = 5481$$

4.

	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	10	11	12

$$P(Sum \ odd) = \frac{18}{36}$$
 =  $\frac{1}{2}$ 

5. 
$$\angle PQR = 180 - (35o + 75)$$
  
=  $70^{\circ}$   
 $PR^2 = 12^2 + 8.4^2 - 2(12)(8.4) \cos 70^{\circ}$   
 $PR = 145.61 = 12.07$ 

6. (a) Terms; 
$$2^5$$
,  $2^4(\sqrt[3]{x})$ ,  $23(\sqrt[5]{x})^2$ ,  $2^2(\sqrt[3]{x})^3$ ,  $2^3(\sqrt[3]{x})^4$   
Co eff 1, 5, 10, 10, 5  
 $(2 + \sqrt[3]{x})^5 = 25 + 5(2)^4(\sqrt[3]{x}) + (2)^3(\sqrt[3]{x})^2 + 10(22)^3/x)^2 + 5(2)(\sqrt[3]{x})$   
 $= 32 + 2140x - 1 + 720x - 2 + 1080x^3 + 820x - 4$ 

(b) 
$$9.5 = 2 + \frac{3}{x}$$
  
 $\frac{3}{x} = 7.5$ 

$$x = \frac{3}{7.5} = 0.4$$

$$(9.5)^{5} = 32 + \frac{240}{0.4} + \frac{720}{(0.4)^{2}} + \frac{1086}{(0.4)^{4}} + \frac{810}{(0.4)^{4}}$$

$$= 53647.625(3d.p)$$



7. 
$$X^{5} - 5x^{4}(0.2) + 10x3(0.20 - 10x2(0.2)^{3} + 5x(0.2)^{4} - (0.2)^{5}$$
  
 $X^{5} - 5x^{4}(^{2}/10) + 10x^{3}{}^{2}/10^{2} - 10x^{2}(^{2}/10)^{3} + 5x(^{2}/10)^{4} - (^{2}/10)^{5} + x^{5} - (^{4}/10)x^{3} - (^{8}/100)x^{2} + 5x16 - 2^{5}/10^{5}$   
 $X^{5} - x^{4}x^{3} - 8/100x^{2} + 80x - 2^{5}/10^{5}$   
90, 392, 079

8. 
$$Log (x +24) = log(x(9-2x))$$
  
 $X + 24 = 81-18x$   
 $X = 3$ 

9. 
$$1 + \underline{x} = 1 + \underline{x} + \underline{5x^{2}} + \underline{5x^{3}}$$

$$\begin{cases} 6 \\ 1 + \underline{x} \\ 12 \end{cases} = 1\frac{1}{4}$$

$$\frac{\underline{x}}{12} = \frac{1}{4}$$

$$x = 3$$

$$\left(\begin{array}{c} \underline{5} \\ 4 \end{array}\right)^{6} = 1 + \underline{3} + \underline{9} + \underline{27} \\ 2 + 48 + 432$$

$$= 2.7500$$

10. (a) 
$$(1 + \frac{1}{2})^8 = 1 + 8(\frac{1}{2}) + 28(\frac{1}{2}x)^2 + 56(\frac{1}{2}x)^3 + 70(\frac{1}{2}x)^4 + 567(\frac{1}{2}x)^5 + 2(\frac{1}{2}x)^6 + 8(\frac{1}{2}x)^7 + (\frac{1}{2}x)^8$$
  
=  $1 + 4x + 7x^2 + 7x^3 + 4.375x^4 + 1.75x^5 + 0.4375x^6 + 0.0625x^7 + \frac{1}{256}x^8$ 

(b) 
$$(1.05)8 = 1 + 4(0.1) + 7(0.1)2 + 7(0.1)3$$
  
=  $1 + 0.4 + 0.07 + 0.0074...$   
=  $1.48$ 

11. 
$$81 + 27x + 9x^{2} + 3x^{3} + x^{y}$$

$$81 + 108x + 54x^{3} + x4$$

$$81 + 108(0.02) + 54(0.02)^{3}$$

$$= 83.182$$

## 53. Probability

1. (a) (i) Total balls = 
$$3 + 6 = 9$$

(ii) = P(BW) or P(WB)

$$= \underbrace{\begin{bmatrix} 3 \times 6 \\ 9 & 9 \end{bmatrix}}_{= 18} + \underbrace{\begin{bmatrix} 6 \times 3 \\ 9 & 9 \end{bmatrix}}_{= 18}$$
$$= \underbrace{\frac{18}{81}}_{= 18} + \underbrace{\frac{18}{81}}_{= 19}$$
$$= \underbrace{\frac{36}{81}}_{= 9} = \underbrace{\frac{4}{9}}_{= 19}$$

(b) (i) 
$$P(WW) = \frac{6}{9} \times \frac{5}{8}$$
  
 $= \frac{30}{72} = \frac{5}{12}$   
(ii)  $P(WW) = \frac{6}{9} \times \frac{6}{9}$   
 $= \frac{4}{9}$ 

2. 
$$P(W) = \frac{7}{12} \quad P(B) = \frac{5}{12}$$

$$(2 \text{ white and one brown})$$

$$= (WWB \text{ or } WBW \text{ or } BWW)$$

$$= (\frac{7}{12} x^{6}/11 x^{5}/10) + (\frac{7}{12} x^{5}/11 x^{6}/10) + (\frac{7}{12} x^{7}/11 x^{6}/10)$$

$$= \frac{22}{44}$$

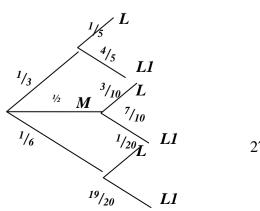
(ii) 
$$P(BBW \text{ or } BWB \text{ or } WBB)$$
  
=  $(5/_{12} x^{4}/_{11} x^{7}/_{10}) + (5/_{12} x^{7}/_{11} x^{4}/_{10}) + (7/_{12} x^{5}/_{11} x^{4}/_{10})$   
=  $7/_{22}$ 

(iii) P (at least one white cup)  
= 
$$(1-P(BBB) = 1-(5/12 x^4/11 x^3/10)$$
  
=  $21/22$ 

(iv) 
$$P$$
 (same colour) =  $P(BBB \text{ or } WWW)$   
=  $(\frac{7}{12} x^{6}/_{11} x^{5}/_{10}) + (\frac{5}{12} x^{4}/_{11} x^{3}/_{10})$   
=  $\frac{9}{44}$ 

$$b) P(E) = \frac{4}{16}$$
$$= \frac{1}{4}$$

4.





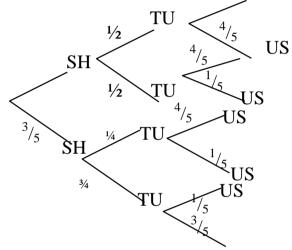


(a) 
$$P(late) = (\frac{1}{3}x^{\frac{1}{5}}) + (\frac{1}{2}x^{\frac{3}{10}}) + (\frac{1}{6}x^{\frac{1}{20}})$$
  
=  $\frac{1}{15} + \frac{3}{20} + \frac{1}{120}$   
=  $\frac{9}{40}$ 

(b) 
$$P = \frac{1}{3} x \frac{1}{5} + (\frac{1}{6} x \frac{1}{20})$$
  
=  $\frac{1}{15} + \frac{1}{20}$   
=  $\frac{3}{40}$ 

(c) 
$$P = (not \ late) = (1 - \frac{9}{40})$$

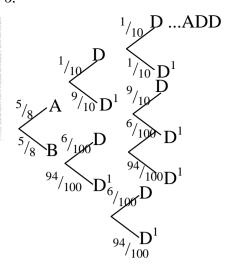
*5. a*)



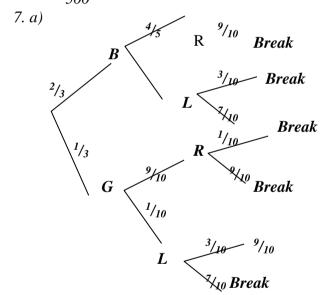
b) i) 
$$P(all faults) = P(SH \text{ and } TU \text{ and } US)$$
  
=  $\frac{2}{5} x \frac{1}{2} x \frac{4}{5} = \frac{4}{25}$ 

ii) 
$$P(exactly\ two) = \frac{2}{5}x\frac{1}{2}x\frac{1}{5} + \frac{2}{5}x\frac{1}{2}x\frac{1}{5} + \frac{3}{5}x\frac{3}{4}x\frac{1}{5}$$





Both defective  $= \underbrace{3 \times 1 \times 1}_{8 \text{ } 10 \text{ } 10 \text{ } 8} \underbrace{100 \text{ } 100}_{100}$   $= \underbrace{3}_{800} + \underbrace{180}_{80000}$   $= \underbrace{24}_{4000}$   $= \underbrace{3}_{500}$ 



b) i) 
$$P(BL \text{ or } GL) = \frac{2}{3}X^{1}/_{10} + \frac{1}{3}X^{1}/_{10}$$
  
=  $\frac{2}{15} + \frac{1}{30} = \frac{5}{30}$ 

ii) P( BL break or GR break)  
= 
$${}^{2}/{}_{3} X^{1}/{}_{5} X^{3}/{}_{1}0 + {}^{1}/{}_{3} X^{1}/{}_{10} X^{3}/{}_{10}$$
  
=  ${}^{2}/{}_{50} + {}^{1}/{}_{100} = {}^{4+1}/{}_{100} = {}^{5}/{}_{100}$ 

iii) P( BR break or GR break)  
= 
$${}^{2}/{}_{3} X^{4}/{}_{5} X^{1}/{}_{10} + {}^{1}/{}_{3} X^{9}/{}_{10} X^{1}/{}_{10}$$
  
=  ${}^{8}/{}_{150} + {}^{9}/{}_{300} = {}^{16+9}/{}_{300} = {}^{25}/{}_{300}$ 

iv) 
$$1 - (5/100 + 25/300) = 1 - 15 + 25/300$$

	1	2	3	4	5	6	
1	2	3	4	5	6	7	
2	3	4	5	6	7	8	
3	4	5	6	7	8	9	
4	5	6	7	8	9	10	
5	6	7	8	9	10	11	
6	7	8	9	10	11	12	

 $P(a two days outing) = \frac{10}{36} = \frac{5}{18}$ 

(b) 1 2 3 4 5 6  
H H1 H2 H3 H4 H5 H6  
T T1 T2 T3 T4 T5 T6  
P(2days and one day pocket money)  
= 
$$5x 10$$
  
 $18 12$   
=  $25$   
 $108$ 

(c) (i) 
$${}^{5}/_{18} \times {}^{2}/_{12}$$
 2D pocket  
=  ${}^{5}/_{108}$  2/<sub>12</sub> 1D pocket  
(ii)  ${}^{5}/_{18}$  2D No pocket  
 ${}^{13}/_{18}$  1D  ${}^{2}/_{6}$  No pocket

 $P(get\ pocket\ money)$ =  $\frac{5}{18} \frac{x^2}{12} + \frac{5}{18} \frac{x^{10}}{12} + \frac{1^3}{18} \frac{x^2}{6}$ 

9. (a) (i) 
$$P(WW) = \frac{4}{10} \times \frac{3}{9}$$
  
 $= \frac{2}{15}$   
(ii)  $P(WW)$  or  $(RR) = \frac{4}{10} \times \frac{3}{9} + \frac{6}{10} \times \frac{5}{9}$   
 $= \frac{2}{15} + \frac{1}{3} = \frac{7}{15}$ 

(iii) 
$$P$$
 (at least Red) =  $1 - P(WW)$   
=  $1 - \frac{2}{15}$   
 $\frac{13}{15}$   
(iv)  $P(WR)$  or  $P(RW) = \frac{3}{5} \times \frac{4}{9} + \frac{2}{5} \times \frac{2}{3}$   
=  $\frac{8}{15}$ 

10. a) i) 
$$\frac{8}{15}$$
 ii)  $\frac{2}{15} + \frac{5}{15} = \frac{7}{15}$ 



$$Gh = \frac{2}{15} x^{1}/_{14} = \frac{2}{21}0 = \frac{1}{105}$$

$$\frac{3}{21} + \frac{7}{45} = \frac{45 + 147}{945}$$

$$=\frac{192}{945}$$

(c)(i)

	Н	T
1	1H	1T
2	2H	2T
3	3H	3T
4	4H	4T
5	5H	5T
6	6H	6T

11. (a)

(b) (i) same colour = 
$$\frac{5}{9} x^{4}/2 x^{3}/7 + \frac{4}{9} x^{3}/8x^{2}/7$$
  
=  $\frac{5}{42} + \frac{1}{7}$   
=  $\frac{11}{42}$ 

(ii) more red balls = 
$$\frac{5}{89} x \frac{1}{2} x \frac{3}{7} + \frac{5}{9} x \frac{1}{2} x \frac{4}{7} + \frac{5}{9} x \frac{1}{2} x \frac{4}{7}$$
  
=  $\frac{5}{42} + \frac{10}{63} = \frac{10}{63}$   
=  $\frac{5}{42} + \frac{20}{63} = \frac{15 + 40}{126} = \frac{55}{126}$ 

(iii) at least black ball was picked

$$= 1 - \frac{5}{9} x \frac{1}{2} x \frac{3}{7}$$

$$= 1 - \frac{5}{21}$$

$$= \frac{16}{21}$$

(iv) Atmost 1 red ball picked

$$= \frac{5}{9} x \frac{4}{2} x \frac{3}{7} + \frac{4}{9} x \frac{5}{8} x \frac{3}{7} + \frac{4}{9} x \frac{3}{8} x \frac{2}{7}$$

$$= \frac{5}{42} + \frac{5}{92} + \frac{1}{21}$$

$$= \frac{5 + 5 + 2}{42}$$

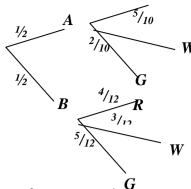
$$= \frac{12}{42}$$

$$= \frac{27}{7}$$

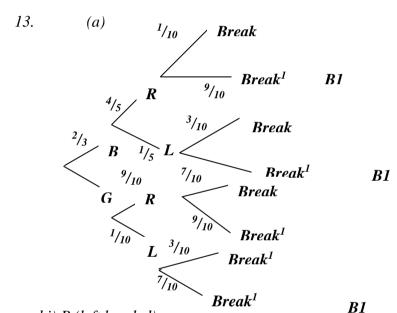
$$^{3}/_{10}$$



12.



$$P(Red) = (\frac{1}{2}x^{3}/10) + (\frac{1}{2}x^{4}/12) = 19 60$$



bi) P (left handed)  
= 
$${}^{2}/_{3} x^{1}/_{5} + {}^{1}/_{3} x^{1}/_{10}$$
  
=  ${}^{2}/_{15} + {}^{1}/_{3}$   
=  ${}^{5}/_{30} = {}^{1}/_{6}$ 

ii) P ( Right handed and will break)
$$= \frac{2}{3} x^{4} / 5 x^{1} / 10 + \frac{1}{3} x^{1} / 9 x^{1} / 10$$

$$= \frac{8}{150} + \frac{9}{300}$$

$$= \frac{25}{300} = \frac{1}{18}$$
c) P (=  $\frac{2}{3} x^{4} / 5 x^{1} / 10 + \frac{2}{3} x^{1} / 5 x^{3} / 10 + \frac{1}{3} x^{9} / 10 x^{1} / 10 + \frac{1}{3} x^{1} / 10 x^{3} / 10$ 

14. (i) 
$$P(RRR) = \underbrace{5}_{15} \underbrace{X}_{15} \underbrace{5}_{15} \underbrace{X}_{15}$$

$$= \underbrace{125}_{3375}$$

$$= \underbrace{1}_{27}$$
(ii)  $\underbrace{125}_{3375} + \underbrace{64}_{3375} + \underbrace{216}_{3375}$ 

$$= 405 \atop 3375$$

$$= 3 \atop 25$$

$$(iii) P (RBG) + P (GRB) + P(BGR)$$

$$5 \times 4 \times 6 + 6 \times 5 \times 4 + 4 \times 6 \times 5$$

$$15 \quad 15 \quad 15 \quad 15 \quad 15 \quad 15 \quad 15$$

$$= 120 + 120 + 120 \atop 3375 \quad 3375 \quad 3375$$

$$= 24$$

B- To bed on time

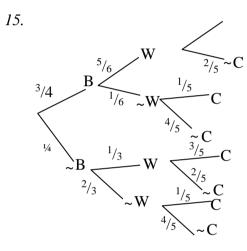
B- To bed late

W- Waking upon time

W- waking up late

C- Getting to class on time

C- Getting to class late



(a) (i)  $P(Bnw) = \frac{3}{4} x^{5}/6$ =  $\frac{5}{8}$ 

ii) P( Waking up late)

$$\begin{pmatrix}
\frac{1}{8} & x & \frac{1}{8} \\
\frac{1}{3} & \frac{1}{8} & \frac{1}{6} \\
\frac{1}{2} & \frac{3}{2} & \frac{4}{24} \\
\frac{7}{24} & \frac{7}{24}
\end{pmatrix}$$

b) (i)  $P(BW\sim C)$  or  $P(B\sim W\sim C)$ 

$$\begin{pmatrix}
\frac{3}{4} \times \frac{1}{6} \times \frac{4}{5}
\end{pmatrix} + \begin{pmatrix}
\frac{3}{4} \times \frac{5}{6} \times \frac{2}{5}
\end{pmatrix}$$

$$\frac{1}{10} + \frac{1}{4} = \frac{4+10}{40}$$

$$= \frac{7}{20}$$

ii)  $P(\sim B \sim C) = \underline{1} \times \underline{1} \times \underline{3} + \underline{1} \times \underline{2} \times \underline{1}$ 

B- To bed on time

~B- To bed late

W- Waking upon time

~W- waking up late

C- Getting to class on time

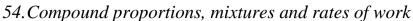
~C- Getting to class late

√tree diagram.

 $\sqrt{Addition of probability}$ 

 $\sqrt{Addition}$  of prob.

 $\sqrt{Addition}$  of prob.



a) Deposit: Total ratio 2 + 3 + 5 = 10Georgina:  $\frac{2}{10} \times 30000 = 6000$ Gilbert:  $\frac{3}{10} \times 30000 = 9000$ Akumu:  $\frac{5}{10} \times 30000 = 15000$ 

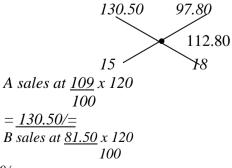
b) Balance to be paid = 510000 - 30000 = 480000Each pays =  $\frac{480000}{3} = 160000$ 

c)  $Profit = {}^{20}/_{100} x 510000 = 102000$   $Georgina\ received: {}^{1}/_{6}x 102000 = 17000$   $Gilbert\ received: {}^{2}/_{6}x 102000 = 34000$  $Akumu\ received: {}^{3}/_{6}x 102000 = 51000$ 

2. Men Days
12 20
16 ?
= (12 x 20) days
16 = 15 days

Cost of mixture  $Sh\ 112.8\ x\ \underline{100} = 94\ per\ kg$  120  $Ratio\ A: B$  (81.50 - 94): (109 - 94) 12.5: 15 2.5: 35: 6

Alt. At selling Price



<u>= 97.80/=</u>

sh 112.80 per kg

 $Ratio\ A: B$ 

(112.80 - 97.8):

(130-112.8)

15: 18

5:6

Let Onacha take x days.

 $Mogutu\ takes\ x+5\ days.$ 

$$\underline{1} + \underline{1} = 1$$

$$\overline{x}$$
  $x+5$  6

$$x^{2}(x + 5) + 6x = x(x - 5)$$

$$x^2 - x - 30 = 0$$

$$(x-10)(x+3)$$

$$x = 10, 3$$

Onacha takes 10 days.

$$5 \qquad \qquad ^{dy}/_{dx} = 6x2 + x - 4$$

When 
$$x = 1$$
,

$$dy/dx = 6+1 -4 = 3$$

Grad of normal = -1/3

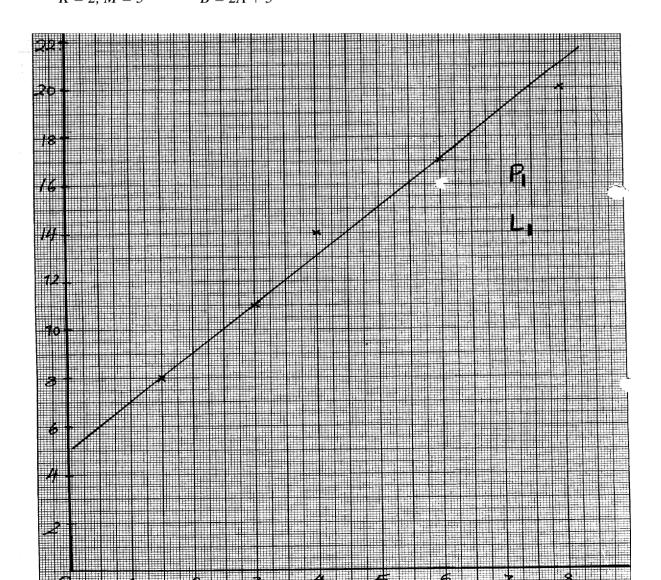
$$y + \frac{1}{2} = -\frac{1}{3}(X - 1)$$

$$y = -1/3 x - 1/6$$

6 Gradient = 
$$11 - 8$$

$$K = 2, M = 5$$

$$B=2A+5$$





$$(70 - 25 \times 60 = 2700$$
  
 $2700 \cos 47$   
 $= 2700 \times 0.68 = 1841.4$ nm

8 
$$\frac{6x 72 + 66 x 4}{10} = 69.6$$

$$100\% = 69.6$$

$$\therefore 105 = 73.10$$

9 (a) (i) A B Mixture  
150 160 156  
1 n 1+n  
150 160n (n+1)156  
150 + 160n = 156(n+1)  

$$N = {}^{6}/_{4} = {}^{3}/_{2}$$
  
= 112 x 156  
100 = shs. 174.72

(b) At 11.45 a.m

Depth filled by P in 2hrs = 2.1m

$$3hrs = \frac{3hr}{2hr} \times 2.1m$$
 $= 3.15m$ 

Depth filled by q in 7hrs = 2.1m

$$3hrs = \frac{3hrs}{7hrs} \times 2.1m$$

$$= 0.9m$$

Depth emptied by R in 6hrs = 2.1m  $\frac{2hrs}{6hrs} = 2hr \times 2.1$ 

:. Depth at 
$$11.45a.m = (3.15 + 0.9) - 0.7 = 3.35m$$

10 Let the amount to be mixed be x kg of the lower, priced grade and y kg for higher price grade X kg of the lower priced grade cost Sh. 420x

Y kg of the higher priced grade cost Sh.470y

Total cost of (x+y0 kg of mixture)

$$= Shs. \underline{420 x + 470 y}$$

$$x + y$$
equating  $420x + 470y = 455$ 

$$x + y$$

$$420 x + 470y = 455x + 455y$$

$$470y - 455y = 455x - 420y$$

$$15y = 35x$$

$$X: y = 3:7$$

11. Cross sectional area =  $r^2$ 

*12* 

$$= (22 \times 35 \times 35) cm^2$$

Flow per second =  $(\underline{22} \times 35 \times 35 \times 45)$ cm<sup>2</sup>

After  $2^{1}/4$  hrs =  $(22 \times 35 \times 35 \times 45 \times 3 \times 60 \times 69)$ liters = 233887.5litres

a) In 2000, Costs Shs  
Material = 
$$\frac{8}{25} \times 1250 = 400$$
  
Labour =  $\frac{14}{25} \times 1250 = 700$   
Transport =  $\frac{3}{25} \times 1250 = 150$ 

In 2003

$$Material = 400 \times 2 = 800$$
  
 $Labour = {}^{130}/_{100} \times 700 = 910$   
 $Transport = {}^{120}/_{100} \times 150 = 180$ 

- b) In 2004 Costs

  Material = 800

  Transport = 180

  :: labour = 1981 (800 + 180) = Shs. 1001
  :: Increase in labour = 1001 910 = 91
  % increase = 91/910 x 100
  = 10%
- 13. Cost price =  $100 \times 114 = shs$ . 95 120 Let A: B = n : 1  $\frac{95}{1} = \frac{80n + 100}{n + 1}$   $\frac{95n + 95}{1} = 80n + 100$   $\frac{15}{1} = \frac{1}{3}$   $\frac{n:1}{1} = 1:3$  $\frac{13}{1} = 1:3$
- 14. Let the ratio be x: y 76x + 84y = 81(x + y) 84y 81y = 81x 76x 3y = 5x 3 = x 5 y x : y = 3 : 5
- 15. a) Cost of  $8kg = 5 \times 25 + 2 \times 30 + 1 \times 45 = 230$ Cost of  $1 kg = \frac{230}{8} = 28.75$ Profit/ $kg = 28.75 \times \frac{20}{100}$  = 5.75b) i) Selling price  $= 28.75 \times \frac{112}{100} = 32.20$   $32.20 \times \frac{120}{100} = 38.64$ 38.64



16. 
$$= 3 (5.60) + 11y = 6.70$$

$$14$$

$$= 16.8 + 11y = 93.8$$

$$11y = 77$$

$$y = 7$$

$$1Kg costs Shs. 7.00$$

## 55. Graphical methods

1. 
$$x^{2} + 4x + y^{2} = 5$$

$$x^{2} + 4x + (\frac{1}{2}x + 4)^{2} + y^{2} = 5 + (\frac{1}{2}x + 4)^{2}$$

$$(x + 2)^{2} + (y + 0)^{2} = 5 + 4$$

$$(x + 2)^{2} + (y + 0)^{2} = 9$$

$$Centre (-2,0)$$

$$Radius \sqrt{9}$$

$$r = 3 \text{ units}$$

2. 
$$x^2 + 6x + (3)^2 + y^2 - 10y + (-5) = 2 + 9 + 25$$
  
 $(x + 3)^2 + (y - 5)^2 = 36$   
 $(x - -3)^2 + (y - +5)^2 = 6^2$   
 $\therefore centre(-3, 5)$   
Radius 6 units

3. 
$$CBE = 40^{\circ}$$
 (alt.segiment theoren)  
 $\angle BCE = 120^{\circ}$  (Suppl. To  $BCD = 60^{\circ}$ alt. seg.)  
 $\therefore (40 + 120 + E) = 180^{\circ}$  (Angle sum of  $\Delta$ )  
 $\angle BEC = 20^{\circ}$ 

4. 
$$X^2 + Y^2 - 10Y + 25 = 25 - 16$$
  
 $(X - 0)^2 + (Y - 5)^2 = 9$   
 $(X - 0)^2 + (Y - 5)^2 = 3^2$   
 $Centre\ (0, 5)$   
 $Radius = 3$ 

5.

х	-5	-4	-3	-2	-1	0	1
$x^3$	-125	-64	-27	-8	-1	0	1
$6x^2$	150	96	54	24	6	0	6
8x	-40	-32	-24	-16	-8	0	8

Completing of sq. for expression in x and y.  $\sqrt{Expression}$ .

√Centre √Radius

-0	-1	U	1
24	6	0	6
-16	-8	0	8

у	-15	0	3	0	-3	0	15
$x^3 + 6x$	$x^2 + 8x >$	>1					

Between

(i) 
$$x = -3.85 \ 0.1 \ and \ x - 2.15 \ 0.1$$

(ii) 
$$x > 0.5 \pm 0.1$$

$$y = x^3 - 3x + 2$$
  

$$x = 0, y = 2$$
  

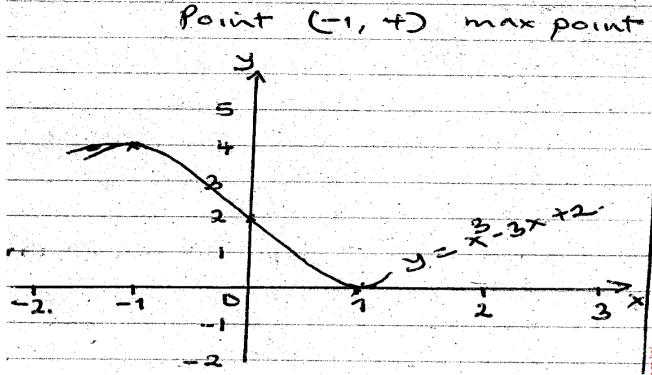
$$(0, 2) \Rightarrow y - intercept.$$

$$\frac{dy}{dx} = 3x^2 - 3 = 0$$
$$x^2 = 1$$
$$x = \mp 1$$

$$x = 1$$
  $y = 0$   
Point  $(1, 0)$  min point  $x = -1$ ,  $y = 4$ 

Point (-1, 4) max point.





7. 
$$4x_2 - 12x + 4y^2 + 12y = 7$$

$$x^2 - 3x + y^2 + 3y = \frac{7}{4}$$

$$x^2 - 3x + (\frac{3}{2})^2 + y^2 + 3y + (\frac{3}{2})^2 = \frac{7}{4} + \frac{9}{4} + \frac{9}{4} = \frac{25}{4}$$

$$(x - \frac{3}{2})^2 + (y + \frac{3}{2})^2 = 25/4$$

$$\therefore Centre\ (1,5, -1.5)$$
Radius 2.5units

8. 
$$Log R = nlog p + log K$$

Log R 1.56 1.69 1.81 1.91 2.00	Log P					
	Log R	1.56	1.69	1.81	1.91	2.00

Gradient = 
$$\frac{2 - 0.6}{0.7}$$
  
=  $\frac{1.4}{0.7}$  = 2

$$Log R intercepts = 0.6 = log k$$
  
 $K= 4$ 

The law connecting R and P is  $R=4P^2$ 

$$900 = 4P^2$$
$$P^2 = \underline{900}$$

$$225 = P^2$$

9. 
$$(x+2)^2 (y-3)^2 = 3^2$$

$$X^2 + 4x + 4 + y^2 - 6y + 9 = 3^2$$

$$X^2 + y^2 + 4x - 6y + 4 = 0$$

*10*.

V	0	2	4	6	8	10
$\frac{1}{T}$	2.04	3.33	4.17	5	6.25	7.30

$$\underline{T} = a$$

$$b + V$$

$$\underline{I} = \underline{b + V}$$

$$T \qquad a \\ \underline{I} = \underline{I}V + \underline{b} \\ T \qquad a \qquad a$$

$$\frac{b)(i)}{a} \quad 1 = \frac{Grad}{\Delta x} \Rightarrow \frac{\Delta y}{10 - 6} = \frac{7.3 - 5}{4} = 2.3 = 0.575$$

$$a = 1.739$$

y = mx + C

$$b = y - Intercept ⇒ 2.04$$
 $a$ 
 $b = 2.04 x 1.739$ 
 $b = 3.547556$ 
 $b ≈ 3.548$ 

(ii) 
$$T = 0.38$$
  
 $L = 2.63$  shown on graph  
 $T$   
 $V = 1$   
(iii)  $L = 4.45$   
 $T$   
 $T = (4.45)$   
 $= 0.2247$   
 $\approx 0.22$ 

11. 
$$y = 2x^3 + x^2 + 3x - 1$$
  
 $\frac{dy}{dx} = 6x^2 + 2x + 3$   
 $\frac{dy}{dx} = 6x^2 + 2x + 3$   
 $\frac{dy}{dx} = 6 + 2 + 3 = 11$   
 $\frac{y - (-5)}{x - 1} = 11$   
 $\frac{y + 5}{y - 1} = 11x - 11$   
 $y = 11x - 16$ 

12. 
$$3^{5} = 3^{-4} \times 3^{-x}$$

$$3^{5} = 3^{-4-x}$$

$$-4 - x = 5$$

$$-x = 9$$

$$x = -9$$
13. 
$$x^{2} + 2x + 1 + y^{2} - 4y + 4 = 4 + 1 + 1$$

$$(x+1)^{2} + (y-2)^{2} = 9$$

$$Centre (-1, 2)$$

$$Radius \quad 3units$$

*14. c*)

X	-4	-3	-2	-1	0	1	2
-6	-6	-6	-6	-6	-6	-6	-6
X	-4	-3	-2	-1	0	1	2

$4x^2$	64	36	16	4	0	4	16
$X^3$	-64	-27	-8	-1	0	1	8
$Y = -6 + x + 4x^2 + x^2$	-10	0	0	-4	-6	0	20

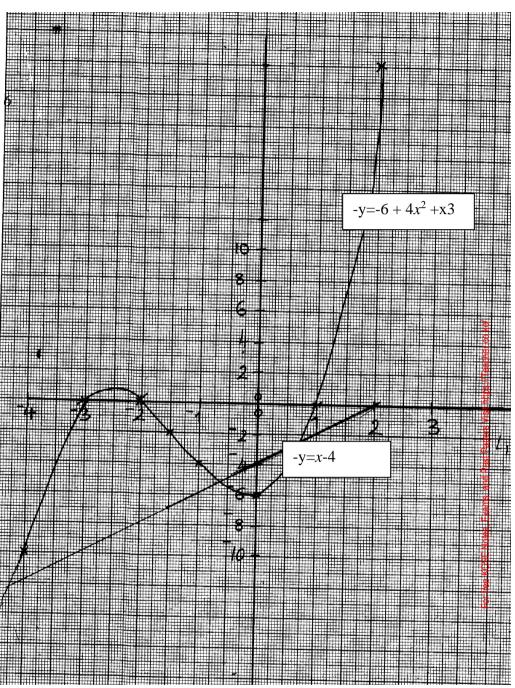


$$y = x^{3} + 4x^{2} + x - 6$$

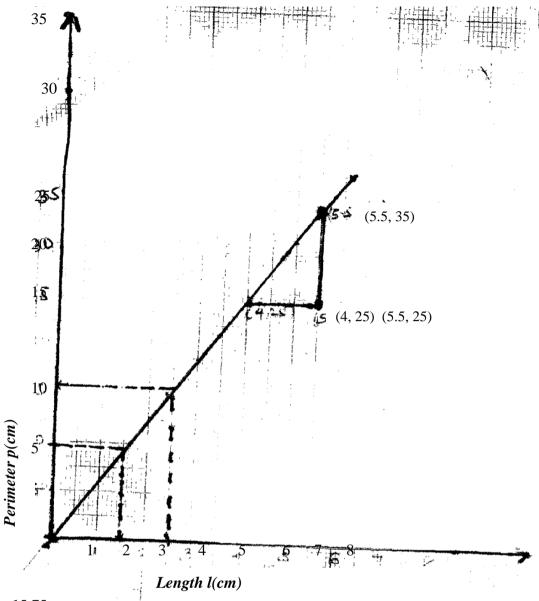
$$0 = x^{3} + 4x^{2} + x - 4$$

$$y = -2$$

(iii) 
$$y = x^3 + 4x^2 + x - \frac{0 = x^3 + 4x^2 + 0 - 2}{y = x - 4}$$







(i) 
$$P = 15.75cm$$

(ii) 
$$l=1.5cm$$

(iii) 
$$m = \frac{35 - 25}{5.5 - 4.0} = \frac{10}{1.5} = 0$$

(c) choose 
$$P(5,31.4)$$

$$\frac{p-31.4}{l-5} = \frac{10}{1.5}$$

$$\frac{p-31.4}{l-5} = \frac{100}{1.5}$$

$$\frac{p-31.4}{l-5} = \frac{100}{1.5}$$

$$15p - 471 = 100k - 500$$

$$15p = 100l - 29$$

$$15 15$$

$$2k = \frac{100}{15}$$

$$k = \frac{100}{15} = 3.33$$

$$2x 15$$

$$c = 1.93$$

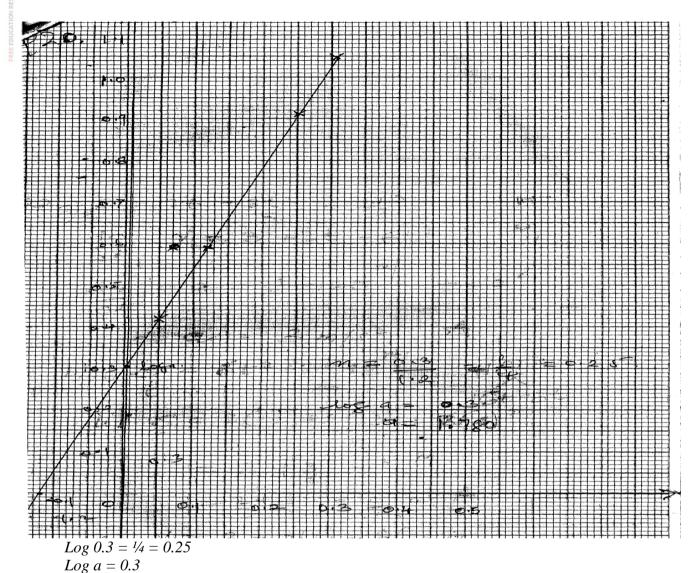
$$P + 0.6 = ar^{h}$$

Log (P + 0.6) = log a + n log R

 $= n \log R + \log 9$ 

P + 0.6	1.33	2.65	3.85	8.04	11.22
Log(P +	-0.13	0.42	0.59	0.91	1.05
0.6)					
Log R	-0.05	0.05	0.12	0.25	0.30





17. 
$$x^{2} + y^{2} - 6x = 3 - 4y$$

$$x^{2} - 6x + (^{-6}/_{2})^{2} + y^{2} + 4y + (^{4}/_{2})^{2} = 3 + (^{-6}/_{2})^{2} + (^{4}/_{2})^{2}$$

$$(x - 3)^{2} (y + 2)^{2} = 3 + 9 = 4$$

$$(x - 3)^{2} (y + 2)^{2} = 16$$

$$C (3, -2)$$

Gradient 
$$\Delta y = 7 - -2 = 3$$

$$\Delta x = 6 - 3$$

Teacher.co.ke

х	-3	-2	-1	0	1	2	3	4
$-x^3$	27	8	1	0	-1	-8	-27	-64
$2x^2$	18	8	2	0	2	8	18	32
-4x	12	8	4	0	-4	-8	-12	-16
2	2	2	2	2	2	2	2	2
у	59	26	9	2	-1	-6	-19	-46

b) Check on the graph paper.

$$c) x = 0.5 + 0.1$$

$$(d) -x^3 + 2x^2 - 5x + 3 = 0$$

Line to allow: y = x - 1

$$\begin{array}{c|ccc} x & 0 & 1 \\ \hline y & -1 & 0 \end{array}$$

$$x = 0.65$$

19. 
$$Dy/dx = 12x^{2} - 12$$
$$12x^{2} - 12 = 0$$
$$12(x^{2} - 1) = 0$$
$$x = 1$$
$$x = -1$$

$$(1,7) (-1,9)$$

Minimum

#### maximum

20. (a) table
(b) plotting
scale
smooth curve
(c) (i) -0.5 < x < 1 and x>1

(c) (i) 
$$-0.5 < x < 1$$
 and  $x > (iii) x = 2.5 \pm 0.1$ 

21. 
$$2x^{2} + 2y^{2} - 6x + 10y + 9 = 0$$

$$x^{2} + y^{2} - 3x + 5y + 9/2 = 0$$

$$x^{2} + y^{2} - 3x + 5y = -9/2$$

$$x^{2} - 3x + 9 + y^{2} + 5y + 25 = 8.5 - 4.5$$

$$4$$

$$(x - 3)^{2} + (y + 5)^{2} = 4$$

$$2$$

$$Radius = 2 \text{ units}$$

$$Centre = (1.5, -2.5)$$



## 56. Matrices and Transformations

a) B (4,-5), C (3,6 ½) Δ ABC drawn Δ ABC drawn

a) ii) Shear maps

$$I (1, 1\frac{1}{2})$$
 $Matrix = 10$ 
 $I \frac{1}{2}$ 

$$= A^{11} B^{11} C^{11}$$

$$\begin{pmatrix} 6 & 4 & -3 \\ -5 & -1 & -2 \end{pmatrix}$$

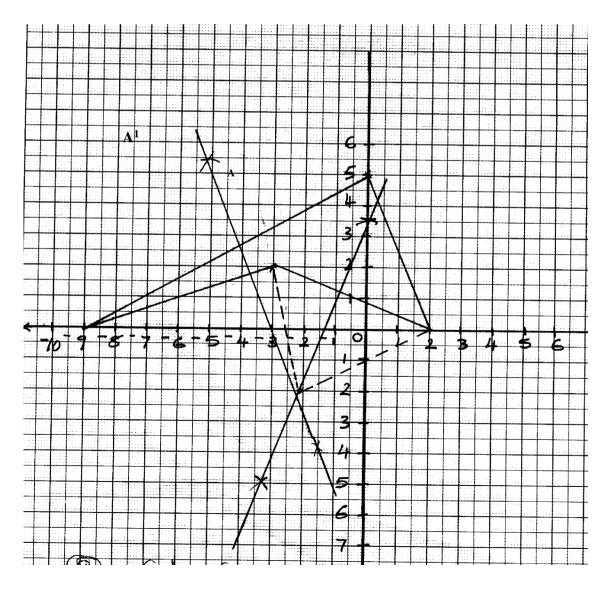
 $\Delta A^{11} B^{11} C^{11} D^{11}$ 

drawn

ii) Half turn about (0,0)

2.

 $\mathbf{B}^{1}$ 



*(b)* 

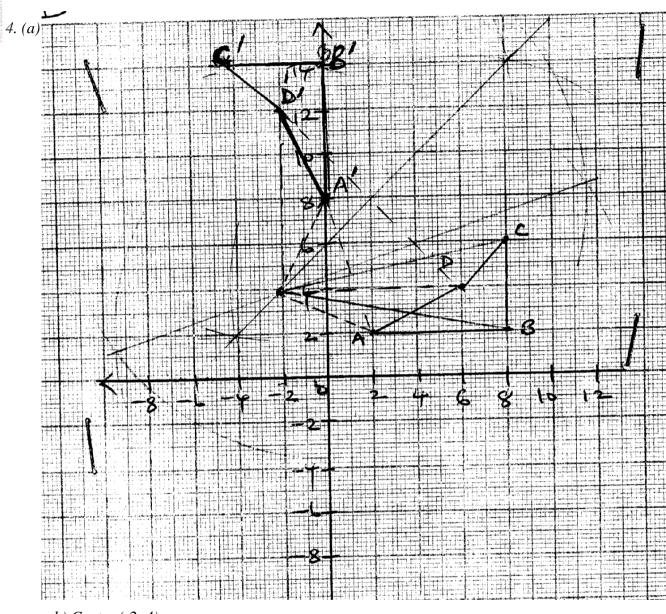


- (a) Centre (-2, -2) 90° (b) A11 (-2, -4), B11 (0, 9) (c) Half-turn about the centre (0, 2)
- $\begin{pmatrix}
  0 & -1 \\
  -1 & 0
  \end{pmatrix}
  \begin{pmatrix}
  A & B & C & D \\
  1 & 6 & 6 & 1 \\
  2 & 2 & 4 & 4
  \end{pmatrix}$   $\begin{pmatrix}
  0 & 1 \\
  -1 & 0
  \end{pmatrix}
  \begin{pmatrix}
  A_1 & B_1 & C_1 & D_1 \\
  -2 & -2 & -4 & -4 \\
  1 & -6 & -6 & -6
  \end{pmatrix}$
- $\begin{pmatrix}
  A^{1} & B^{1} & C^{1} & D^{1} \\
  -2 & -2 & -4 & -4 \\
  -1 & -6 & -6 & -6
  \end{pmatrix}
  \begin{pmatrix}
  A_{1}(-2, -1) \\
  B_{1}(-2, -6) \\
  C_{1}(4, -6) \\
  D_{1}(-4, -1)
  \end{pmatrix}$   $\begin{pmatrix}
  A_{2} & B_{2} & C_{2} & D_{2} \\
  -1 & -6 & -6 & -6 \\
  2 & 2 & 4 & 4
  \end{pmatrix}
  \begin{pmatrix}
  A_{2}(-1, 2) \\
  B_{2}(-2, -6) \\
  C_{2}(-6, 4) \\
  D_{2}(-6, 4)
  \end{pmatrix}$

 $D_2$  (-6, 4)

- (c) (i) U - positive three-quarter turn about the origin
  - (ii)UT Reflection I the line x = 0
- (*d*)  $Idet I = I2.5 \ x 2 1x \ 0 \ I = 5$ 
  - $\therefore$  Area = 5x(5x2) = 20sq. units





$$Angle + 90^{\circ}$$

$$R^{l} = \begin{bmatrix} -2 \\ -3 \end{bmatrix} + \begin{bmatrix} -3 \\ -2 \end{bmatrix}$$

$$= \begin{bmatrix} -5 \\ -5 \end{bmatrix}$$

$$\begin{bmatrix} \end{bmatrix}$$

$$P^{I}R^{I} = -5 - -25$$
  
 $-5 - 5$   
 $= -7$   
 $0$ 

$$Mag. = 7units$$

$$A^{1} = (0+1, -1-2) = (1, -3)$$

$$B^{I} = (4 + 1), 3-2) = (4, 1)$$

$$C^1 = (2 + 1, 2-2) = (3-0)$$

$$C^{I} = (2 + 1, 2 - 2) = (3 - 0)$$
Matrix  $\begin{pmatrix} 3 & 0 \\ 0 & 3 \\ 3 & \theta \\ 0 & 3 \\ A^{II} & (3, -9) B^{IJ} & (15, 3) & C^{II} & (9, 0) \end{pmatrix} = \begin{pmatrix} 3 & 15 & 9 \\ -9 & 3 & 0 \end{pmatrix}$ 

$$Determinant(0-9) = -9$$

$$Area = 9x24 = 216cm^2$$

$$\begin{pmatrix}
a & b \\
c & d \\
5(31 - 9b = 1) & 5(3c - 9d = -3)
\end{pmatrix} = \begin{pmatrix}
1 & 5 \\
-9 & 3
\end{pmatrix}$$

$$\frac{-15a + 3b = 5}{-48b = 0} & \frac{15c + 3d = 1}{-48d = -16}$$

$$b = 0 & d = \frac{1}{3}$$

$$a = \frac{1}{3} & c = 0$$

$$matrix \begin{pmatrix}
1/3 & 0 \\
0 & \frac{1}{3}
\end{pmatrix}$$

#### 7. Scale used S1

## △ABC drawn B<sub>1</sub>

$$\Delta A_1B_1C_1$$
 drawn  $B_1$ 

Line 
$$x = 4 L_1$$

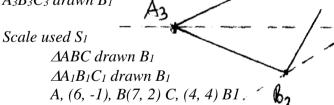
#### $\Delta A_2 B_2 C_2 drawn B_1$

#### Two seen B<sub>1</sub>

## Centre of rotation

### Angle of centre of rotation $B_1$

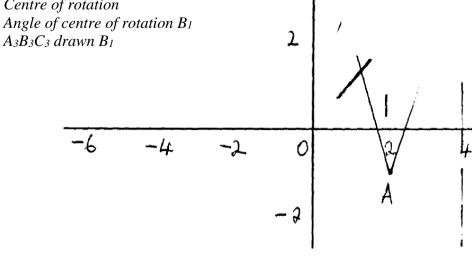
$$A_3B_3C_3$$
 drawn  $B_1$ 

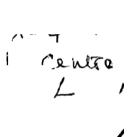


## Line $x = 4 L_1$ $\Delta A_2 B_2 C_2 drawn B_1$

$$\Delta A_2 B_2 C_2 arawn B_1$$

$$A_3B_3C_3$$
 drawn  $B_1$ 







(a) 
$$P(6, -2)$$
  
 $X^{l} = 6 - 3 (-2) = 12$   
 $Y^{l} = 2(6) = 12$   
 $(X^{l}, Y^{l}) = (12, 12)$ 

(b) (i) 
$$A^{1}(3, 4)$$
  
(ii)  $B^{1}(3, 2)$   
 $C^{1}(1, 4)$   
 $D^{1}(4, 3)$ 

$$(c) (i) \quad \begin{pmatrix} 1 & -2 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} A^{1} & B^{1} & C^{1} & D^{1} \\ 3 & 3 & 1 & 4 \\ 4 & 2 & 4 & 5 \end{pmatrix}$$

$$= \begin{pmatrix} A^{11} & B^{11} & C^{11} & D^{11} \\ -5 & -1 & -7 & -6 \\ 4 & 2 & 4 & 5 \end{pmatrix}$$

$$A^{11}(-5, 4)$$
,  $B^{11}(-1, 2)$ ,  $C^{11}(-7, 4)$  and  $D^{11}(-6, 5)$ 

(b) 
$$1-3 xyz xIyIzI$$
  
 $X_2(2, 10) y_2(2, 14)$   
 $X_2y_2Z_2 well drawn \begin{pmatrix} 0 & -2 \\ 2, & 0 \end{pmatrix} \begin{pmatrix} 5, & 7 & -2 \\ -1, & -1, & 2 \end{pmatrix} \begin{pmatrix} 5, & 7 & -2 \\ -1, & -1, & 2 \end{pmatrix}$ 

$$\begin{pmatrix} 0 & -2 \\ 2, & 0 \end{pmatrix} \quad \begin{pmatrix} 1 & -1 \\ 0, & 1 \end{pmatrix} \qquad \begin{pmatrix} 0, & -2 \\ 2, & -6 \end{pmatrix}$$

(d)) Area of 
$$\Delta X_2 y_2 Z_2$$
  
 $= 4x15 = 60cm^2$   
10.  $\begin{pmatrix} a & b \\ c & d \end{pmatrix}$  2 4 4 2 = 7 14 14 8  
 $\begin{pmatrix} c & d \end{pmatrix}$  1 1 4 4 8 7 16 16  
 $\begin{pmatrix} 2a + b = 8 \end{pmatrix}$   
 $\begin{pmatrix} 4a + b = 14 \\ -2a = -6 \end{pmatrix}$ 

$$6 + b = 8$$
$$b = 2$$

$$.:6 + b = 8$$

$$b=2$$

$$2c + d = 7$$

$$\frac{4c + d = 7}{-2c} = 0$$

$$c = 0$$

$$d = 7$$

$$\therefore \begin{bmatrix} 3 & 2 \end{bmatrix}$$

- it is an enlargement with scale factor 3 with centre (-1, -2)

$$(c) \begin{bmatrix} 8 \\ 7 \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 7 \\ 9 \end{bmatrix}$$

$$a + 8 = 7 \qquad 7 + b = 9$$

$$a = -1 \quad b = 2$$

$$\therefore T = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$$

- 11. ABCD drawn B<sub>1</sub> a) Name – Parallelogram B<sub>1</sub>
  - $A^{1}B^{1}C^{1}D^{1}$  drawn  $B_{1}$ *b*) Attempt to joining any two points and bisecting.  $B_1$ Description – Rotation +  $90^{\circ}$ .  $B_1$  or quarter turn about (0,0)
  - c)  $A^{11}B^{11}C^{11}D^{11}$  drawn.  $B_1$ Description – Enlargement centre (0, 0) Scale factor –Z. B<sub>1</sub>

$$d) A^{111}B^{111}C^{111}D^{111} - drawn. B_1$$

$$9-2, 4$$

$$C^{111} = (-8, 4) \, B_1 \, All \, correct$$
  
 $D^{111} \, (-4, 8)$ 

$$B^{111} = (-6, 0)$$

$$B^{111} = (-6, 0)$$

$$\begin{pmatrix}
4 & 0 & -2 \\
1 & 0 & 2
\end{pmatrix}$$

$$A^{III} = B^{III} = (-6, 0)$$

$$\begin{pmatrix} -1 & 1 \\ 2 & -3 \end{pmatrix} \begin{pmatrix} 4 & 0 & -2 \\ 1 & -2 & 4 \end{pmatrix}$$

$$\begin{pmatrix} -3 & -2 & 6 \\ 5 & 6 & -16 \\ 4/(-3 & 5) \end{pmatrix}$$

$$B^{\prime}(-2, 6)$$

$$\begin{pmatrix}
2 & -1 & -3 \\
1 & 2 & 5
\end{pmatrix} = \begin{pmatrix}
-2 & 6 \\
6 & -6
\end{pmatrix}$$

$$\begin{pmatrix}
A'' & B'' & C^{\downarrow} \\
-11 & -10 & 18 \\
7 & 10 & -6 \\
A^{I}(-11, 7) & B^{I}(-10, 10) & C'' & (18, -6)
\end{pmatrix}$$

$$A^{||} B^{||} C^{||}$$

7 10 -6   
$${}^{1}(-11, 7) B^{1}(-10, 10) C'' (18, -6)$$

$$\begin{array}{ccc}
MN & = \begin{pmatrix} 2 & -1 \\ 1 & 2 \end{pmatrix} & \begin{pmatrix} -1 & 1 \\ 2 & -3 \end{pmatrix} \\
= \begin{pmatrix} -4 & 5 \end{pmatrix}
\end{array}$$





$$p-1 = \frac{1}{-12} \begin{pmatrix} 5 & -7 \\ 4 & 8 \end{pmatrix}$$
$$\begin{pmatrix} -\frac{5}{1/3} & \frac{7}{12} \\ \frac{1}{3} & \frac{-2}{3} \end{pmatrix}$$

13. 
$$Det = 2 - 6$$
  
= -4  
 $A.S.F = 4$   
 $25.6 = 4$   
 $x$   
 $x = 6.4cm^2$   
 $Area of \triangle ABC = 6.4cm^2$ 

14. 
$$T + (2) = (4)$$

$$-4 0$$

$$T = (4 - 2) = (2)$$

$$0 + 4 4$$

$$\therefore (2) + (-1) = (1)$$

$$4 2 6$$

$$Q(1,6)$$

16. 
$$5x^{2} + 6 = \frac{110}{10}$$
$$5x^{2} + 6 = 11$$
$$x^{2} = 1$$
$$x = \pm 1$$

## 57. Statistics II

1.

	Mid					
Mass	term	F	d = x A	fd	$d^2$	$fd^2$
kg	x					
50 - 54	52	19	-15	-285	225	4275
55 - 59	57	23	-10	-230	100	2300
60 - 64	62	40	-5	-200	25	1000
65 - 69	67	28	0	0	0	0
70 - 74	72	17	5	85	25	425
75 - 79	<i>77</i>	9	10	90	100	900
80 - 84	82	4	15	60	225	900
		$\Sigma f =$		$\Sigma fd$		$\Sigma fd =$
		140		= -		9800
				480		

Marks awarded for  $\sqrt{table}$  as follows:-

 $\sum f = 140$  BI Column for d B1 Column for fd B1  $\Sigma fd = -480 \ B1$ Teacher.co.ke

$$Standard \ deviation = \sum f d^2 - \sum f d$$
$$\sum f \sum f$$

$$= \sqrt{\frac{9800}{140}} - (3.43)^{2}$$

$$= \sqrt{58.24} = 7.631$$

$$= 7.6$$

2. 
$$= \frac{8}{150} + \frac{6}{150} + \frac{9}{300} + \frac{3}{300}$$
$$= \frac{40}{300} = \frac{2}{15}$$

- a) Construction of AB B1 Construction of BC B1 Construction of AC B1
- b) Construction of bisect of AC B1
  Construction of bisect BC B1
  Radius 3.6 cm B1
- c) Construction of bisect < CAB B1 OC B1 Construction of AD B1 AD = 12.8cm B1

*3. a*)

Class	f	X	d = A - x	fd	$d^2$	$fd^2$
41 - 50	20	45.5	15	300	225	4500
51 – 55	60	53	7.5	450	56.25	3375
<i>56</i> – <i>65</i>	60	60.5	0	0	0	0
66 - 70	50	68	-7.5	-375	56.25	2812.50
71 – 85	15	73	-12.5	187.5	156.25	2343.75
				$\sum fd \ 562.5$		$\sum fd^2$ 13031.25

$$(b) S = \frac{\int fd^2}{\sum f} \frac{2}{\sum fd}$$

$$S = \sqrt{\frac{13031.25}{205} - \left(\frac{562.5}{205}\right)^2}$$

$$= \sqrt{63.567 - 7.529}$$

$$= 7.486$$

$$15 (ax)^4 (-2/x^2) = 4860$$

$$60a^4 = 4860$$

$$a^4 = 81$$

$$a = 3$$

Marks(x)	Freq.(f)	fx	d=x-x	$d^2$	$Fd^2$
5.5	1	5.5	-40.45	1636	1636
15.5	6	99	-30.45	927.2	5563
25.5	10	255	-20.45	418.2	4182
35.5	20	710	-10.45	109.2	2184
45.5	15	682.5	-0.45	0.2025	3038
55.5	5	277.5	9.55	91.20	456
65.6	14	917	19.55	382.2	535
75.5	5	377.5	29.55	873.2	4366
85.5	3	256.5	39.55	1564	4692
95.5	1	95.5	49.55	2455	2455
	∑f=80	$\Sigma f99x=3676$			$\Sigma fx^2 33,923$

$$Mean = \underbrace{\Sigma f x}_{\Sigma} = \underbrace{3676}_{80}$$

(b) 
$$Q1 = 30.5 + \frac{3}{14}x 10$$

$$S.I.R = \frac{1}{2}(62.64 - 32)$$

(c) Standard deciation

$$= \underbrace{\sum f d^2}_{\sum f} = \underbrace{33923}_{80}$$
$$= 20.59$$

6. a) 
$$x = 90 - (2 + 13 + 51 + 27 + 14 + 1)$$
  
=  $90 - 84 = 6$ 

*c*) *i*)

Class	x	f	D=x-A	fd	$D^2$	$Fd^2$
5-9	7	2	-15	-30	225	450
10-14	12	13	-10	-130	100	1300
15-19	17	31	-5	-155	25	775
20-24	22	23	0	0	0	0
25-29	27	14	5	70	350	4900
30-34	32	6	10	60	600	3600
35-39	37	1	15	15	225	225

8.

Ef = 90 Efd = 170

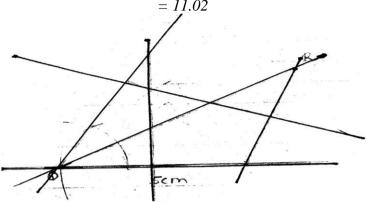
$$Efd^2 = 11250$$

$$Mean = \underbrace{E + d}_{Ef} + A$$

$$= \underbrace{-170}_{90} + 22$$

$$= 22 - 1.888 = 20.11$$

ii) 
$$S.d = \sqrt{\underline{Efd}} - [\underline{Efd}]^2$$
  
 $Ef \qquad Ef$   
 $= \sqrt{122 - (-1.888)^2}$   
 $= \sqrt{125 - 3.566} = \sqrt{121.4}$   
 $= 11.02$ 



$$RQ = 7.5 \pm 0.1$$
  
<  $PRQ 40^{\circ} \pm 1$   
 $B1 \ circle \ through \ P, \ Q \ and \ R$ 

d) 
$$r = 4.1 \circ 0$$
  
 $A = \pi r^2$   
 $2^{2} / x \cdot 4.1 \cdot x \cdot 4.1 = 52.83$ 

Class limits	f	cf
-0.5 – 19.5	7	7
19.5- 39.5	21	28
39.5 – 59.5	38	66
59.5 – 79.5	27	93
79.5 -= 99.5	7	100

*i) from the curve* 

- median = 52. M1 A1

- (ii) Inter quartile range = 66-38 = 28.
- (iii) 7th 7/10 = 62.46 marks
- (*iv*) 60th percentile 56.34

9. 
$$25^{2} + 24^{2} + 22^{2} + 23^{2} + x^{2} + 262 + 21^{2} + 23^{2} + 22^{2} + 27^{2} = 5154$$
$$5.625 + 576 + 2(484) + 2(529) + 676 + 441 + 729 + x2 = 5154$$
$$X^{2} = 81$$
$$X = 9$$

(ii) 
$$X = \frac{222}{10} = 22.2$$
  
 $-\Sigma(X-x)^2 = 2.8^2 + 1.8^2 + 0.22 + 0.8^2$ 

$$13.2^{2} + 3.8^{2} + 1.22 + 0.8^{2} + 0.2^{2} + 4.8^{2}$$

$$(x-x)^{2} = 7.84 + 3.24 \ 2(0.04) + 2(0.64)$$

$$+174.24 + 14.44 + 1.44 + 23.04$$

$$= \frac{225.6}{10}$$

$$s.d \ 22.56$$

$$= 4.75$$

10. a) i) 
$$x = A + \sum f \frac{d}{\sum} f$$
  
=  $45.6 + (-74)$   
=  $43.75$ 

Class	Mis-pt x	d = (x - A)	Frequency f	fd	$Fd^2$
1 - 10	5.5	-40.1	1	-40.1	1608.01
11 - 20	15.5	-30.1	3	-90.3	8154.05
21 - 30	25.5	-20.1	4	-80.4	6464.16
31 - 40	35.5	-10.1	7	-70.7	4998.49
41 - 50	45.5	-0.1	12	-1.2	1.44
51 - 60	55.5	9.9	9	89.1	7938.81
61 - 70	65.5	19.9	2	39.8	1584.04
71 - 80	75.5	29.9	1	29.9	894.01
81 - 90	85.5	39.9	0	0	0
91 - 100	95.5	49.9	1	49.9	2410.01

i) Standard Deviation

$$D = \sqrt{\frac{\sum f d^2}{\sum f} - \left(\frac{\sum f d}{\sum f}\right)^2}$$

$$= 10 \sqrt{\frac{34135.11}{40} - \left(\frac{-74}{40}\right)^2}$$

$$10 \times 29.1531 = 29.1531$$

b) 
$$30^{th}$$
 student =  $10^{th}$  from bottom  
 $30.5 + \left(\frac{10 - 8}{7}\right)10$   
=  $30.5 + 2.9 = 33.4$  marks.

11. a) Mean 45. 
$$5 + \underline{530}$$

$$60$$

$$= 54.33$$

(b) Median = 
$$50.5 + \left(\frac{30.5 - 23}{14}\right)$$
 10  
=  $55.86$ 

# (c) Standard deviation =

(d) Modal class 51-60

x	f	d	d2	fd	fd2
24.5	4	-30	900	-120	3600
34.5	26	-20	400	-520	10400
44.5	72	-10	100	-720	7200
54.5	53	0	0	0	0
64.5	25	10	100	250	2500
74.5	9	20	400	180	3600
84.5	11	30	900	330	9900
	200			-600	37200

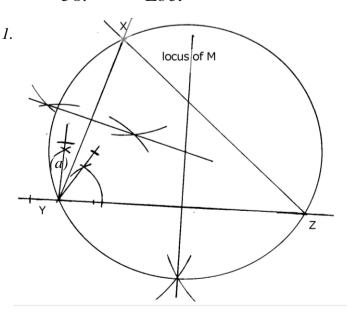
(a) (i) Mean = 
$$A + \underline{\Sigma fd}$$
  
 $\Sigma f$   
=  $54.5 - \underline{600}$   
 $200$ 

$$= 51.5$$

$$= \underbrace{\frac{\Sigma f d^2 - \Sigma f d^2}{\Sigma f}}_{\Sigma f} = \underbrace{\frac{37200 - (-3)^2}{200}}_{186 - 9} = 13.30$$

(b) 
$$Q_1 = 39.5 + \frac{50 - 30}{72} \times 10$$
  
 $= 42.28$   
 $Q_3 = 49.5 + \frac{150 - 102}{53} \times 10$   
 $= 58.56$   
 $Q_3 - Q_1 = 58.56 - 42.28$   
 $= 16.28$ 

#### 58. Loci



 $\sqrt{Construction of \angle 60^{\circ} and \angle 90^{\circ}}$ Bisect  $\angle$  btw 90° and 60° to obtain  $\angle$ 75°  $\sqrt{\text{Construction of the given sides}}$ 

Construction of  $\Delta XYZ$ 



(b)  $\angle XYZ = 42^o \pm 1^o$   $XZ = 8.8 \pm 0.1$  cm c) Bisecting any two sides Drawing the circle (d)Perpendicular bisector of YZ Identification of locus of M

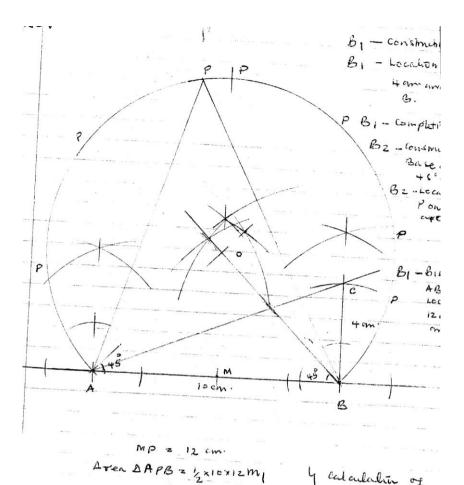
$$AC = 8 cm \pm 0.1$$

$$\angle ACB = 46^{\circ} \pm 1^{\circ}$$

- 3. a)  $AC = 12.9 \pm 0.1$ cm
  - $b)\ i)\ Line\ and\ well\ shaded\ B2$
  - *c*)  $h = 7 \pm 0.1$

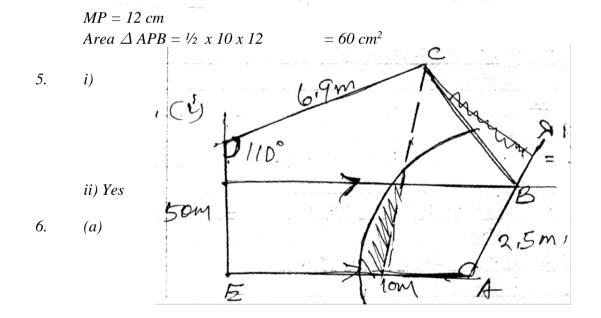
d) 
$$\triangle ABC$$
 \_\_\_\_\_ Area =  $\frac{1}{2} \times 8 \times 7cm$   
=  $28cm$   
i.e.  $\frac{3}{4} \times 28 = Area \text{ for } ARB$   
=  $21cm$   
i.e.  $\frac{1}{2} \times 8 \times h = 21$   
 $h = 5.25$ 

4.





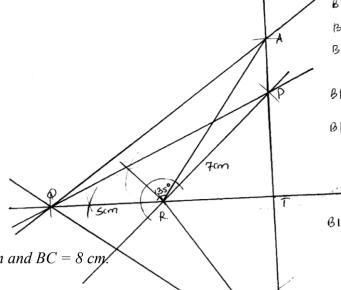
Constructing of 90<sup>0</sup>
Location of C 4 cm away from B.
Completing ΔABC
Construction of Base angles 45<sup>0</sup>.
Location of P on major arc APB
Bisecting AB to locate P 12 cm away
Calculation of maximum area of ΔAP
B. B1
B1



2 60 cm



- $(b) < PQR = 26^{\circ} + 1^{\circ}$
- d)4.9 + 0.1cm
- *e*) AT = u = 8.7cm
- f) < AQR = 37 + 1



a)  $\triangle$  ABC line AB = 7 cm and BC = 8 cm/s. 7.

Construction of  $\angle 60^{\circ}$ 

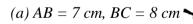
(b) 
$$AC = 7.6 \pm 0.1$$
 and

$$\angle ACB = 53 + 1^{\circ}$$

- (c) 2 sides bisector 1 Circle drawn radius 4.4.  $\pm 0.1$
- (d) Bisect  $\angle ACB$

Bisection line to cut the circle to identify P

∡ PBC measure ≡



$$\angle ABC = 60^{\circ}$$

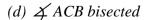
(b)  $AC = 7.6 \pm 0.1 \ cm$ 

$$\angle ABC = 53^{\circ} \pm 0.1$$

(c) Perpendicular bisectors of any two st

Circle drawn

 $Radius = 4.4. \pm 0.1. cm$ 

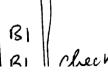


Bisection line drawn to cut circle at P

$$\angle BPC = \angle BAC = 67^{\circ}$$

$$\angle PBC = 88 \pm 0.1^{\circ}$$

B





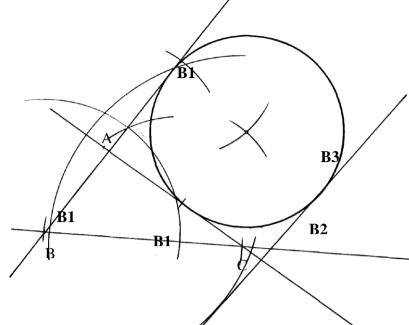
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5.4cm

8. B1 – Line AC B1Line AB B1 AD

B3 – Drawing correct circle

B2- Tangent correctly drawn



8см

9. a) B1 for constructing 15
B1 for constructing 75
B1 for completing trial
B1 for AC = 8.8 ± 0.1

(b) (i) B1For locating locus centre B1 for locus of X

(ii) B1 for constructing arcs 6.8cm from AC

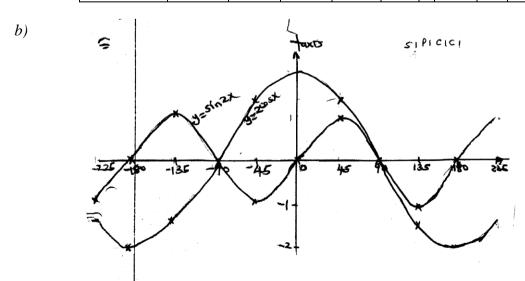
B1 for locus Y

(c)B2 for shading the locus of P



*1. a)* 

$X^o$	-225	-180	-135	-90	-45	0	45	90	135	180	225
$y = \sin 2x$		0		0	1.0		1.0	0		0	
$y = 2\cos x$		-2.0		0	1.4		1.4	0			
										2.0	





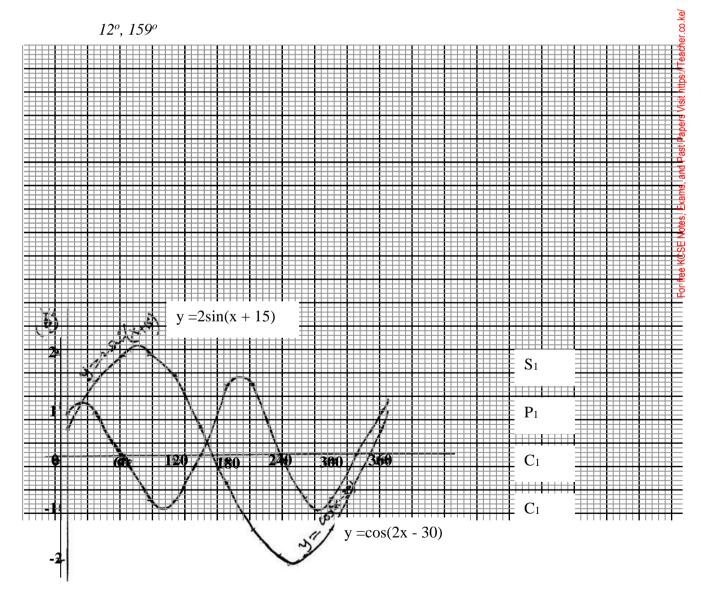
(c) -90° or 90° (d) (i) Highest point 1 unit Lowest point - 1.4

X	0	30	60	90	120	150	180	210
$2\sin(x+15^{\circ})$	0.52	1.41	1.93	1.93	1.41	0.52	-0.52	-
								1.41
$Cos(2x - 30^{\circ})$	0.87	0.87	0	-0.87	0.87	0	0.87	0.87

Х	240	270	300	330	360	
$2\sin(x+15^{\circ})$	-1.93	-1.93	-1.41	-0.52	0.52	В
$Cos(2x-30^{\circ})$	0	-0.87	-0.87	0	0.87	

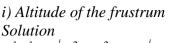
 $B_1$   $B_1$ 

(i) Amplitudes:, 
$$y = 2 \sin (x + 15)$$
  
=  $2 units$   
 $y = \cos (2x - 30)$   
=  $1 unit$   $B_1$ 





Determine the



Solution  

$$A^{I}C^{I} = \sqrt{4^{2} + 4^{2}} = \sqrt{32}$$
  
 $AC = \sqrt{10^{2} + 10^{2}}$   
 $= \sqrt{200}$   
 $= 10\sqrt{2}$ 

$$AM + XM = 10\sqrt{2} - 4\sqrt{2}$$
$$= 6\sqrt{2}$$

$$AM = \frac{6\sqrt{2}}{2} = 3\sqrt{2}$$

Height = 
$$AM = \sqrt{5^2 - (3\sqrt{2})^2} = \sqrt{25 - 18}$$
  
=  $\sqrt{7} = 2.646$ 

: the altitude of the frustrum = 2.646 cm

ii) Angle between AC and the base 
$$AX = 3\sqrt{2} + 4\sqrt{2} = 7\sqrt{2}$$
 5cm
$$Tan \phi = \frac{CX}{AX} = \frac{\sqrt{7}}{7\sqrt{2}} = \frac{\sqrt{2}}{\sqrt{2}}$$

$$= 0.2673$$

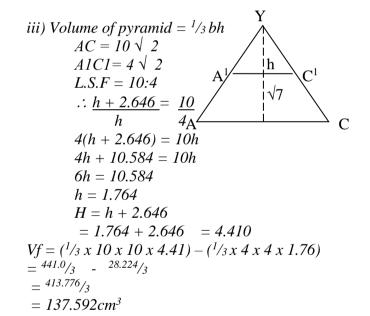
$$\theta = tan^{-1}0.2673$$

$$= 14.96^{\circ}$$

5cm

 $4\sqrt{2}$ 

5cm



- 4.  $\checkmark$ (a) table completed
  - *(b)*
  - (c) (i) 3 P1 pløtting S1- scale C1 – smooth curve
  - (ii) 180°
  - (iii) Line y = 1 drawn  $x = 4.5^{\circ}$  or  $72.8^{\circ}$  -  $107.2^{\circ}$  -  $175.4^{\circ}$

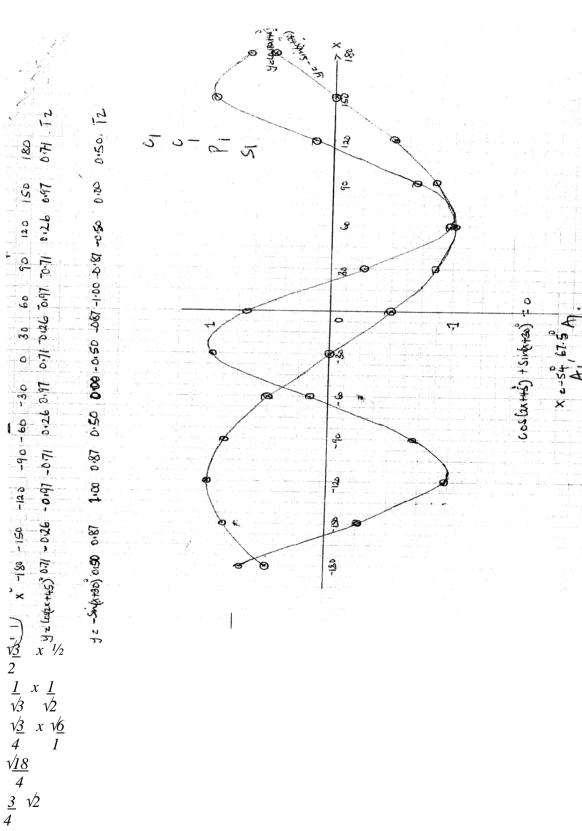
5. 
$$({}^{A}/{}_{B})^{2} = \underline{p + 33q}$$
  
 $q - 3P$   
 $A^{2}q - 3A^{2}P = BP + 3Bq$ 

$$Aq^{2} - 3Bq = BP + 3A^{2}P$$

$$2(A^{2} - 3B) = BP + 3A^{2}P$$

$$Q = \frac{BP + 3A^{2}P}{A^{2} - 3B}$$



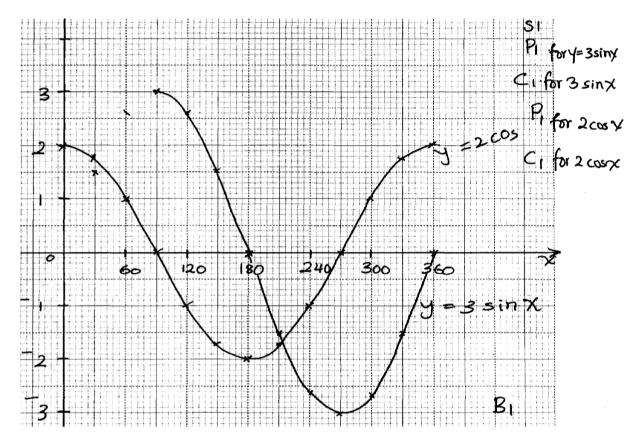


*7. 7.* 

8. a)

X	0	30	60	90	120	150	180	210	240	270	300	330	360
3sinx		1.5			2.6	1.5					-		0
											2.6		
2cos	2			0	-			-		0			
x					1.0			1.7					





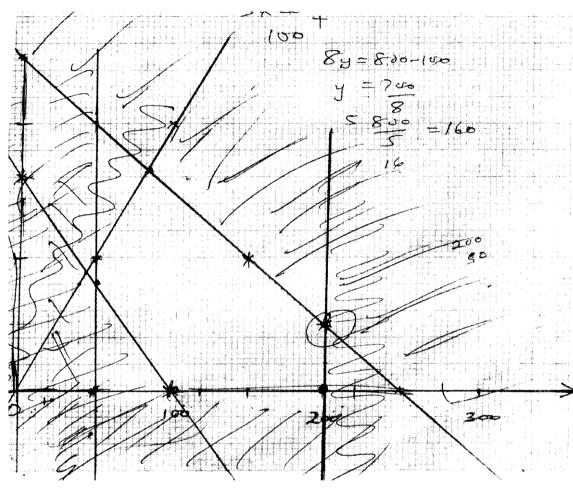
(c) (i) Amplitude =3  
(ii) 
$$x = 36^{\circ}$$
  
 $x = 216^{\circ}$   
(iii)  $33^{\circ} \le x \le 213^{\circ}$ 

X	0	90	180	270	360	450	540	630	720	810
sin ½x	0	0.71	1	0.71	0	-0.71	-1	-0.71	0	0.71
$3Sin(\frac{1}{2}x +$	2.6	2.9	1.5	-	-2.6	2.9	-1.5	0.78	2.6	2.9
60)				0.78						

10.

X	$0^{o}$	<i>30</i> °	<i>60</i> °	90°	120°	150°	180°
$2 \sin x$	0	1	1.73	2	1.73	1.00	0
1-Cos X	1	0.13	0.50	1	0.06	1.87	2





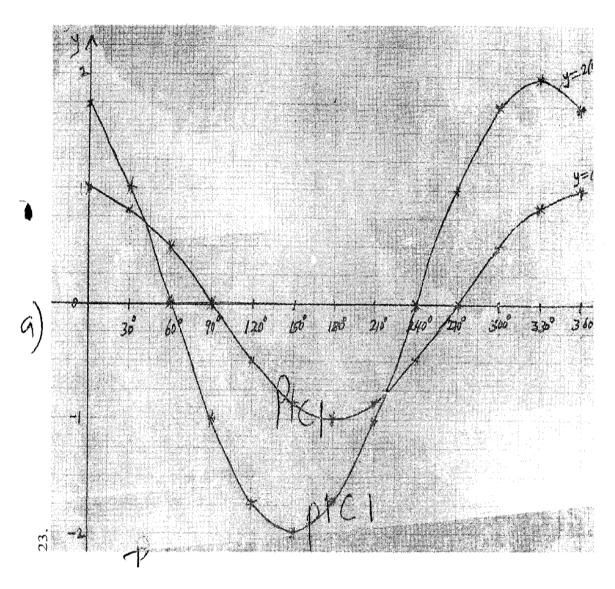
11. 
$$Sin (x + 30) = 0.5$$
  
 $x + 30 = 30^{\circ}$   
 $x = 0$   
0, 180, 360

12. 
$$(c)10\sin x = \frac{-1}{50} + 5$$
  
  $Y = \frac{-1}{50} + 5$ 

X	0	50
у	5	4

$$X_1 = 28^o \pm 1$$
  
 $X_2 = 70^o \pm 1$ 





i) amplitude = 1 ii) Period = 360° iii) 45°, 219°

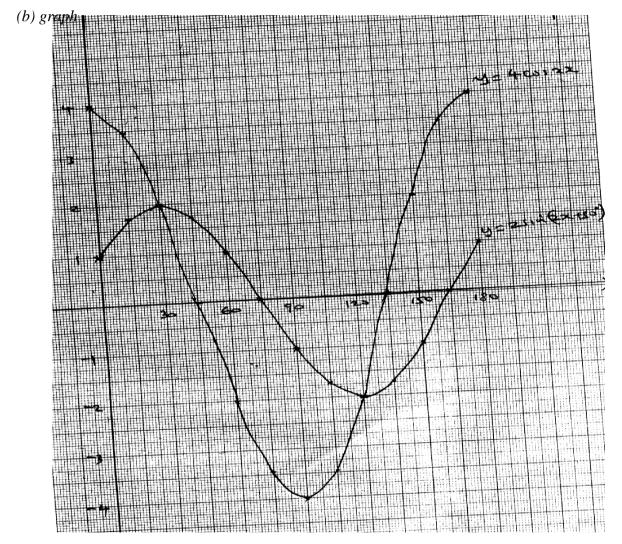
13. 
$$2\theta + 10 = 210^{\circ}, 330^{\circ}, 570^{\circ}, 690^{\circ}$$
  
 $2\theta = 200, 320, 560, 680$   
 $= 100^{\circ}, 160^{\circ}, 280^{\circ}, 340^{\circ}$   
 $= \frac{5\pi^{c}}{90}, \frac{8\pi^{c}}{9}, \frac{14\pi^{c}}{9}, \frac{17\pi^{c}}{9}$ 

14.  $4\sin 2x + 4\cos x - 5 = 0$   $4(1-\cos 2X) + 4\cos x - 5 = 0$   $4\cos 2x - 4\cos x + 1 = 0$   $4\cos 2x - 2\cos x - 2\cos x + 1 = 0$   $(2\cos x - 1)2 = 0$  $X = 60^{\circ}, 300^{\circ}$ 



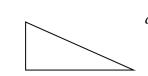
*15*.

X	15°	60°	150°	165°
4 Cos 2x	3.46			3.46
$2Sin(2x + 30^{\circ})$		1.00	-1.00	



- (c)(i) Amplitude = 4 (ii) period =  $180^{\circ}$ 
  - (d)  $x = 30^\circ$ ,  $120^\circ$

# 60. Three dimensional geometry



$$QN = \sqrt{12^2 - 6^2} = 10.39$$

$$Q = \sqrt{108}$$

$$X = \frac{10.37}{b}$$
N

$$QX = (\sqrt{108})^2 - 6^2$$
  
=  $\sqrt{72}$   
= 8.485

$$Q$$
 $8.485$ 
 $X$ 
 $\theta$ 
 $T$ 

$$\tan \theta = \frac{8.485}{6}$$

$$\theta = 54.73^{0}$$

$$d) \tan \theta = \frac{6}{10}$$

$$\theta = 30.96$$

$$\frac{6}{10} \quad obtuse = 180^{0} - 30.96$$

$$= 149.04^{0}$$

2. a) 
$$Sin_{...}36^{0} = 5$$

Where a is the side
$$a = \underline{5}$$

$$sin_{...}36$$

$$= 8.507$$

$$h^2 = 18.2 - 8.507$$
  
= 258.87  
 $H = 16.09 cm$ 

b) 
$$\frac{1}{2}$$
 ab sin  $\theta$   
 $\frac{1}{2}$  x 8.507<sup>2</sup> Sin 72 x 5  
= 172.06 cm<sup>2</sup>

c) 
$$Tan \ 36^0 = 5$$
  
 $x$   
 $x = 6.882$   
 $Tan \ \theta = 16.09$   
 $6.882$   
 $\theta = 66.84^2$   
d)  $\frac{1}{3}x \ 172.06 \ x \ 16.09 = 922.8cm^3$   
e)  $S = 23.2$ 

$$23.2 (23.2 - 18.2) (23.2 - 10)$$
  
=  $87.50 cm^3$ 

$$87.50cm^3$$

(i) 
$$\underline{1} \times 4.2 \times 7.5h = 52.5$$
  
 $3$   
 $h = \underline{52.5 \times 3} = 5.0cm$ 

(ii) 
$$AC = \sqrt{4.2^2 + 7.5^2}$$
  
=  $\sqrt{17.64 + 56.25}$   
=  $\sqrt{73.89}$   
=  $8.596$ 

4.2 x 7.5

$$AO = 8.596 \div 2 = 4.298$$

$$AO = 8.396 \div 2 = 4.298$$

$$AV = AO^{2} + OV^{2}$$

$$= 4.298^{2} + 5^{2}$$

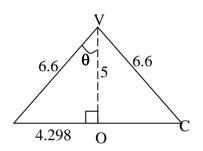
$$= 18.47 + 25$$

$$= 43.47$$

$$= 6.6cm$$

(iii) 
$$Tan\theta = \underline{4.298}$$
  
 $5$   
 $= 0.8596$   
 $\theta = 40.68^{\circ}$ 

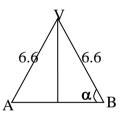
$$\angle AVC = 40.68 \times 2$$
  
= 81.36

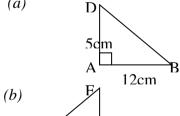


### Alternative

$$\cos\theta = \underline{5} = 0.7576$$
  
6.6  
 $\theta = 40.749^{\circ}C$   
 $\angle AVO = 40.749^{\circ}$   
 $\angle AVC = 81.498^{\circ}$ 

(iv) 
$$Cos\alpha = 2.1$$
  
 $6.6$   
 $= 0.3182$   
 $\alpha = 71.45^{\circ}$  Acute angle  
obtuse angle =  $180^{\circ} - 71.45^{\circ}$   
 $= 108.55^{\circ}$ 





$$BD^2 = 122 + 52 = 144 + 25 = 169$$
  
 $BD = \sqrt{169} = 13m$ 

$$AF^{2} = 13^{2} + 6.52 = 169 + 42.25$$
  
=211.25  $AF = 211.25 = 14.53cm$  B1  
 $tan \theta = 6.5 \ge 0.5$  M1  
 $13$   
 $\theta = 26.57^{\circ}$  A1

2.5 cm

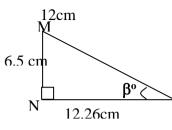
$$tan\alpha^{o} = \underline{6.5} = 1.3$$
 M1  
 $\alpha^{o} = 52.43$  A1

$$NC^2 = 2.5^2 + 12^2 = 150.25$$
  
313

 $\mathbf{C}$ 

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Ba



$$MC^{2} = 6.52 + 150.25$$
  
=  $42.75 + 150.25$   
=  $192.5$   
 $MC = 192.5 = 13.87$   
 $\tan \beta^{\circ} 6.5 = 0.5302$   
 $12.26$   
 $\beta^{\circ} = 27.93^{\circ}$  B1

5.

i) 
$$Or = 16^2 - 5^2$$

$$= \sqrt{256 - 25}$$

$$= 15.198 \text{ cm}$$
ii)  $tan \theta = \underline{5.066} = 1.2665$ 

 $\theta 51.71^{0}$ 

6. a) Height

$$AC = \sqrt{AB^2 + BC^2}$$

$$= \sqrt{10^2 + 10^2}$$

$$= \sqrt{200}$$

$$= 14.142$$

$$\therefore OA = \frac{1}{2}AC = \frac{14.14^2}{2} = 7.71$$

$$OE = \sqrt{AE^2 - AO^2}$$

$$= \sqrt{64 - 59.44} = 4.56$$

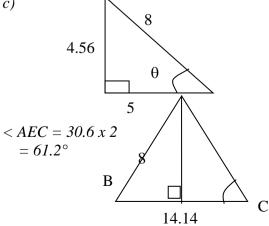
 $Tan \ \theta = \underline{4.56} = 0.912$ b)i)5.00  $\theta = 65.78^{\circ}$ 

4.56 θ 5

*ii)* 
$$Tan \ \theta = \underline{4.56} = 0.5914$$
 7.71

$$\theta = 30.6^{\circ}$$

c)





Let length of cut off pyramid be meters

Let length of cut off pyramid be mete  
Then 
$$\frac{7+h}{H} = \frac{5.5}{2.1}$$
  
 $14.7 + 2.1h = 5.5$   
 $3.4h = 14.7$   
 $h = 4.3$   
Slant height of big pyramid  
 $= \sqrt{11.3^2 + 2.75^2} = 11.6$ 

$$=\sqrt{11.3^2+2.75^2}=11.6$$

Slant height of the pyramid cut off

$$= \sqrt{4.3^2 + 1.05^2} = 4.4m$$

Area of EFCD = 
$$\frac{1}{2} \times 11.6 \times 5.5 - \frac{1}{2} \times 4.4 \times 2.1$$
  
= 27.28 m

 $Total\ surface\ area = 4\ x\ 27.28 + 2.1\ x\ 2.1\ = 113.5$ 

*b*) ½ litre paint 10m<sup>2</sup> 4 litres paints 80m<sup>2</sup>  $\therefore$  113.5 $m^2$  requires 2 tins  $2 \times 650 = Kshs.1300/=$ 

8. (a) 
$$PR = 12^{2} + 9^{2} = 144 + 81 = 225 = 15cm$$

$$\begin{array}{rcl}
h &= 19.52 - 7.52 \\
= 380.25 - 56.25
\end{array}$$

$$= 18$$
(b)  $tan \theta = 18 = 2.4$ 

$$7.5$$

$$\theta tan 2.4 = 67.38^{\circ}$$

$$(c) tan \alpha = \frac{6}{18} = \frac{1}{18 \cdot 3}$$

$$\alpha = tan^{-1} 0.3333$$

$$= 18.43^{\circ}$$

 $\therefore \angle x \ OY = 2 \ x \ 18.43 = 36.\overline{\mathbf{B6}}$ 

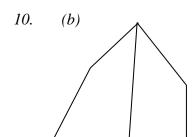
9. a) 
$$AC^2 = 12^2 + 12^2 = 288$$
  
 $AC = \sqrt{2}88 = 16.97$   
 $AC^2 = h^2 = 24^2 - (16.97)^2 = 504$ 

(*d*)  $Volume = 1 \times 12 \times 9 \times 18$  $= 648cm^3$ 

$$h = \sqrt{504} = 22.45cm$$

b) Base area = 
$$12x12 = 144cm$$
  
::Volume =  $\frac{1}{3}x$  144 x 22.45  
=  $1077.6cm^3$ 

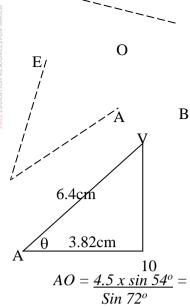
c) Slanting surface = 
$$\sqrt{30(30\text{-}24)(30\text{-}24)(30\text{-}12)}$$
  
=  $139.44$ cm<sup>2</sup>  
Total curved S.A =  $139.44$ cm<sup>2</sup> x 4 +  $144$ cm<sup>2</sup>  
=  $701.6$ cm<sup>2</sup>

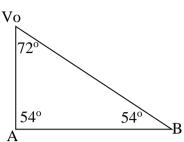


6

3





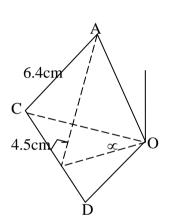


$$AO = \frac{4.5 \times \sin 54^{\circ}}{\sin 72^{\circ}} = 3.82cm$$

$$= \cos^{-1} \frac{(3.82)}{6.4} = 53.35^{\circ}$$

6.4cm

(c) 
$$Vo = \sqrt{6.42 - 3.82}$$
  
= 5.13  
 $VX = \sqrt{6.4^2 - 2.55^2}$   
= 5.99cm  
 $\infty = Sin^{-1} (Vo/vx) Sin-1(5.13/5.99)$   
 $\infty = 58.91^{\circ}$ 



11. a) Longitude difference = 
$$139 \circ + 41 \circ$$
  
=  $180 \circ$ 

b) Distance along latitude = 
$$\frac{\emptyset}{360} \times 2 \pi r \cos \theta$$
  
=  $\frac{180}{360} \times 2 \times \frac{22}{7} \times 6370 \cos 60^{\circ}$   
=  $22 \times 910 \times 0.5$   
=  $10,010 \text{ Km}$ 

Or via north pole (great circle)

Latitude difference = 
$$60^{\circ}$$

Distance = 
$${}^{60}/_{360} \times 2 \times {}^{22}/_{7} \times 6370$$
  
=  $6673.33 \text{ Km}$ 

c) Distance = 
$$\frac{\log diff}{360} \times 2\pi R \cos 60^{\circ}$$
  
 $420 = \frac{\emptyset}{360} \times 2 \times \frac{22}{7} \times 6370 \cos 60^{\circ}$   
 $\theta = \frac{420 \times 360 \times 7}{2 \times 22 \times 6370 \cos 60^{\circ}}$   
= 7.552°  
Longitude of  $C = 41^{\circ} - 7.55^{\circ} = 33.45^{\circ}N$ 

## 61. Longitudes and latitudes

1. 
$$(70-25 \times 60 = 2700 \times 0.68 = 1841.4nm)$$

 $(a) \underline{22} \times 6370 \times 2 \times \underline{\alpha} = 1600$   $7 \quad 360$ 

 $\alpha = 14.4^{\circ}$ 

Position (4.4°N, 60°E)

(b)  $72 \times 60 \cos 4.4^{\circ}$ 

$$= 4307nm$$

(c)  $T = \underline{D} = \underline{4307 \times 1.853}$ 

$$= 9.976 \ hrs$$

(d) Difference in longitude =  $72^{\circ}$ 

$$15^{o}-1hr$$

$$.:72^o = \underline{72}$$

$$15 = 4.8 hrs = 4 hrs 48 mins behind$$

1300hrs

8.12a.m

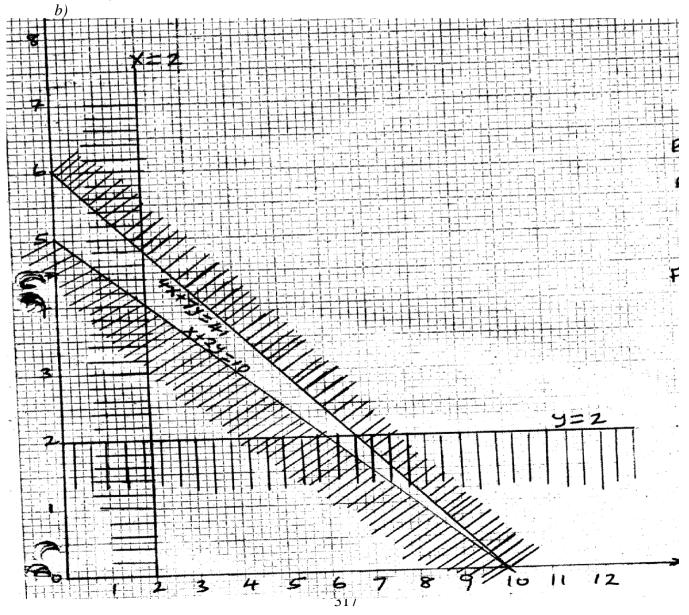
3. a)  $800 x + 1600 y \ge 8000$ 

$$x + 2y \ge 10$$

$$4x + 7y \le 41$$

$$x \ge 2$$

$$y \ge 2$$





c) For type A = 3 and B = 4No. of operators = (3x4) + (4x7)

a)  $^{180}/_{300} \times 2 \times 22/7 \times 6370 \cos 48 = 13,396 \text{Km}$ 

b)  $Km = (\underline{180 - 96}) \times 2 x^{22} / 7 \times 6370$   $= \frac{84}{360} \times 2 \times \frac{22}{7} \times 6370$  = 9342.7 km Time =  $\underline{9342}_{280}$  = 33.36 km/hr

 $c)\theta = 180^{\circ}$   $time = (4 \times 180) = 12 \text{ hrs}$  60(14:15 - 12:00) = 2:15a.m

 $d) \underline{600} Nm$   $60^{\circ}$  Q = (12N, 30W)

5. Long Difference = 24-12=  $12^{\circ}$  $12 \times 60 \text{ Cos} 34^{\circ} = 596.9 \text{nm}$  $S = \frac{\text{"5.96"nm}}{1.5}$ = 397.9 knots

6. (i)  $AB = \underline{80} \times 2 \times 3.142 \times 25$  - | 360  $0 = \underline{4 \times 25} \times 3.142$   $= \underline{314.2} \text{ cm}$  = 34.9111 cm.

(ii)  $\theta \times 2 \times 3.142 \times 25\cos 50^{\circ} = \frac{314.2}{9}$   $\theta = \frac{314.2}{9} \times 360$   $\theta = \frac{314.2}{9} \times 3.142 \times \cos 50$  $\theta = 93.35^{\circ}$ 

Longitude of  $BC(93.35^{\circ} - 90^{\circ})E = 03.35^{\circ}E$ .

(iii)  $\frac{\theta}{360}$  x 3.142 x 50 = 314.2  $\theta = 314.2 x 360$  0 = 314.2 x 360 0 = 314.2 x 50 $0 = 80^{\circ}$ 

Latitude of  $B (80^{\circ} - 50) S$ =  $30^{\circ} S$ 

Position of  $B \Rightarrow (30^{\circ}\text{S}, 03.35^{\circ}\text{E})$ 

 $2133.6 = \underbrace{x}_{2} \times 2 \times 22 \times 6380 \cos 70^{\circ}$ 

360 7

 $\infty + 15^{\circ} = 56^{\circ}$ =  $56 - 15 = 41^{\circ}N$ 

: Location of B is  $B(70^{\circ}S, 41^{\circ}N)$ 

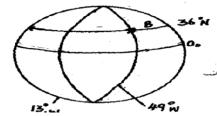




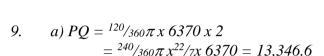
(b) (i) 
$$^{180}/_{360} \times 2 \times ^{22}/_{7} \times 6370 \times \cos 360o$$
  
=  $16196.52m$ 

$$(ii)^{180/360} \times 2 \times 2^{22/7} \times 6370$$
$$= 12012km$$

(c) 
$$\theta/360 \times 2x^{22}/7 \times 6370 \cos 36 = 840$$
  
=  $9.3353^{\circ}$   
=  $position C = 131-9.3^{\circ}W$   
 $C(36^{\circ} N, 121.7^{\circ}W)$ 



B



b) 
$$2PR \cos 60^{\circ}$$
  
 $PR = \frac{100}{360} \times 2\pi \times 6370 \cos 60^{\circ}$ 

 $= \frac{200}{360}x^{22}/7 \times 6370 \cos 60 = 5561.1 \text{km}$ 

c) 
$$PN = \frac{30}{360}x2 \ x^{22}/7 \ x \ 6370$$
  
= 3336.67 km

10. (a) (i) 
$$60 (z-50) = 1200$$
  
 $Z = 20$   
 $Z = 70^{\circ}S$ 

(ii) 
$$xy = 48 \times 2 \times 6370 \cos 50$$
  
 $360 = 3431.629km$ 

(b) (i) 
$$XZ = 3431.627 + 1200$$
  
 $1.853 = 3051.9 \text{km}$   
 $Time = 3051.9 = 7.6 \text{hrs}$ 

(b) (ii) 
$$tie = 7.36 + 4.28 = 12.04$$

$$\frac{360}{9} = \frac{88 \times 910}{9}$$
= 8897.78 km
≈ 8898km ( to nearest km)



c) B- 
$$C = \frac{60}{360} \times 2 \times 22 \times 6370 \times \cos 45^{0}$$
  
 $= \frac{22 \times 910 \times 0.7071}{63}$   
 $= 471.8.7 \text{ km}^{3}$   
 $A - C \text{ in } Km = (8898 + 4718.70)$   
 $= 13616.7 \text{ KM}$   
 $T \text{ ime taken} = \frac{13616.7}{840} = 16.21 \text{ hours}$   
 $= 16 \text{ hrs } 13 \text{min}$   
 $= 16.13$   
 $= 12.28 \text{ am followinmorning}$ 

## 62. Linear programming

1. 
$$30x + 20y \le 4800....(i)$$
  
 $30x + 40y \ge 3600...(ii)$   
 $10x (30y...(iii)$   
 $x \ge 0 y \ge 0$ 

objective function 10 x + 12 y = K

(ii) consider (60,40)  

$$10 (60) + 12(40) = 600 + 480$$
  
 $= 1080$   
 $10x + 12y = 108 0$   
 $5x + 6y = 540 - search line$ 

X	20	40	60
у	73	57	40

Maximum profit at ( $\alpha$ , 240) No queen cake, 240 marble cakes

$$(iii)$$
 240 X 12 = sh. 2880

(iv) 
$$10x + 12y \ge 600 \implies 10x + 12y = 600$$
  
 $5x + 6y = 300$ 

X	α	12	60
у	50	40	0

2. Machine A

Machine B

Shirts	Jerseys	Shirts	Jerseys
Sittis	Jerseys	Sittis	Jerseys
No. x	у	$\mathcal{X}$	У
Hrs. @2hrs	@3hrs	@2hrs	@1hr
	(i) 2x + 3y = 24		

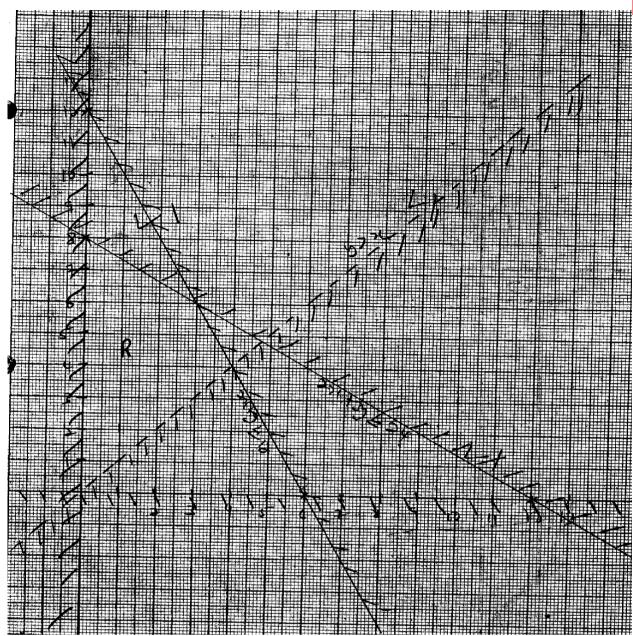
(iv) y = 0

x = 0



= Shs. 1800





3. (a) 
$$3x + 7y \le 210$$
  
 $x + y = 20$   
 $x < 2y$   
 $x > 15$ 

(c) 
$$120x + 140y = 120 \times 130 + 140 \times 10$$
  
Profit = shs.5960  
 $x = 31$ 

$$y = 16$$

4. Passengers

$$64x + 48y \ge 384 \text{ i.e. } 8x + 6y \ge 48$$
  
 $x > 0$   
 $y > 0$   
 $x + y \ge 7$ 

Cost equation

$$Total\ cost = 2500x + 20000y$$

 $L_1$ 

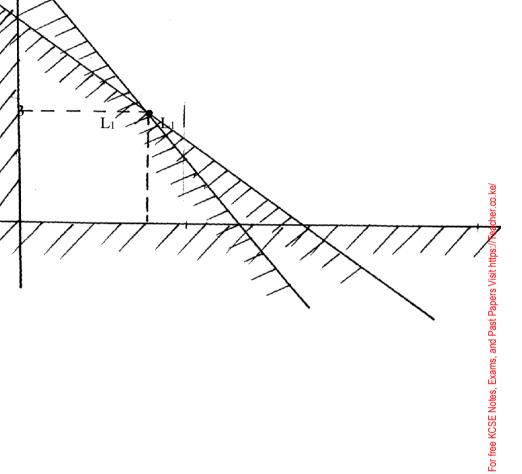


4

 $3x + 4y \le 120$ 5.  $400x + 150y \ge 9000$  $x \ge 8$  y > 12

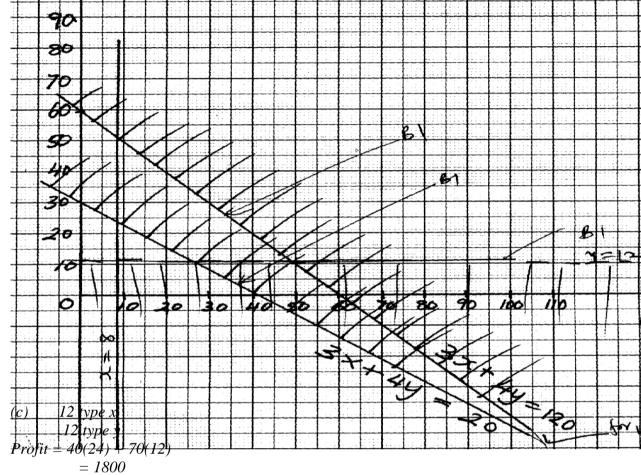
(iv) y 12

(b)(i) 3x + 4y 20(ii) 40x + 15y 900 (iii) x 8



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ble showing calculation of profit f				
Points	Objective function $40x + 70y$	Profit		
(i) (8,24)	320 + 1680	2000		
(ii) (24, 12)	960 + 840	1800		
(iii) (8, 12)	320 + 840	1160		



6. 
$$100 x = 160y = 16000$$
$$= 100 x 200 + 160 x 50$$
$$20000 + 8000$$
$$28000/=$$

$$5 x 200 + 8 x 50$$

$$1000 + 4000$$

$$10 x 200 + 16 x 50 =$$

$$10x + 16y = 1600$$

$$5x + 8y = 800$$

$$5 x 20 + 100$$

$$8y = 800 - 100$$

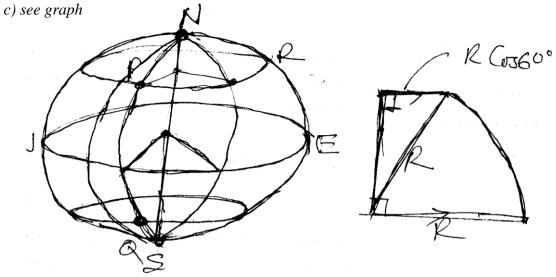
$$y = \frac{700}{8}$$

$$8^{800}/5 = 160$$

a) 
$$y < 2x$$
,  $50 \le x \le 200 \ x > 100$   
 $y > 0$ ,  $x + y \le 250$ ,  $100x + 160y \ge 16000$ 

b) See graph



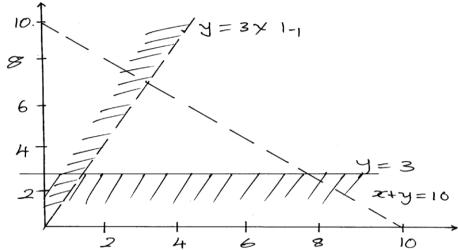


profit?

7. 
$$x + y < 10$$

$$y < 3x$$

$$y > 3$$



(c) Obejctive function 3x = 2y = I or use of serach line 5 packets of cups and 4packets of stucks

x y Profit	
2 4 14	
2     4     14       2     5     16       3     4     17       3     5     19       3     6     21	
3     4     17       3     5     19       3     6     21	
3 5 19	
4     4     20       4     5     22	
4 5 22	
5 4 23	

8. 
$$Panga - P$$
,  $Jembe\ J$   
 $(a)\ 50P + 30J = 4260$   
 $50P + 15J = 1290$   
 $50P + 30J \neq 4260$   
 $10P + 30J \neq 1290$   
 $40P = 1680$   
 $P = 168 = 42$ 

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$$4
50(42) + 30J = 4260
2100 + 30J = 4260
30J = 2160
J = (2160)
30
J = 72$$

Wholesaler  $\underline{110} \times 42 = shs.46.50 = pangas$   $\underline{100}$   $\underline{85} \times 72 = shs 60 = jembes$   $\underline{100}$ 

For B
$$50 \times 46.50 + 30 \times 61.2$$

$$2310 + 1836 = 4146$$
Saving = 4260
$$\frac{4116}{144}$$

(b) Discount 5000 - 3500 = 1500% discount =  $1500 \times 100$  5000= 30%a)  $X \ge 0$ ,  $y = \ge 0$ 

9. 
$$a) X \ge 0, y = \ge 0$$
  
 $10x + 20y \ge 120$   
 $4x + y \ge 20$ 

b) On the graph.

c) i) 
$$(4,4)$$
  
 $4 \times 100 + 4 \times 300$   
 $400 + 1200 = 1600$ 

10. Distance Covered = 
$$(3t^2 - 3t - 6)dt$$
  
=  $t^3 - \frac{3}{2}t^2 - 6t \cdot 4^{-4}$   

$$\begin{cases} 4^3 - \frac{3}{2}(4)^2 - 6(4) \\ 2 \end{cases} - \begin{cases} 1^3 - 3(1)^2 - 6(1) \\ 16 - \frac{-13}{2} = \end{cases}$$

### 63. Differentiation

1. 
$$S = t^{3} - 3t^{2} + 2t$$

$$(a) V = \underline{ds} = 3t^{2} - 6t + 2$$

$$dt$$

$$When t = 2$$

$$V = 3(4) - 6(2) + 2$$

$$= 2m/s$$

(b) At minimum velocity:

$$\frac{dv}{dt} = 0$$

$$\frac{dv}{dt} = 6t - 6$$

$$6t - 6 = 0$$

$$t = 1$$

$$Min-velocity = 3(1)^2 - 6(1) + 2$$

(c) 
$$3t^2 - 6t + 2 = 0$$
  
 $t = 6 \pm \sqrt{(-6) - 4(3)(2)}$   
 $6$   
 $= 6 \pm 5.2$ 

= -1m/s

 $t = 1.58 \ or \ 0.4 sec$ 

$$(d) acc = \underline{dv} = 6t - 6$$

$$dt$$

$$a = 6(3) - 6 = 12m/s^{2}$$

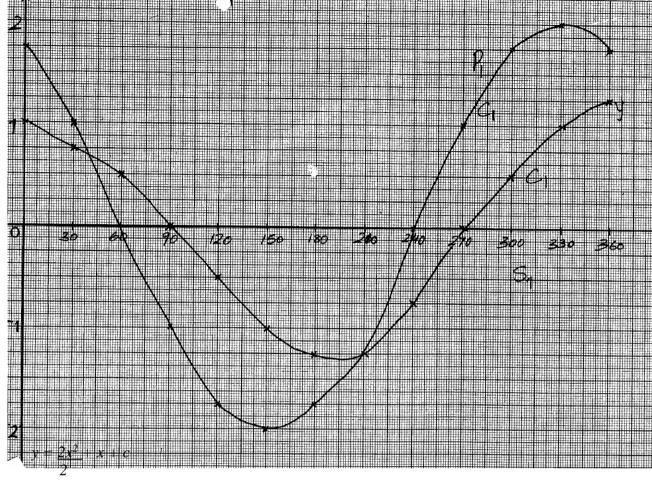
2. *a*)

X	2	5	8	10	
у	5	26	65	101	

b) 
$$A = h (2 + 10 + 26 + 50 + 82)$$
  
= 2 x 170  
= 34 square units

c) 
$$A = (x^2 + 1) dx$$
  
=  $(^{1000}/_3 + 10) - 0$   
=  $333.33 + 10$   
=  $343.33$   
=  $343.33$  square units





$$a + x = -4$$
,  $y = 6$   
 $6 = (-4)^2 - 4 + c$   
 $c = -6$   
 $y = x^2 + x - 6$ 

3.

4. a) 
$$-2t^2 + t + 28 = 0$$
  
 $P = -56$   
 $S = 8, -7$   
 $-2t^2 + 8t - 7t + 28 = 0$   
 $-2t(t-4) - 7(t-4) = 0$   
 $t = 3.5$   
 $t = 4$ 

b) 
$$AC = -4t + 1$$
  
 $-4t + 1 = 0$   
 $T = \frac{1}{4}$   
 $V = -2(\frac{1}{4})2 + \frac{1}{4} + 28$   
 $V = 28.125$ 

c) 
$$Acc = -4t + 1$$
  
 $At \ rest \ t = 3.5, \ t = 4$   
 $Acc = -4 \ x \ 4 + 1$   
 $= -15m/s^2$   
 $At \ t = 3.5$   
 $A = -13m/s^2$ 



d)(i) 
$$D = \frac{2t^3}{3} + \frac{t^2}{2} + 28t + 5$$

$$Distance = -2 \times 3^3/_3 + 3^2/_3 + 28 \times 3 + 5 = 75.5m$$

ii) 
$$D = \frac{2t^3}{3} + \frac{t^2}{2} + 28t + 5$$

$$D = -2x \frac{3^3}{3} + \frac{3^2}{3} + 28x \frac{3}{3} + 5$$

$$= -18 + 4.5 + 84 + 5$$

$$= 70.5 + 5 = 75.5$$

5. 
$$ai$$
  $V = 15 + 4t - 3t^2$ 

$$\frac{dv}{dt} = Acc = 4 - 6t$$

*ii*) 
$$V = 15 + 4t - 3t^2$$

$$V = \frac{dv}{dt} = 15 + 4t - 3t^2$$

$$S = \begin{cases} (15 + 4t - 3t^{2}) dt \\ S = 15t + \frac{4t^{2}}{2} - \frac{3t^{2}}{3} + C \\ S = 15t + 2t^{2} - t^{3} + C \\ b) i) Acc = 0 \text{ hence } \underline{dv} = 0 \\ dt \\ 4 - 6t = 0 \\ -6 = -4 \\ t = \frac{2}{3} \text{ sec.} \end{cases}$$

$$ii) S = \begin{cases} 15t + 2t^2 - t^3 + 0 \\ 0 \end{cases}$$

$$= 15 \binom{2}{3} + 2 \binom{2}{3} - \binom{2}{3} \frac{3}{3}$$

$$= \frac{10}{1} + \frac{8}{9} = \frac{8}{27}$$

$$= \frac{286}{27} = 10.5925 \approx 10.59$$

c) 
$$Acc. 4-6t$$
  
 $-4 = -6t$   
 $t = \frac{2}{3} Acc. = 0$   
 $\therefore$  Time is 0 and  $\frac{2}{3}$ 

Bth. 0 and  $\frac{2}{3}$  sec.

6. (a) 
$$x^2 = -x^2 + 8$$
  
 $2x^2 = 8$   
 $x = 2$   $a = -2$ ,  $b = 2$ 

(b) Area of 
$$\int_{-2}^{2} x^2 = \left(\frac{x^3}{3}\right)_{-2}^{2}$$
  
=  $\frac{8 - 8}{3}$ 

$$Area = (x^{2} + 8)dx$$

$$= \left(\frac{-x^{3}}{3}\right) + 8x$$

$$= \left(\frac{-80}{3} + 16\right) \left(-\frac{-8}{3} - 16\right)$$

= <u>16</u>

(c) 
$$Area = \underline{80} + \underline{16} = \underline{96}$$
  
3 3 3 = 32

7. 
$$a = \frac{d^{2}s}{dt^{2}} = \frac{d^{2}}{dt^{2}} (t^{3} - 5t^{2} + 2t + 5)$$

$$dt^{2} dt^{2} 2$$

$$= \frac{d}{dt} = 3t^{2} - 5t + 2$$

$$dt$$

$$= 6t - 5$$
If  $a = 0$ 

$$6t - 5 = 0$$

$$t = \frac{5}{6}$$

$$v = \frac{ds}{dt} = 3t^{2} - 5t^{2} = 3 \times \frac{25}{6} - 5 \times \frac{5}{6} + 2$$

$$dt$$

$$= -1m/s$$
12

8. (a) 
$$V = 6t + 4 = 3t^2 + 4t + c$$
  
 $5 = 3(0)^2 + 4(0) + c$   
 $5 = c$   
 $V = 3t^2 + 4t + 5$   
(b)  $V = 3(4)^2 + 4(4) + 5$   
 $= 69 \text{ m/s}$ 

(c) (i) 
$$\int 3t^2 + 4t + 5$$
  
=  $t^3 + 2t^2 + 5t + c$   
When  $t = 0$   $S = 0$   
 $S = t^3 + 2t^2 + 5t$ 

(ii) 
$$S = t^3 + 2t^2 + 5t 4$$

$$= (4)^3 + 2(4)^2 + 5(4) - (1)^3 + 2(1)^3 + 5(1)$$

$$9. a) S = 3t + 3t^{2} - 2t^{3}$$

$$\frac{ds}{2} = v = 3 + 3t - 6t^{2}$$

$$\frac{dv}{dt} = a = 3 - 12t \qquad t = 0$$

$$a = 3m/s^{2}$$

b)i) 
$$O = -6t^2 = 3t + 3$$
 $t = 1$ 
 $+6t - 3t$ 

ii) 
$$S = 3(1) + \frac{3(1)^2}{2} - 6(1)^3$$
  
=  $3 + \frac{3}{2} - 2$   
=  $\frac{2}{2} + \frac{3}{2} = \frac{5}{2}$ 

c) 
$$V = 3 + 3(1) - 6(1)$$
  
=  $3+3-6$   
=  $0m/s$ 

10. 
$$dy/dx = 12x2 - 4x - 3 \text{ at } (2,23)$$

$$= 12(4) - 4(2) - 3$$

$$= 48 - 8 - 3$$

$$= 40 - 3$$

$$= 37$$

$$M = y - y \text{ or } y = mx + c$$

$$= \frac{23 - y}{2 - x}$$

$$23 - y = 37(2-x)$$

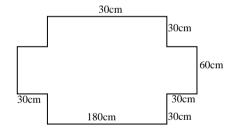
$$23 - y = 74 - x$$

$$23 = 37(2) + c$$

C = 23 - 74 = -51

Hence equation is y = 37x - 5

11.



(i) 
$$(180 \times 30 \times 2) = 10800$$
  
 $(60 \times 30 \times 2) = 3600$   
 $(180 \times 60 \times 1) = 10800$   
 $(180 \times 60 \times 1) = 25200 \text{cm}^2$ 

(ii) Volume of the cuboid  
= 
$$(180 \times 60 \times 30) \text{ cm}^3 = 324,000 \text{cm}^3$$
  
 $Mass = (2.5 \times 180 \times 60 \times 30)$   
=  $\frac{810000}{1000}$   
=  $810 \text{kg}$   
Volume of water =  $(324,000 \text{ cm}^3)$   
 $Mass of water = \frac{(324,000 \times 1)}{1000}$ 

= 324kg

 $Mass\ of\ cuboid\ = 324+810$ 

Full of water = 1,134kg

#### 12. Let length of square cut off be xLength of box = 8 - 2xWidth of box = 5 - 2xHeight of box = x



$$V = (8 - 2x) (5 - 2x)x$$

$$= 4x^3 - 26x^2 + 40x$$

$$\frac{dv}{dx} = 12x^2 - 52x + 40$$

$$12x^2 - 52x + 40 = 0$$

$$3x^2 - 13x + 10 = 0$$

$$3x^2 - 10x - 3x + 10 = 0$$

$$X(3x - 10) - 1(3x - 10) = 0$$

$$(x - 1)(3x - 10) = 0$$

$$x = 1$$

$$x = \frac{10}{3}$$

$$d^{2}/dx^{2} = 24x - 52$$

$$x = 1$$

$$d^{2}/dx^{2} = 24x - 52 = -28$$

maximum

x = 1cm gives maximum vol (8-2) (5-2) X 1 = 6 x 3= 18cm<sup>3</sup>

y = -x - 1

13. a) 
$$\frac{dy}{dx} = 3x^2 - 2$$

$$Gradient of the tangent is 1 so, gradient of the normal is -1$$

$$\frac{y - 2}{x - 1} = \frac{-1}{1}$$

$$\frac{y + 2}{x - 1} = \frac{-1}{1}$$

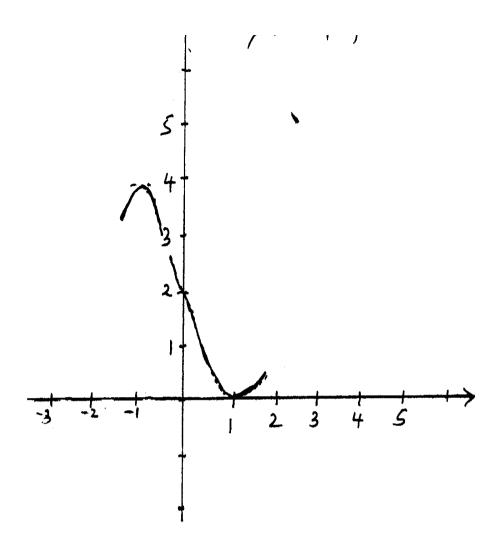
(b) 
$$dy = 3x^2 - 3 = 0$$
  
 $3x^2 - 1) = 0$   
 $(x-1) = 0$   
 $x = 1, y = 0 & x = -1, y = 4$   
Coordinates of turning points  
 $(1,0)$  and  $(-1, 4)$   
For  $(1,0)$   $x < 1$ ,  $dy$  is  $-ve$   
 $dx$   
 $x > 1$ ,  $dy$  is  $+ve$   
 $dx$   
 $(1,0)$  is a minimum point for  $(-1, 4)$   $x < -1$ ,  $dy$  is  $+ve$   
 $dx$   
 $(1, 0)$  is a minimum point for  $(-1, 4)$   $x < -1$ ,  $dy$  is  $+ve$   
 $dx$   
 $x > -1$ ,  $dy$  is  $-ve$   
 $dx$   
 $\Rightarrow (-1, 4)$  is a maximum point

To sketch the curve we

- (i) Its turning points and their nature
- (ii) The points the graph cuts the x and y axis i.e the x and y-intercepts



(b)  $\Rightarrow$ Indicating that the curve turns at (-1, 4) (1, 0) and cuts the y-axis at (0, 2)  $B_1$   $\Rightarrow$  $C_1$  for correct sketch



14. a) 
$$-2t^{2} + t + 28 = 0$$

$$t^{2} - t - 28 = 0$$

$$2t^{2} - 8t + (7t - 28) = 0$$

$$+ (t-4) + 7(t-4) = 0$$

$$t + 7 + (t-4) = 0$$

$$t = -3.5 \text{ or } 4$$

p.B at rest at t=4seconds

(b) 
$$a = 1-4t$$
  
 $1-4t = 0$   
 $0.25s = t$   
 $V = 28 + 25 - 2(0.25)^2$   
 $= 28.25 - 0.125$   
 $V = 28.125m/s$ 

(c) (i) 
$$S = 28t + t^2 - 2t^3 + C$$
  
2 3  
when  $t = 0$ ,  $s = 0$   
 $\therefore S = 28t + t^2 - 2t$ 

PB at rest after 4s  

$$\therefore S = 28 \times 4 \times 42 - 2 \times 4^{3}$$

$$3$$

$$= 112 + 8 - 42.667$$

$$= 120 - 42.6667 = 77.33m$$

15. 
$$S = t^{3} - 3t^{2} + 2t$$
(a) 
$$V = \underline{ds} = 3t^{2} - 6t + 2$$

$$dt$$
When 
$$t = 2$$

$$V = 3(4) - 6(2) + 2$$

$$= 2m/s$$

(b) At minimum velocity:  $\frac{dv}{dt} = 0$   $\frac{dv}{dt} = 6t - 6$   $\frac{dt}{dt}$  6t - 6 = 0 t = 1  $Min-velocity = 3(1)^2 - 6(1) + 2$ 

$$(c) 3t^2 - 6t + 2 = 0$$

= -1m/s

$$t = \frac{6 \pm (-6) - 4(3)(2)}{6}$$

$$= \frac{6 \pm 5.2}{6}$$

$$t = 1.58 \text{ or } 0.4\text{sec}$$

$$(d) \ acc = \frac{dv}{dt} = 6t - 6$$

$$dt$$

$$a = 6(3) - 6 = 12\text{m/s}^2$$

### 60. Approximation of area

$$A = 0.8 (5 + 5) + 2 (7.56 + 8.84 + 8.84 + 7.56)$$

$$\begin{cases} = 0.4 & 10 + 2 \\ 0.4 & x = 75.6 \\ = 30.24 & sq. & units \end{cases}$$

2. 
$$y_0 = 0$$
  
 $y_1 = 2.5$   
 $y_2 = 6$   
 $y_3 = 10.5$   
 $y_4 = 16$   
 $y_5 = 22.5$   
 $y_6 = 30$   
 $A = \frac{1}{2}x 1(0+30) + 2(2.5+6+10.5+16+22.5)$   
 $= \frac{1}{2}x 145 = 72.5$   
(b)  $\frac{1}{2}x^2 - 2 = \frac{x^3}{6} - x$   
 $= \frac{8^3}{6} - 8 - \frac{2^3}{6} - 2$   
 $= 77.33 - 0.67$   
 $= 78 \text{ square units}$ 

(c) % error = 
$$\frac{72.5 - 78}{78}x$$
 100  
= -7.05%

3 
$$y_0 = 0$$
  
 $y_1 = 2.5$   
 $y_2 = 6$   
 $y_3 = 10.5$   
 $y_4 = 16$   
 $y_5 = 22.5$   
 $y_6 = 30$   
 $A = \frac{1}{2}x 1(0+30) + 2(2.5+6+10.5+16+22.5)$   
 $= \frac{1}{2}x 145$   
 $= 72.5$ 



$$\begin{array}{rcl}
(b) & \frac{1}{2}x^2 - 2 & = & \frac{x^3}{6} - x \\
& = & \frac{8^3}{6} - 8 - & \frac{2^3}{6} - 2 \\
& = & \frac{77.33}{6} - 0.67 \\
& = & 78 \text{ square units}
\end{array}$$

(c) % error = 
$$\frac{72.5 - 78}{78}$$
 x 100  
= -7.05%

4 a) 
$$-2x^{2} + 3x + 4 = 2x + 3$$

$$-2x^{2} + x + 1 = 0$$

$$-2x^{2} + 2x - x + 1 = 0$$

$$(x-1)(-2x-) = 0$$

$$x = 1 \text{ or } x = -\frac{1}{2}$$

$$when x = 1 \text{ } y = 2x \text{ } 1 + 3 = 5$$

$$Q(1, 5)$$

$$(b) -2x^{2} + 3x + 4)dx - (2x+3)dx$$

5. a) X -5.5 -5 -4.25 -3.75 y 16.25 12 6.56 3.56

b) 
$$A = 0.5 (18.56 + 14.06 + 10.06 + 6.56 + 3.56 + 1.06)$$
  
=  $0.5 \times 53.86 = 26.93$ 

c) i) 
$$\int x^{1} + 2x - 3$$

$$[x^{3} + x^{2} - 3x]^{-3}$$

$$3$$

$$= [(-3)^{3} + (-3)^{2} - 3(-3)]$$

$$= 9 + 18 = 27 \text{ square units}$$
ii) 
$$\frac{27 - 26.93}{27} \quad X \cdot 100$$

$$= 0.25925 \% = 0.2593 \%$$

6

х	2	2.5	3	3.5	4	4.5	5	5.5	6	6.5	7
у	18	28. 25	<i>4 1</i>	<i>56. 25</i>	7 4	94. 25	1 1	142 .25	<i>1 7</i>	20 0.2	23 3
							7		0	5	

$$\therefore Area = \frac{1}{2} n \quad (y_0 + y_n) + 2(y_1 + \dots y_n - 1)$$

$$= \frac{1}{2} (1) \left\{ (18 + 233) + 2(41 + 74 + 55 + 170) \right\}$$

$$= \frac{1}{2} \left\{ 251 + 2(340) \right\}$$

= 
$$\frac{1}{2}$$
 (251 + 680)  
=  $\frac{1}{2}$  (831)  
= 415.5 sq. units.

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## 65. Integration

$$S_{10} = 100$$

$$\int_{2}^{6} 2 \frac{(x-1)(x-2)}{(x-2)} dx$$

$$x - 2$$

$$= \int_{2}^{6} 2x - 1 dx$$

$$= \int_{2}^{x^{2}/2} 2x \int_{2}^{6} 2x$$

2. 
$$\int (x^2 + 1) dx = 2a$$

$$\left(\frac{x^3 + x}{3} = 2a\right)_0^a$$

$$\frac{a^3 + a - 0}{3} = 2a$$

$$a^3 + 3a = 6a$$

$$a^3 = 3a$$

$$(a^3 - 3a) = 0$$

$$a(a^2 - 3) = 0$$

$$a = 0$$

$$or 3 = \pm 1.732$$