## 1. Volume and capacity

1. The figure below shows a bucket of depth 30 cm used to fill a cylindrical tank of radius 1.2 m and height 1.35 m which is initially three-fifth full of water.

a) Calculate, in terms of $\Pi$;
(i) The capacity of the bucket in litres
(ii) The volume of water required to fill the tank in litres
(iii) Calculate the number of buckets that must be drawn to fill the tank
(3mks)
2. A bucket is in the shape of a frustum with base radius 12 cm and top radius 16 cm . The slant height of the bucket is 30 cm as shown below. The bucket is full of water.
(a) Calculate the volume of the water. (Take $\pi=3.142$ )

(b) All the water is poured into a cylindrical container of circular radius 12 cm . If the cylinder has height 45 cm , calculate the surface area of the cylinder which is not in contact with water. (4 marks)
3. The British government hired two planes to airlift football fans to South Africa for the World cup tournament. Each plane took $101 / 2$ hours to reach the destination.
Boeng 747 has carrying capacity of 300 people and consumes fuel at 120 litres per minute. It makes 5 trips at full capacity. Boeng 740 has carrying capacity of 140 people and consumes fuel at 200 litres per minute. It makes 8 trips at full capacity. If the government sponsored the fans one way at the cost of 800 dollars per fan, calculate:
(a) The total number of fans airlifted to South Africa.
(b) The total cost of fuel used if one litre costs 0.3 dollars.
(c) The total collection in dollars made by each plane.
(d) The net profit made by each plane.
4. The figure below represents a part in form of a frustum of a right circular cover. The upper and the lower radii are 50 cm and 15 cm respectively. The slant height is 70 cm .

a. Calculate the height of the pail. $(5 \mathrm{~cm})$
b. Find the capacity of the pail to the nearest a litre. ( 5 mks )
5. Consider the vessel below

a) Calculate the volume of water in the vessel.
b) When a metallic hemisphere is completely submerged in the water, the level of the water rose by 6 cm . Calculate:
i) the radius of the new water surface.
ii) the volume of the metallic hemisphere (to 4 s.f)
iii) the diameter of the hemisphere
6. A village water tank is in the form of a frustrum of a cone of height 3.2 m .

The top and bottom radii are 18 m and 24 m respectively
(a) Calculate:
(i) The surface area of the tank excluding the bottom
(ii) The capacity of the water tank
(b) 15 families each having 15 members use the water tank and each person uses
7. The diagram below shows a bucket with a top diameter 30 cm and bottom diameter 20 cm .

The height of the bucket is 28 cm
(a) Calculate the capacity of the bucket in litres

(b) Find the area of the metal sheet required to make 100 such buckets taking $10 \%$ extra for overlapping and wastage
8. A rectangular water tank measures 2.6 m by 4.8 m at the base and has water to a height of 3.2 m . Find the volume of water in litres that is in the tank
9. The figure alongside shows a cone from which a frustum is made. A plane parallel to the base cuts the cone two thirds way up the vertical height of the cone to form frustum ABCD. The top surface radius of the frustum is labeled $\mathbf{r}$ and the bottom radius is $\mathbf{R}$

a) Find the ratio $r: R$
b) Given that $r=7 \mathrm{~cm}$, find R
c) If the height VY of the original cone is 45 cm , calculate to the nearest whole number the volume of the frustum
d) The frustum represents a bucket which is used to fill a rectangular tank measuring 1.5 m long, 1.2 m wide and 80 cm high with water. How many full buckets of water are required to fill the tank
10. Three litres of water (density $1 \mathrm{~g} / \mathrm{cm}^{3}$ ) is added to twelve litres of alcohol (density $0.8 \mathrm{~g} / \mathrm{cm}^{3}$. What is the density of the mixture?
11. A rectangular tank whose internal dimensions are 2.2 m by 1.4 m by 1.7 m is three fifth full of milk.
(a) Calculate the volume of milk in litres
(b) The milk is packed in small packets in the shape of a right pyramid with an equilateral base triangle of sides 10 cm . The vertical height of each packet is 13.6 cm . Full packets obtained are sold at shs. 30 per packet. Calculate:
(i) The volume in $\mathrm{cm}^{3}$ of each packet to the nearest whole number
(ii) The number of full packets of milk
(iii) The amount of money realized from the sale of milk
12. An 890 kg culvert is made of a hollow cylindrical material with outer radius of 76 cm and an inner radius of 64 cm . It crosses a road of width 3 m , determine the density of the material used in its construction in $\mathrm{Kg} / \mathrm{m}^{3}$ correct to 1 decimal place.

