## 1. Statistics II

1. The table below shows the number of defective bolts from a sample of 40

| No of bolts | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 20 | 8 | 6 | 4 | 1 | 1 |

Calculate the standard deviation of the data above
2. The table below shows the masses to the nearest kg of all the students of marigu-ini secondary. School.

| Masses (kg) | No. of students |
| :--- | :--- |
| $30-34$ | 5 |
| $35-39$ | 7 |
| $40-44$ | 10 |
| $45-49$ | 10 |
| $50-54$ | 19 |
| $55-59$ | 20 |
| $60-64$ | 20 |
| $65-69$ | 6 |
| $70-74$ | 2 |
| $75-79$ | 1 |

a) Taking the assumed mean $\mathrm{A}=52 \mathrm{~kg}$

Calculate:
(i) the actual mean mass of the students.
(3 marks)
(ii) the standard deviation of the distribution.
(3 marks)
b) Draw a cumulative frequency curve and use it to estimate the number of students whose masses lie between 44.5 kg and 59.5 kg .
3. Sixty form four students in Tahidi high sat for a mathematics examination. Their marks were grouped into seven classes as follows: $30-34,35-39,40-44,45-49,50-54,55-59,60-64$ and then named as cheetah, lion, zebra, rabbit, giraffe, elephant and buffalo respectively. The form 4 students population was then analyzed in the form of a pie-chart as shown below.


Using the information above
(a) Complete the table below.

| Name | Marks | No. of students |
| :--- | :--- | :--- |
| Cheetah | $30-34$ |  |
| Lion | $35-39$ |  |
| Zebra | $40-44$ |  |
| Rabbit | $45-49$ |  |
| Giraffe | $50-54$ |  |
| Elephant | $55-59$ |  |
| Buffalo | $60-64$ |  |

(b) Calculate the inter quartile range.
(c) Using an assumed mean of 47, calculate the standard deviation of the data.
4. At an agricultural Research Centre, the length of a sample of 50 maize cobs were measured and recorded as shown in the frequency distribution table below.

| Length | $8-10$ | $11-13$ | $14-16$ | $17-19$ | $20-22$ | $23-24$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of Labs | 4 | 7 | 11 | 15 | 8 | 5 |

a) State the modal class and size.

Calculate
b) the mean
c) (i) the variance
(ii) the standard deviation.
5. The table below shows the masses to the nearest kg of a number of people.

| Mass (kg) | $50-54$ | $55-59$ | $60-64$ | $65-69$ | $70-74$ | $75-79$ | $80-84$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 19 | 23 | 40 | 28 | 17 | 9 | 4 |

a)Using an assumed mean of 67.0 , calculate to one decimal place the mean mass.
(b) Calculate to one decimal place the standard deviation of the distribution.
6. Use only a ruler and pair of compasses in this question;
(a) construct triangle ABC in which $\mathrm{AB}=7 \mathrm{~cm}, \mathrm{BC}=6 \mathrm{~cm}$ and $\mathrm{AC}=5 \mathrm{~cm}$
(b) On the same diagram construct the circumcircle of triangle ABC and measure its radius
(c) Construct the tangent to the circle at C and the internal bisector of angle BAC. If these lines meet at D , measure the length of AD
7. Below is a histogram drawn by a student of Got Osimbo Girls Secondary School.

a) Develop a frequency distribution table from the histogram above.
b) Use the frequency distribution table above to calculate;
i) The inter-quartile range.
ii) The sixth decile.
8. ABC is a triangle drawn to scale. A point $\mathbf{x}$ moves inside the triangle such that
i) $\mathrm{AX} \leq 4 \mathrm{~cm}$
ii) $\mathrm{BX}>\mathrm{CX}$
iii) Angle $\mathrm{BCX} \leq$ Angle XCA.

Show the locus of $\mathbf{X}$.

9. The following able shows the distribution of marks of 80 students

| Marks | $1-10$ | $11-20$ | $21-30$ | $31-40$ | $41-50$ | $51-60$ | $61-70$ | $71-80$ | $81-90$ | $91-100$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 1 | 6 | 10 | 20 | 15 | 5 | 14 | 5 | 3 | 1 |

(a) Calculate the mean mark
(b) Calculate the semi-interquartile range
(c) Workout the standard deviation for the distribution
10. The table below shows the marks of 90 students in a mathematical test

| Marks | $5-9$ | $10-14$ | $15-19$ | $20-24$ | $25-29$ | $30-34$ | $35-39$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of students | 2 | 13 | 31 | 23 | 14 | $\mathbf{X}$ | 1 |

a) Find $\mathbf{X}$
b) State the modal class
(c) Using a working mean of 22, calculate the; i) Mean mark
ii) Standard deviation
11. (a) Using a ruler and a pair of compasses only construct triangle $P Q R$ in which $P Q=5 \mathrm{~cm}$, $\mathrm{PR}=4 \mathrm{~cm}$ and $\angle \mathrm{PQR}=30^{\circ}$
(b) Measure; (i) RQ
(ii) $\angle \mathrm{PQR}$
(c) Construct a circle, centre O such that the circle passes through vertices $\mathrm{P}, \mathrm{Q}$, and R
12. The ages of 100 people who attended a wedding were recorded in the distribution table below

| Age | $0-19$ | $20-39$ | $40-59$ | $60-79$ | $80-99$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 7 | 21 | 38 | 27 | 7 |

a) Draw the cumulative frequency
b) From the curve determine: i) Median
ii) Inter quartile range
iii) $7^{\text {th }}$ Decile
iv) $60^{\text {th }}$ Percentile
13. The marks obtained by 10 students in a maths test were:-
$25,24,22,23, x, 26,21,23,22$ and 27
The sum of the squares of the marks, $\Sigma x^{2}=5154$
(a) Calculate the:
(i) value of $x$
(ii) Standard deviation
(b) If each mark is increased by 3 , write down the:-
(i) New mean
(ii) New standard deviation
14. 40 form four students sat for a mathematics test and their marks were distributed as follows:-

| Marks | $1-10$ | $11-$ <br> 20 | $21-30$ | $31-40$ | $41-50$ | $51-60$ | $61-70$ | $71-80$ | $81-90$ | $91-100$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> students | 1 | 3 | 4 | 7 | 12 | 9 | 2 | 1 | 0 | 1 |

a) Using 45.6 as the working mean, calculate;
i) The actual mean.
ii) The standard deviation.
b) When ranked from first to last, what mark was scored by the $30^{\text {th }}$ student?
(Give your answer correct to 3 s.f.)
15. The table below shows the distribution of marks scored by pupils in a maths test at Nyabisawa Girls.

| Marks | $11-20$ | $21-30$ | $31-40$ | $41-50$ | $51-60$ | $61-70$ | $71-80$ | $81-90$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 2 | 5 | 6 | 10 | 14 | 11 | 9 | 3 |

a)Using an Assumed mean 45.5, calculate the mean score.
b) Calculate the median mark.
c) Calculate the standard deviation.
d) State the modal class.
16. The table below shows the marks scored in a mathematics test by a form four class;

| Marks | $20-29$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of students | 4 | 26 | 72 | 53 | 25 | 9 | 11 |

(a) Using an assumed mean of 54.5, calculate:-
(i) The mean
(ii) The standard deviation
(b) Calculate the inter quartile range

