## 1. Graphical Methods

1. The equation of a circle is given as
$2 x^{2}+2 y^{2}-8 x+5 y+10=0$. Find the radius of the circle and the coordinates of its centre. (3 mks)
2. The equation of a circle is given by $x^{2}+4 x+y^{2}-5=0$. Find the centre of the circle and its radius.
3. The equation of a circle is $x^{2}+y^{2}+6 x-10 y-2=0$. Determine the co-ordinates of the centre of the circle and state its radius
4. In the diagram below ABE is a tangent to a circle at B and DCE is a straight line. If $\mathrm{ABD}=60^{\circ}, \mathrm{BOC}=80^{\circ}$ and O is the centre of the circle, find with reasons $\angle \mathrm{BEC}$

5. Obtain the centre and the radius of the circle represented by the equation:
$x^{2}+y^{2}-10 y+16=0$
6. Complete the table below, for the function $y=x^{3}+6 x^{2}+8 x$

| x | -5 | -4 | -3 | -2 | -1 | 0 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{x}^{3}$ | -125 |  | -27 | -8 |  | 0 | 1 |
| $6 \mathrm{x}^{2}$ |  | 96 | 54 |  | 6 | 0 | 6 |
| 8 x | -40 |  | -24 |  |  | 0 | 8 |
| y |  |  | 3 | 0 |  | 0 | 15 |

(a) Draw a graph of the function $y=x^{3}+6 x^{2}+8 x$ for $-5 \leq x \leq 1$ and use the graph to estimate the roots of the equation $x^{3}+6 x^{2}+8 x=0$
(b) Find which values of $\mathbf{x}$ satisfy the inequality $x^{3}+6 x^{2}+8 x-1>0$
7. Sketch the curve of the function $y=x^{3}-3 x+2$ showing clearly minimum and maximum points and the y - intercept.
8. Show that $4 y^{2}+4 x^{2}=12 x-12 y+7$ is the equation of a circle, hence find the co-ordinates of the centre and the radius
9. Two variables R and P are connected by a function $\mathrm{R}=\mathrm{KP}{ }^{\mathrm{n}}$ where K and n are constants. The table below shows data involving the two variables

| P | 3 | 3.5 | 4 | 4.5 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| R | 36 | 49 | 64 | 81 | 100 |

(a) Express $\mathbf{R}=\mathbf{K} \mathbf{P}^{\mathbf{n}}$ in a linear form
(b) Draw a line graph to represent the information above
(c) Find the values of constants $\mathbf{K}$ and $\mathbf{n}$
(d) Write down the law connecting $\mathbf{R}$ and $\mathbf{P}$
(e) Find the value of $\mathbf{P}$ when $\mathbf{R}=\mathbf{9 0 0}$
10. A circle of radius 3 cm has the centre at $(-2,3)$. Find the equation of the circle in the form of $x^{2}+y^{2}+P x+q y+c=0$
11. In an experiment, the values of two quantities $V$ and $T$ were observed and the results recorded as shown below.

| V | 0 | 2 | 4 | 6 | 8 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| T | 0.49 | 0.30 | 0.24 | 0.20 | 0.16 | 0.137 |

It is known that $\mathbf{T}$ and $\mathbf{V}$ are related by a law of the form $T=\frac{a}{b+V}$
where $\mathbf{a}$ and $\mathbf{b}$ are constants.
a) Draw the graph of $\underline{I}$ against V

T
b) Use your graph to find;
i) The values of $\mathbf{a}$ and $\mathbf{b}$.
ii) $\mathbf{V}$ when $\mathbf{T}=0.38$
iii) $\mathbf{T}$ when $\mathbf{V}=4.5$
12. Find the equation of the tangent to the curve $y=2 x^{3}+x^{2}+3 x-1$ at the point ( $1,-5$ ) expressing you answer in the form $\mathrm{y}=\mathrm{m} x+\mathrm{c}$
13. Given that :- $\quad 243=(81)^{-1} \times(1 / 27)^{x}$ determine the value of $x$
14. Show that $3 x^{2}+3 y^{2}+6 x-12 y-12=0$ is an equation of a circle hence state the radius and centre of the circle
15. (a) Fill in the table below for the function $y=-6+x+4 x^{2}+x^{3}$ for $-4 \leq x \leq 2$

| $x$ | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -6 | -6 | -6 | -6 | -6 | -6 | -6 | -6 |
| $x$ | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| $4 x^{2}$ |  |  | 16 |  |  | 4 |  |
| $x^{3}$ |  |  |  |  |  |  |  |
| y |  |  |  |  |  |  |  |

(b) Using the grid provided draw the graph for $y=-6+x+4 x^{2}+x^{3}$ for $-4 \leq x \leq 2$
(c) (i) Use the graph to solve the equations:-
(i) $x^{3}+4 x^{2}+x-4=0$
(ii) $-6+x+4 x^{2}+x^{3}=0$
(iii) $-2+4 x^{2}+x^{3}=0$
16. The table below shows the results obtained from an experiment to determine the relationship between the length of a given side of a plane figure and its perimeter

| Length of side $\mathbf{t}(\mathrm{cm})$ | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Perimeter P $(\mathrm{cm})$ | 6.28 | 12.57 | 18.86 | 21.14 | 31.43 |

(a) On the grid provided, draw a graph of perimeter $\mathbf{P}$, against 1
(b) Using your graph determine;
(i) the perimeter of a similar figure of side 2.5 cm
(ii) the length of a similar figure whose perimeter is 9.43 cm
(iii) the law connecting perimeter p and the length i
(c) If the law is of the form $\mathbf{P}=\mathbf{2 k} \mathbf{~}+\mathbf{c}$ where $\mathbf{k}$ and $\mathbf{c}$ are constants, find the value of $\mathbf{k}$
17. In an experiment with tungsten filament lamp, the reading below of voltage (V) current (I), power $(\mathrm{P})$ and resistance $(\mathrm{R})$ were obtained. It was established that $\mathbf{P}$ was related to $\mathbf{R}$ by a law $P=a R^{n}-0.6$. Where $\mathbf{a}$ and $\mathbf{n}$ are constants.

| $\mathbf{V}$ | 1.30 | 2.00 | 2.80 | 4.40 | 5.70 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{I}$ | 1.50 | 1.80 | 2.10 | 2.50 | 2.90 |
| $\mathbf{P}$ | 0.73 | 2.05 | 3.28 | 7.44 | 10.62 |
| $\mathbf{R}$ | 0.89 | 1.13 | 1.33 | 1.78 | 1.99 |

Plot a suitable line graph and hence use it to determine the value of $\mathbf{a}$ and $\mathbf{n}$
18. Find the gradient of a line joining the centre of a circle whose equation is $\mathbf{x}^{2}+\mathbf{y}^{2}-\mathbf{6 x}=\mathbf{3}-\mathbf{4 y}$ and a point $\mathrm{P}(6,7)$ outside the circle..
19. a) Complete the table below for the function $\mathbf{y}=-\mathbf{x}^{3}+\mathbf{2} \mathbf{x}^{2}-\mathbf{4 x}+\mathbf{2}$.

| $\mathbf{x}$ | $\mathbf{- 3}$ | $\mathbf{- 2}$ | $\mathbf{- 1}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $-\mathrm{x}^{3}$ | 27 | 8 |  | 0 |  | -8 |  |  |
| $2 \mathrm{x}^{2}$ | 18 | 8 | 2 | 0 |  |  |  |  |
| -4 x |  | 8 |  | 0 |  |  |  | -16 |
| 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| y |  | 26 |  | 2 |  | -6 |  | -46 |

b) On the grid provided below draw the graph of $-x^{3}+2 x^{2}-4 x+2$ for $-3 \leq x \leq 4$.
c) Use the graph to solve the equation $-\mathbf{x}^{3}+\mathbf{2} \mathbf{x}^{2}-\mathbf{4 x}+\mathbf{2}=\mathbf{0}$.
d) By drawing a suitable line on the graph solve the equation. $-\mathbf{x}^{\mathbf{3}}+\mathbf{2} \mathrm{x}^{2}-\mathbf{5 x}+\mathbf{3}=\mathbf{0}$.
20. Determine the turning point of the curve $y=4 x^{3}-12 x+1$. State whether the turning point is a maximum or a minimum point.
21. (a) Complete the table below for the equation of the curve given by $\mathbf{y}=\mathbf{2} \mathbf{x}^{\mathbf{3}}-\mathbf{3} \mathbf{x}^{\mathbf{2}}+\mathbf{1}$

| $\mathbf{X}$ | -2 | -1.5 | -1 | -0.5 | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2 \mathbf { x } ^ { 3 }}$ | -16 |  | -2 |  | 0 |  | 2 |  | 16 |  |  |
| $\mathbf{- 3 \mathbf { x } ^ { 2 }}$ | -12 |  |  | 0.75 | 0 | -0.75 |  |  |  |  | -27 |
| $\mathbf{1}$ | 1 |  |  |  | 1 |  |  |  |  |  |  |
| $\mathbf{y}$ | -27 | -12.5 |  |  | 1 |  |  |  |  |  | 13.5 |

(b) Use the table to draw the graph of the function $\mathbf{y}=\mathbf{2} \mathbf{x}^{3}-\mathbf{3} \mathbf{x}^{2}+\mathbf{1}$
c) Use your graph to find the values of $x$ for :-
(i) $\mathrm{y}>0$
(ii) The roots of the equation $2 x^{3}-3 x^{2}+1=0$
(iii) $2 x^{3}-3 x^{2}=9$
22. Find the radius and the centre of a circle whose equation is :

$$
2 x^{2}+2 y^{2}-6 x+10 y+9=0
$$

