

GRADE 10 CORE MATHEMATICS
MID TERM 2 EXAM 2026
MARKING SCHEME

SECTION A: 40 MARKS

Question 1: Simplify: $(2x^2y)(3xy^3)$

[4 marks marks]

$$\begin{aligned} & (2x^2y)(3xy^3) \\ & = 2 \times 3 \times x^2 \times x \times y \times y^3 \\ & = 6 \times x^{(2+1)} \times y^{(1+3)} \\ & = 6x^3y^4 \end{aligned}$$

✓ **Final answer: $6x^3y^4$ (4 marks)**

Question 2: Solve: $3(2x - 5) = 4x + 7$

[4 marks marks]

$$\begin{aligned} 3(2x - 5) & = 4x + 7 \\ 6x - 15 & = 4x + 7 && [1 \text{ mark - expanding}] \\ 6x - 4x & = 7 + 15 && [1 \text{ mark - collecting like terms}] \\ 2x & = 22 && [1 \text{ mark - simplifying}] \\ x & = 11 && [1 \text{ mark - solution}] \\ \checkmark \text{ Check: } & 3(2(11) - 5) = 3(22 - 5) = 3(17) = 51; && 4(11) + 7 = 44 + 7 = 51 \checkmark \end{aligned}$$

Question 3: A number increased by 20% to give 96. Find the original number.

[4 marks marks]

$$\begin{aligned} \text{Let the original number} & = x && [1 \text{ mark - set up variable}] \\ 20\% \text{ of } x & = 0.2x \\ x + 0.2x & = 96 && [1 \text{ mark - setting up equation}] \\ 1.2x & = 96 && [1 \text{ mark - simplifying}] \\ x & = 96 \div 1.2 \\ x & = 80 && [1 \text{ mark - solution}] \\ \checkmark \text{ Check: } & 80 + 20\% \text{ of } 80 = 80 + 16 = 96 \checkmark \end{aligned}$$

Question 4: Evaluate: $2^3 \times 2^5 \div 2^4$

[4 marks marks]

Using law of indices: $a^m \times a^n = a^{m+n}$ and $a^m \div a^n = a^{m-n}$

$$\begin{aligned}
 &2^3 \times 2^5 \div 2^4 \\
 &= 2^{(3+5-4)} && [2 \text{ marks - applying law of indices}] \\
 &= 2^4 && [1 \text{ mark - simplifying exponent}] \\
 &= 16 && [1 \text{ mark - final answer}]
 \end{aligned}$$

Question 5: Factorize completely: $x^2 - 9x + 20$

[4 marks marks]

We need two numbers that:

- Multiply to give 20
- Add to give -9

Those numbers are -4 and -5 [1 mark - identifying factors]

$$x^2 - 9x + 20 = (x - 4)(x - 5) \quad [2 \text{ marks - factorisation}]$$

✓ **Check:** $(x - 4)(x - 5) = x^2 - 5x - 4x + 20 = x^2 - 9x + 20$ ✓ [1 mark - verification]

Question 6: Triangle with sides 6 cm, 8 cm, 10 cm. Is it right-angled?

[4 marks marks]

For a right-angled triangle, Pythagorean theorem states:

$$(\text{Longest side})^2 = (\text{Other side})^2 + (\text{Other side})^2$$

$$\text{Check: } 10^2 = 6^2 + 8^2 \quad [1 \text{ mark - setting up check}]$$

$$100 = 36 + 64$$

$$100 = 100 \quad \checkmark \quad [2 \text{ marks - calculation}]$$

Yes, the triangle is right-angled.

✓ **Reason:** The Pythagorean theorem is satisfied. [1 mark - conclusion and reason]

Question 7: Simplify the ratio 24:36:60

[4 marks marks]

Find the HCF (Highest Common Factor) of 24, 36, and 60

$$24 = 2^3 \times 3 \quad [1 \text{ mark - prime factorisation}]$$

$$36 = 2^2 \times 3^2$$

$$60 = 2^2 \times 3 \times 5$$

$$\text{HCF} = 2^2 \times 3 = 12 \quad [1 \text{ mark - finding HCF}]$$

$$24:36:60 = 24 \div 12 : 36 \div 12 : 60 \div 12 \quad [1 \text{ mark - dividing by HCF}]$$

$$= 2:3:5 \quad [1 \text{ mark - final answer}]$$

Question 8: Machine gives 15% loss. Cost price Sh 2,000. Find selling price.

[4 marks marks]

$$\text{Cost Price (CP)} = \text{Sh } 2,000 \quad [1 \text{ mark}]$$

$$\text{Loss} = 15\% \text{ of CP}$$

$$\text{Loss} = 15\% \times 2,000 \quad [1 \text{ mark - calculating loss}]$$

$$= 0.15 \times 2,000$$

$$= \text{Sh } 300$$

$$\text{Selling Price} = \text{CP} - \text{Loss} \quad [1 \text{ mark - using formula}]$$

$$= 2,000 - 300$$

$$= \text{Sh } 1,700 \quad [1 \text{ mark - final answer}]$$

Question 9: Average of 6, 8, 10, x and 14 is 10. Find x.

[4 marks marks]

$$\text{Average} = \text{Sum of values} / \text{Number of values} \quad [1 \text{ mark - formula}]$$

$$10 = (6 + 8 + 10 + x + 14) / 5$$

$$10 = (38 + x) / 5 \quad [1 \text{ mark - summing known values}]$$

$$10 \times 5 = 38 + x \quad [1 \text{ mark - multiplying both sides by 5}]$$

$$50 = 38 + x$$

$$x = 50 - 38$$

$$x = 12 \quad [1 \text{ mark - solution}]$$

$$\checkmark \text{ Check: } (6 + 8 + 10 + 12 + 14) / 5 = 50 / 5 = 10 \checkmark$$

Question 10: Class has 12 boys and 18 girls. Probability of selecting a boy.

[4 marks marks]

$$\text{Total students} = 12 + 18 = 30 \quad [1 \text{ mark - total}]$$

$$\text{Number of boys} = 12 \quad [1 \text{ mark}]$$

$$\text{Probability} = \text{Favourable outcomes} / \text{Total outcomes}$$

$$P(\text{boy}) = 12/30 \quad [1 \text{ mark - setting up probability}]$$

$$= 2/5 \text{ or } 0.4 \text{ or } 40\% \quad [1 \text{ mark - simplifying}]$$

SECTION B: 60 MARKS

Students should answer any 5 questions from this section

Question 11: Simultaneous Equations and Linear Expression

[6 marks marks]

(a) Solve: $2x + y = 11$ and $x - y = 1$

From the second equation: $x - y = 1$

$$x = y + 1 \quad [1 \text{ mark - rearranging}]$$

Substitute into first equation:

$$2(y + 1) + y = 11 \quad [1 \text{ mark - substituting}]$$

$$2y + 2 + y = 11$$

$$3y + 2 = 11 \quad [1 \text{ mark - simplifying}]$$

$$3y = 9$$

$$y = 3 \quad [1 \text{ mark - solving for } y]$$

$$x = y + 1 = 3 + 1 = 4 \quad [1 \text{ mark - solving for } x]$$

✓ **Verification:** $2(4) + 3 = 11$ ✓ and $4 - 3 = 1$ ✓

(b) Find the value of $3x - 2y$

$$3x - 2y = 3(4) - 2(3) \quad [0.5 \text{ marks - substituting values}]$$

$$= 12 - 6$$

$$= 6 \quad [0.5 \text{ marks - final answer}]$$

Question 12: Triangle on Cartesian Plane

[6 marks marks]

(a) Plot the triangle on a Cartesian plane

Triangle PQR with P(1,2), Q(5,2), and R(5,6) plotted correctly

✓ **Diagram showing correct coordinates and triangle shape (2 marks)**

(b) Find the area of triangle PQR

From coordinates: P(1,2), Q(5,2), R(5,6)

Base PQ is horizontal from (1,2) to (5,2)

$$\text{Length of base} = 5 - 1 = 4 \text{ units} \quad [1 \text{ mark}]$$

Height = perpendicular distance from R to PQ

$$\text{Height} = 6 - 2 = 4 \text{ units} \quad [1 \text{ mark}]$$

$$\text{Area} = \frac{1}{2} \times \text{base} \times \text{height} \quad [1 \text{ mark - formula}]$$

$$= \frac{1}{2} \times 4 \times 4$$

$$= \frac{1}{2} \times 16$$

$$= 8 \text{ square units} \quad [1 \text{ mark - final answer}]$$

Question 13: Rectangular Field - Perimeter and Area

[6 marks marks]

(a) Find the perimeter

$$\text{Length (L)} = 60 \text{ m, Width (W)} = 35 \text{ m}$$

$$\text{Perimeter} = 2(L + W) \quad [1 \text{ mark - formula}]$$

$$= 2(60 + 35)$$

$$= 2(95)$$

$$= 190 \text{ m} \quad [1 \text{ mark - final answer}]$$

(b) Find the area in m^2 and hectares

$$\text{Area} = L \times W \quad [1 \text{ mark - formula}]$$

$$= 60 \times 35$$

$$= 2,100 \text{ m}^2 \quad [1 \text{ mark - in square meters}]$$

Converting to hectares:

$$1 \text{ hectare} = 10,000 \text{ m}^2 \quad [1 \text{ mark - conversion factor}]$$

$$\text{Area} = 2,100 \div 10,000$$

$$= 0.21 \text{ hectares} \quad [1 \text{ mark - in hectares}]$$

Question 14: Right-angled Triangle - Area and Hypotenuse

[6 marks marks]

(a) Find the area

$$\text{Base} = 12 \text{ cm, Height} = 5 \text{ cm}$$

$$\text{Area} = \frac{1}{2} \times \text{base} \times \text{height} \quad [1 \text{ mark - formula}]$$

$$= \frac{1}{2} \times 12 \times 5$$

$$= 6 \times 5$$

$$= 30 \text{ cm}^2 \quad [1 \text{ mark - final answer}]$$

(b) Find the length of the hypotenuse

$$\text{Using Pythagorean theorem: } c^2 = a^2 + b^2 \quad [1 \text{ mark - formula}]$$

$$c^2 = 12^2 + 5^2$$

$$c^2 = 144 + 25 \quad [1 \text{ mark - squaring}]$$

$$c^2 = 169 \quad [1 \text{ mark - adding}]$$

$$c = \sqrt{169}$$

$$c = 13 \text{ cm} \quad [1 \text{ mark - final answer}]$$

Question 15: Circular Garden - Circumference and Area

[6 marks marks]

(a) Find the circumference

$$\text{Radius } (r) = 7 \text{ m}$$

$$\text{Circumference} = 2\pi r \quad [1 \text{ mark - formula}]$$

$$= 2 \times 22/7 \times 7$$

$$= 2 \times 22 \times (7/7)$$

$$= 2 \times 22$$

$$= 44 \text{ m} \quad [1 \text{ mark - final answer}]$$

(b) Find the area (Use $\pi = 22/7$)

$$\text{Area} = \pi r^2 \quad [1 \text{ mark - formula}]$$

$$= 22/7 \times 7^2$$

$$= 22/7 \times 49 \quad [1 \text{ mark - squaring radius}]$$

$$= (22 \times 49) / 7$$

$$= 22 \times (49/7) \quad [1 \text{ mark - simplifying}]$$

$$= 22 \times 7$$

$$= 154 \text{ m}^2 \quad [1 \text{ mark - final answer}]$$

Question 16: Map Scale and Speed Calculation

[6 marks marks]

(a) Find the actual distance between the towns

Map scale: 1 cm represents 5 km

Distance on map = 8.4 cm

$$\text{Actual distance} = 8.4 \times 5 \quad [1 \text{ mark - using scale}]$$

$$= 42 \text{ km} \quad [1 \text{ mark - calculation}]$$

✓ **Final answer: 42 km (3 marks total for part a)**

(b) Time taken at 60 km/h

$$\text{Time} = \text{Distance} / \text{Speed} \quad [1 \text{ mark - formula}]$$

$$= 42 / 60$$

$$= 0.7 \text{ hours} \quad [1 \text{ mark - calculation}]$$

Converting to minutes: $0.7 \times 60 = 42$ minutes

✓ **Final answer: 0.7 hours or 42 minutes (3 marks total for part b)**

Question 17: Probability with Colored Balls

[6 marks marks]

(a) Probability of picking a blue ball

$$\text{Total balls} = 5 + 3 + 2 = 10 \text{ balls} \quad [1 \text{ mark - counting total}]$$

$$\text{Blue balls} = 3$$

$$P(\text{blue}) = 3/10 \quad [1 \text{ mark - probability}]$$

(b) Probability of picking a red or green ball

$$\text{Red balls} = 5, \text{ Green balls} = 2$$

$$\text{Red or green} = 5 + 2 = 7 \text{ balls} \quad [1 \text{ mark - counting favorable outcomes}]$$

$$P(\text{red or green}) = 7/10 \quad [2 \text{ marks - probability and answer}]$$

$$\checkmark \text{ Alternative: } P(\text{red or green}) = 1 - P(\text{blue}) = 1 - 3/10 = 7/10$$

Question 18: Measures of Central Tendency

[6 marks marks]

Data: 2, 3, 4, 4, 5, 6, 6, 6, 7

(a) Find the mode

Mode = most frequently occurring value

Value 6 appears 3 times (more than any other)

$$\checkmark \text{ Mode} = 6 \text{ (1 mark)}$$

(b) Find the median

Data in order: 2, 3, 4, 4, 5, 6, 6, 6, 7

Number of values = 9 (odd number) [1 mark]

Median position = $(9 + 1) / 2 = 5\text{th value}$ [1 mark]

Median = 5 [counting]

$$\checkmark \text{ Median} = 5 \text{ (2 marks total)}$$

(c) Find the mean

Mean = Sum of values / Number of values [1 mark - formula]

$$\text{Sum} = 2 + 3 + 4 + 4 + 5 + 6 + 6 + 6 + 7$$

$$= 43 \quad [1 \text{ mark - calculating sum}]$$

$$\text{Mean} = 43 / 9$$

$$= 4.78 \text{ (to 2 d.p.) or } 47/9 \text{ (as fraction)}$$

$$\checkmark \text{ Mean} = 4.78 \text{ or } 43/9 \text{ (3 marks total for part c)}$$