

INSTRUCTIONS: ANSWER ALL QUESTIONS**TIME: (1 HR 30 MINS)**

1. The sum of the first 3 terms of a geometric series is 26. If the common ratio is 3. Find the sum of the first 6 terms. (3 mks)

$$S_n = a \frac{(r^n - 1)}{r - 1} m_1$$

$$26 = a \frac{(3^3 - 1)}{2}$$

$$a = 2 m_1$$

$$S_6 = 2 \frac{(3^6 - 1)}{2}$$

$$= \underline{\underline{728}} m_1$$

2. a. Use matrix method to solve the following simultaneous equation. (3 mks)

$$x - 2y = 4$$

$$2x + y = 3$$

$$\begin{pmatrix} 1 & -2 \\ 2 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 4 \\ 3 \end{pmatrix}$$

$$\text{Det} = 1 - (-4) = 5$$

$$\frac{1}{5} \begin{pmatrix} 1 & 2 \\ -2 & 1 \end{pmatrix} \begin{pmatrix} 1 & -2 \\ 2 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{5} \begin{pmatrix} 12 & 4 \\ 2 & 3 \end{pmatrix} \begin{pmatrix} 4 \\ 3 \end{pmatrix} m_1$$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} \frac{1}{5} & \frac{2}{5} \\ -\frac{2}{5} & \frac{1}{5} \end{pmatrix} \begin{pmatrix} 4 \\ 3 \end{pmatrix} m_1$$

$$x = \frac{1}{5} \times 4 + \frac{2}{5} \times 3 = 2 m_1$$

$$y = -\frac{2}{5} \times 4 + \frac{1}{5} \times 3 = -1 m_1$$

b. Given $P = \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix}$, $Q = \begin{bmatrix} 2 & 0 \\ 1 & 3 \end{bmatrix}$ and $R = \begin{bmatrix} 3 & 0 \\ 2 & 2 \end{bmatrix}$ find:

PQR. (3 mks)

$$PQ = \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix} \begin{bmatrix} 2 & 0 \\ 1 & 3 \end{bmatrix} = \begin{bmatrix} 4 & 6 \\ 4 & 12 \end{bmatrix} = \begin{bmatrix} 24 & 12 \\ 36 & 24 \end{bmatrix}$$

$$PQR = \begin{bmatrix} 4 & 6 \\ 4 & 12 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 2 & 2 \end{bmatrix} = \begin{bmatrix} 24 & 12 \\ 36 & 24 \end{bmatrix}$$

$\frac{1}{2}Q + P$. (3 mks)

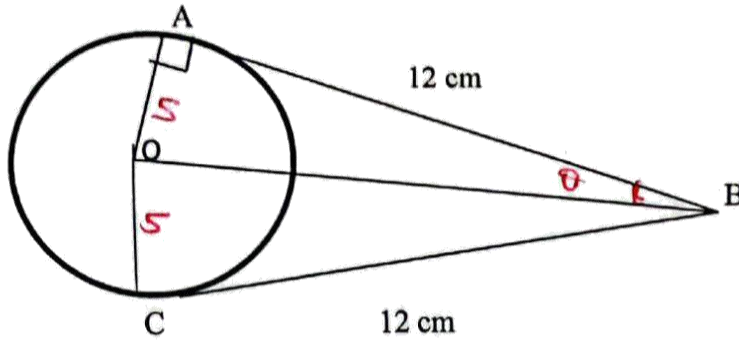
$$\frac{1}{2}Q = \frac{1}{2} \begin{bmatrix} 2 & 0 \\ 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & \frac{3}{2} \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & \frac{3}{2} \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 0 & 4 \end{bmatrix}$$

$$= \underline{\underline{\begin{bmatrix} 2 & 2 \\ \frac{1}{2} & \frac{11}{2} \end{bmatrix}}}$$

3. In the figure below the tangent AB and BC are 12 cm long, with O as the centre of the circle and the radius 5 cm. Find



a. OB

$$OB = \sqrt{12^2 + 5^2} = \sqrt{169} = 13$$

b. Angle ABC

$$\tan \theta = \frac{5}{12}$$

$$\theta = \tan^{-1}\left(\frac{5}{12}\right) = 22.62^\circ$$

$$\begin{aligned} \angle ABC &= 2 \times 22.62 \\ &= \underline{\underline{45.24^\circ}} \end{aligned}$$

4. The cash price of a phone is sh 9000. A customer bought the phone by paying 15 monthly installments of 950 each. Calculate the carrying charge and the rate of compound interest (4 mks). Use deposit of 2,500

$$C.P \Rightarrow 9000$$

$$15 \times 950 = 14250$$

$$\begin{aligned} H.P.P &= 14250 + 2500 \\ &= \text{Sh. } 16750 \end{aligned}$$

$$\text{Interest} = 16750 - 9000$$

$$\text{C. charge} = \text{Sh. } 7750$$

$$A = P\left(1 + \frac{r}{100}\right)^n$$

$$14250 = 6500\left(1 + \frac{r}{100}\right)^{15}$$

$$2.1923 = \left(1 + \frac{r}{100}\right)^{15}$$

$$\left(2.1923\right)^{\frac{1}{15}} = 1 + \frac{r}{100}$$

$$1.17 = 1 + \frac{r}{100}$$

$$0.17 = \frac{r}{100}$$

$$r = \underline{\underline{17\%}}$$

5. Find the equation of a circle of centre (2,1) and radius $\sqrt{13}$. (2 mks)

$$\begin{aligned} C.C(2,1), r &= \sqrt{13} \quad M_1 \\ (x-h)^2 + (y-k)^2 &= r^2 \\ (x-2)^2 + (y-1)^2 &= (\sqrt{13})^2 \end{aligned} \quad \left| \begin{aligned} x^2 - 4x + 4 + y^2 - 2y + 1 &= 13 \\ x^2 + y^2 - 4x - 2y &= 8 \quad M_1 \end{aligned} \right.$$

6. Find the value of y. (3 mks)

$$2 + \log 3 + \log y = \log 5 + 1$$

$$1 + \log 3 + \log y = \log 5$$

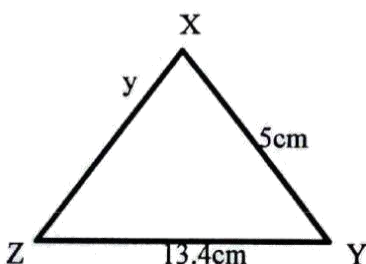
$$1 = \log 10 \quad M_1$$

$$\begin{aligned} \log 10 + \log 3 &= \log 5 - \log y \quad M_1 \\ \log(10 \times 3) &= \log\left(\frac{5}{y}\right) \\ 30 = \frac{5}{y} & \quad y = \frac{5}{30} = \frac{1}{6} \end{aligned}$$

$$y = \frac{1}{6} \quad M_1$$

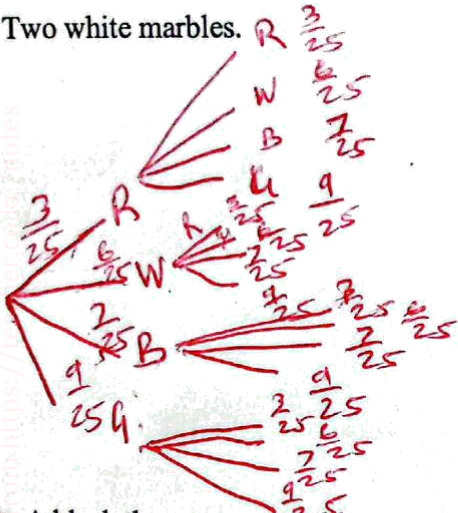
7. Find the values of x, y and z in the following triangles

(4 mks)



8. Two marbles are picked in turn with replacement from a pack containing three red marbles, six white marbles, 7 black marbles and 9 green marbles. Using a tree diagram, determine the probability of picking: (5 mks)

a. Two white marbles.



$$\frac{6}{25} \times \frac{6}{25} = \frac{36}{625}$$

b. A black then a green marble.

$$\frac{7}{25} \times \frac{9}{25} = \frac{63}{625}$$

c. No red marble.

(WW or WB or WB) or (BW or BB or BB) or (GW or GB or GB)

9. The resistance to the motion of a bicycle is partly constant and partly varies as the square of the speed. The resistance is 265 N when the speed 20 km/h and 365 N when the speed is 30 km/h. Find the resistance when the speed is 35 km/h. (4 mks)

Let resistance be R & Speed be S.

$$R \propto S^2 + C$$

$$R = kS^2 + C$$

$$265 = 400k + C \quad M_1$$

$$365 = 900k + C$$

$$-100 = -500k$$

$$k = \frac{1}{5} M_1$$

$$C = 265 - 400\left(\frac{1}{5}\right) = 185 M_1$$

$$S = 35 \text{ km/hr}$$

$$R = \frac{1}{5} \times 35^2 + 185$$

$$= 430$$

$$R = \underline{\underline{430 \text{ N}}}$$

10. Using Pascal's triangle expand the following. (4 mks)

$$a. (P+Q)^6$$

$$= {}^6C_0(P+Q)^0 + {}^6C_1(P+Q)^1 + {}^6C_2(P+Q)^2 + {}^6C_3(P+Q)^3 + {}^6C_4(P+Q)^4 + {}^6C_5(P+Q)^5 + {}^6C_6(P+Q)^6 M_1$$

$$= P^6 + 6P^5Q + 15P^4Q^2 + 20P^3Q^3 + 15P^2Q^4 + 6PQ^5 + Q^6 M_1$$

$$= P^6 + 6P^5Q + 15P^4Q^2 + 20P^3Q^3 + 15P^2Q^4 + 6PQ^5 + Q^6 M_1$$

$$b. (2x+3y)^6$$

$$= {}^6C_0(2x)^0(3y)^6 + {}^6C_1(2x)^1(3y)^5 + {}^6C_2(2x)^2(3y)^4 + {}^6C_3(2x)^3(3y)^3 + {}^6C_4(2x)^4(3y)^2 + {}^6C_5(2x)^5(3y)^1 + {}^6C_6(2x)^6(3y)^0 M_1$$

$$= 64x^6 + 96x^5y + 144x^4y^2 + 216x^3y^3 + 324x^2y^4 + 486xy^5 + 729y^6$$

$$= 64x^6 + 576x^5y + 2160x^4y^2 + 4320x^3y^3 + 4860x^2y^4 + 2916xy^5 + 729y^6 M_1$$

11. The length of an arc of a circle is 11.0 cm. Find the radius of this circle if the arc subtends 90° at the centre of the circle. (3 mks)

$$l = \frac{90}{360} \times 2\pi r \quad M_1$$

$$\frac{44}{2\pi} = r, \quad r = 7 \text{ cm} \quad M_1$$

12. Express in surd form and simplify $\frac{1+\cos 30^\circ}{1-\sin 60^\circ}$ (3 mks)

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \quad M_1$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\left| \frac{\left(1 + \frac{\sqrt{3}}{2}\right)\left(1 + \frac{\sqrt{3}}{2}\right)}{\left(1 - \frac{\sqrt{3}}{2}\right)\left(1 + \frac{\sqrt{3}}{2}\right)} \right| \quad M_1$$

$$= \frac{1 + 2\frac{\sqrt{3}}{2} + \frac{3}{4}}{1 - \frac{3}{4}} = \frac{7 + 4\sqrt{3}}{4}$$

$$= \frac{7 + 4\sqrt{3}}{4} \times 4 = \underline{\underline{7 + 4\sqrt{3}}} \quad M_1$$

13. The temperature of a body is measured and recorded as 29.5°C . Find the percentage error. (3 mks)

$$29.5^\circ\text{C}$$

$$A.E = \frac{0.1}{2} = 0.05 \quad M_1$$

$$29.55 - 29.5 = 0.05$$

$$29.5 - 29.45 = 0.05 \quad M_1$$

$$A.E = \frac{0.05 + 0.05}{2} = 0.05$$

$$\% E = \frac{0.05}{29.5} \times 100\%$$

$$= \underline{\underline{0.17\%}} \quad M_1$$