## MATHEMATICS

FORM 4
PAPER 2
END OF TERM 22022
TIME: $21 / 2$ HOURS

## INSTRUCTIONS.

## Answer all the questions in the spaces provided.

## SECTION 1 (50mks)

1. The sum of $n$ terms of the sequence:
$3,9,15,21 \ldots$ Is 7500
a) Find the $20^{\text {th }}$ term of the sequence.
(2mks)
b) Determine the value of $n$.
2. A quadratic curve passes through the points $(-2,0)$ and $(1,0)$. Find the equation of the curve in the form $y=a x^{2}+b x+c$, where $a, b$ and $c$ are constants.
3. Make $h$ the subject of the formula.
$\mathrm{q}=\frac{1+\mathrm{rh}}{1-\mathrm{ht}}$
4. $P(1,2)$ and $Q(9,8)$ are the points on the ends of the diameter of a circle. Write down in terms of $x$ and $y$ the equation of the circle in the form: $a x^{2}+b y^{2}+x+y+c=0$.
5. In the figure below, $O$ is the centre of the circle and $A T$ is a tangent to the circle at $A$. $A T=2 \sqrt{6} \mathrm{~cm}$ and $\mathrm{DT}=4 \mathrm{~cm}$.


Determine:
a) OA
(2mks)
b) The value of angle AOB
(2mks)
6. In a transformation, an object with an area of $5 \mathrm{~cm}^{2}$ is mapped onto an image whose area is $30 \mathrm{~cm}^{2}$. Given that the matrix of the transformation is $x \quad x-1$
a) Find the value of $x$.
(2mks)
b) Hence determine the inverse of the matrix $\left(\begin{array}{cc}x & x-1 \\ 2 & 4\end{array}\right)$
7. The co-ordinates of $P$ are $(0,7)$ and Q are $(3.5,1.4)$. A point $S$ divides $P Q$ externally in the ratio 9:2. Find the co-ordinates of S.
8. The top of a coffee table is a regular hexagon. Each side of the hexagon measures 50.0 cm , find the percentage error in calculating the perimeter of the top of the table.
(3mks)
9. The figure below represents a cuboid $\mathrm{ABCDEFGH} . \mathrm{AB}=60 \mathrm{~cm}, \mathrm{BC}=11 \mathrm{~cm}$ and $\mathrm{CH}=10 \mathrm{~cm}$.

10. Expand and simplify the expression $\left(4 x-\frac{y}{2}\right)^{5}$ up to the third term.
b. Hence use the expansion in (a) above to approximate the value of $(39.6)^{5}$ correct to 3 significant figures. (2mks)
11. A solution was gently heated, its temperature readings taken at intervals of 1 minute and recorded as shown in the table below:

| Time (min) | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Temperature <br> $\left({ }^{\circ} \mathrm{C}\right)$ | 4 | 5.2 | 8.4 | 14.3 | 16.8 | 17.5 |

a) On the grid provided below, draw the time - temperature graph.
(2mks)

b) Use the graph to find the average rate of change in temperature between $\mathrm{t}=1.8$ and $\mathrm{t}=3.4$. (2mks)
12. The shortest distance between two points $\mathrm{A}\left(40^{\circ} \mathrm{N}, 20^{\circ} \mathrm{W}\right)$ and $\mathrm{B}\left(\theta^{\circ} \mathrm{S}, 20^{\circ} \mathrm{W}\right)$ on the surface of the earth is 8008 km . given that the radius of the earth is 6370 km , determine the position of B. (Take $\pi={ }^{22} / 7$ ).
(3mks)
13. Simplify $\frac{\sqrt{3}}{\sqrt{3-\sqrt{2}}}$
(2mks)
14. The table below shows income tax rates in a certain year.

| Monthly income in Kshs. | Tax rate in each shilling |
| :--- | :--- |
| Up to 9680 | $10 \%$ |
| From 9681 to 18800 | $15 \%$ |
| From 18801 to 27920 | $20 \%$ |
| From 27921 to 37040 | $25 \%$ |
| Over 37040 | $30 \%$ |

In that year, a monthly personal tax relief of ksh. 1056 was allowed. Calculate the monthly income tax paid by an employee who earned a monthly salary of kshs. 32,500.
15. Three types of beverages are mixed in the ration 1:3:5 respectively. Type A costs sh 26 , type B costs sh 28 and type C sh 32 , per packet. Find the cost of the mixture per packet.
(3mks)
16. The gradient of a curve is given by $\frac{d y}{d x}=x^{2}-4 x+3$. The curve passes through the point $(1,0)$. Find the equation of the curve.
(3mks)

## SECTION II (50MKS)

17. The hire purchase (H.P) price of an electronic device was ksh. 276,000. A deposit of ksh 60,000 was paid followed by 18 equal monthly installments.
a) Calculate the monthly installment.
b) The cash price of the electronic device was $10 \%$ less than the hire purchase (H.P) price. Calculate the cash price.
(2mks)
c) Madam Kanini decided to buy the electronic device in cash. She was allowed a 5\% discount on the cash price, she took a bank loan to buy the device. The bank charged compound interest on the loan at the rate of $20 \%$ p.a. the loan was repaid in 2 years.
i. Calculate the amount repaid to the bank by the end of the second year.
(3mks)
ii. Express as a percentage of the hire purchase (HP) price, the difference between the amount repaid to the bank and the hire purchase price.
(3mks)
18. An examination involves a written test and a practical test. The probability that a candidate passes the written test is $\% / 11$. If the candidate passes the written test, then the probability of passing the practical test is $3 / 5$, otherwise it would $\mathrm{be}^{2} / 7$.
a) Illustrate this information on a tree diagram.
(2mks)
b) Determine the probability that a candidate is awarded:
i. For passing both tests.
ii. For passing the written test.
(2mks)
c) Determine the probability that the candidate;
i. Passes one test.
(2mks)
ii. Fails for not passing the written test.
(2mks)
19. Construct triangle PQR with $\mathrm{PQ}=7.2 \mathrm{~cm}, \mathrm{QR}=6 \mathrm{~cm}$ and $\angle \mathrm{PQR}=48^{\circ}$.
(3mks)
a) The locus L 1 , of points equidistant from P and Q and Locus L 2 of points equidistant from P and $R$, meet at M. Locate $M$ hence measure QM. (4mks)
b) A point X moves within triangle PQR such that $\mathrm{QX} \geq \mathrm{QM}$. Shade and label the locus of X . (3mks)
20. Triangle $P Q R$ shown on the grid below has vertices $P(5,5), Q(10,10)$ and $R(10,15)$

a. Find the coordinates of the points $\mathrm{P}^{\prime} \mathrm{Q}^{\prime}$ and $\mathrm{R}^{\prime}$ the images of $\mathrm{P}, \mathrm{Q}$ and R respectively under transformation M whose matrix is $-0.6\left[\begin{array}{cc}0.8 & \\ 0.8 & 0.6\end{array}\right) \quad$ (3mks)
a) Given that M is a reflection:
i. Draw triangle $P^{\prime} Q^{\prime} R^{\prime}$ and the mirror line of the reflection.
(2mks)
ii. Determine the equation of the mirror line of the reflection.
(2mks)
b) Triangle $P^{\prime \prime} Q^{\prime \prime} R$ " is the image of triangle $P^{\prime} Q^{\prime} R^{\prime}$ under reflection $N$, where $N$ is a reflection in the Y-axis.
i. Determine triangle $\mathrm{P}^{\prime \prime} \mathrm{Q}^{\prime \prime} \mathrm{R}^{\prime \prime}$ (1mk)
ii. Determine a $2 \times 2$ matrix equivalent to the transformation NM.
(2mks)
21. In the figure below, $P R$ is the diameter of the circle with centre $O$. Points $P, Q, R$ and $S$ are on the circumference of the circle. Angle $\mathrm{PRQ}=72^{\circ}, \mathrm{QS}=\mathrm{QP}$ and line USV is a tangent to the circle at S . Giving reasons, calculate the size of:

i. $\angle \mathrm{QPR}$ (2 marks)
ii. $\angle \mathrm{PQS}$ (2 marks)
iii. $\angle O Q S$ (2 marks)
iv. $\angle \mathrm{RTS}$ (2 marks)
v. $\angle \mathrm{RSV}$ (2 marks)
22. Three quantities $R, S$ and $T$ are such that $R$ varies directly as $S$ and inversely as the square of $T$.
a) Given that $\mathrm{R}=480$ when $\mathrm{S}=150$ and $\mathrm{T}=5$, write an equation connecting $\mathrm{R}, \mathrm{S}$ and T .
(4mks)
b) (i) Find the value of R when $\mathrm{S}=360$ and $\mathrm{T}=1.5$.
(2mks)
(ii) Find the percentage change in R if s increase by $5 \%$ and T decreases by $20 \%$. (4mks)
23. For a C B C inservice training course for teachers, at least four (4) but not more that nine(9) teachers are to be chosen per school. The ratio of the number of male teachers to the number of female teachers must be less than $2: 1$ and there must be more males than females. If $x$ and $y$ represent the number of male teachers and female teachers respectively:
a) Write down in their simplest form the inequalities that x and y must satisfy.
b) On the gird provided below, represent the inequalities on the graph.

c) Use the graph to determine the composition of the training group of:
i. The largest size.
ii. The smallest size.
(1mk)
24. The equation of a curve is given by $y=5 x-1 / 2 x^{2}$.

a) On the grid provided below, draw the curve of $y=5 x-1 / 2 x^{2}$ for $0 \leq x \leq 6$. (3mks)
b) By integration, find the area bounded by the curve, the line $x=6$ and the $x$-axis. (3mks)
c) On the same grid, draw the line $y=2 x$.
d) Determine the area bounded by the curve and the line $\mathrm{y}=2 \mathrm{x}$.
